

# Overview of meeting

Locomotion and Manipulation are related to each other. Both are heavily based on controlling physical interaction with an environment; both are ruled by the same laws of motion and contact; and both are subject to the same constraints and limitations imposed by our models of those laws. Despite these similarities, there exists a current dichotomy in techniques for approaching planning, control, perception, and design for locomotion and manipulation.

Part of the specialization can be attributed to the assumptions they respectively make, either (a) about the nature of the interactions with the environment, for example ranging from the spaced and periodic in time to the continuous, and from the localized in space to the distributed; or (b) the nature of the uncertainty, either in the state of the robot or the environment. Many of the grand challenges that both fields face require, pushing the boundaries of those assumptions. In this workshop we would like to explore in depth the reasons for these differences and come up with ideas to bring them closer together.

The workshop will consist of invited talks, breakout sessions, and discussion panels to initiate a conversation between the two communities, identify tools and algorithms from locomotion with potential application in manipulation and vice versa, and create a summary document with relevant research topics at the intersection of locomotion and manipulation.

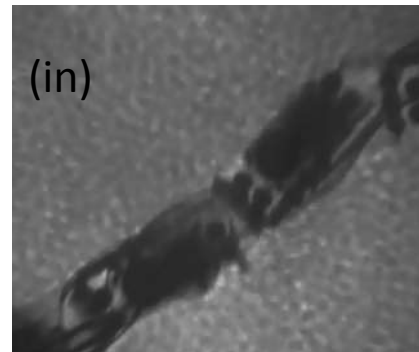
# Locomotion & Manipulation: Why the Great Divide?

Session 2: High Dimensional Locomotion and Manipulation

## Locomotion and manipulation **on, in, and of** deformable granular media

Prof. Daniel I. Goldman

School of Physics  
Georgia Institute of Technology



FUNDING

NSF CAREER/PECASE, NSF PoLS, DARPA YFA, BWF, Blanchard Milliken, ARL, ARO

# A plea for humility...



There are more things in heaven and  
earth, Horatio,  
Than are dreamt of in your **ROBOTICS**  
- *Hamlet* (1.5.167-8), Hamlet to Horatio

# Questions from the organizers

State-of-the-art methods for locomotion and manipulation can be pushed to deal with systems up to 50 DOF, which is fairly impressive compared to what we could achieve just a few years ago.

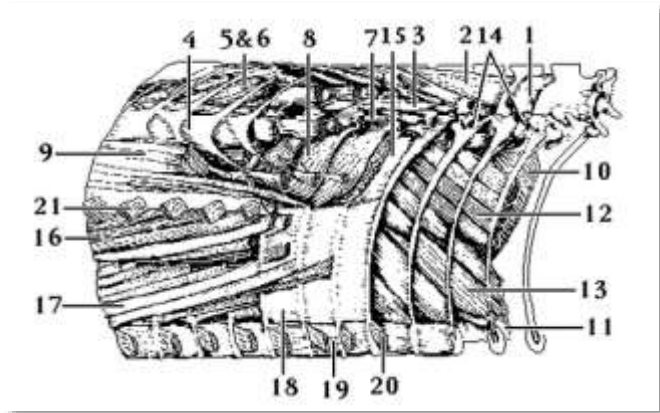
- How can we push this dimensionality even further, perhaps all the way to infinity?
- How do we locomote with soft structures?
- How do we manipulate deformable objects?
- How do we plan and control continuum robots?
  - Templates (low DOF control targets) to manipulate the body and environment to effect locomotion

# Physics of Locomoting Systems

Study of the *emergence* of movement resulting from **many** degree of freedom, hierarchically organized, nonlinear biological & robotic systems interacting **effectively** with their **environments**

Going from *many* internal DOF to behavior is hard!

Search for **low order control templates** (Full & Koditschek, 1999)  
and general principles for effective  
**environmental interaction** (manipulation?)



(J.P. Gasc, 1974, Cundall, 1987)



Howie Choset, CMU, 2001...

# Locomotor-environment interaction

~~Terrestrial~~

~~Aerial~~

~~Aquatic~~



Forbes online



Prof. Howie Choset, CMU

TECH | NOVEMBER 2, 2011 | 5,412 views

## Robotic Snakes Slither Their Way Into Ancient Archaeology

[Comment Now](#) [Follow Comments](#)

To paraphrase REM, the ancient Egyptians were all too familiar with the "horrible asp."

But not even the most clairvoyant pharaohs could have imagined their kingdoms invaded by robotic snakes.

In arguably an archaeological first, that's exactly what happened a



*Search and rescue*



*IED detection*



*Exploration*



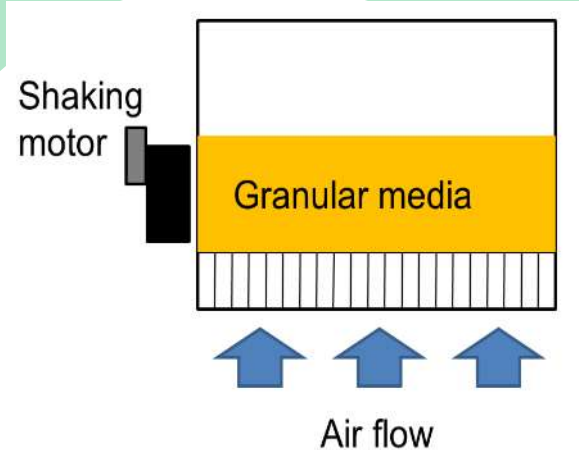
# Discover principles of terrestrial locomotion

goldmanlab.gatech.edu

Bio/neuromechanics



Substrate control

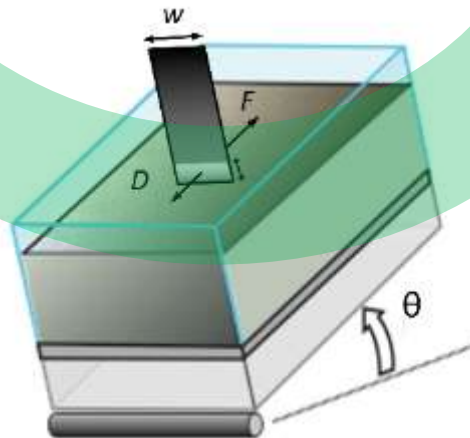


Physical models  
"robophysics"

Aguilar et al, *Rep. Prog. Physics*, in prep.



Soft matter interaction physics



Yuma, AZ, USA



Dr. Hamid  
Marvi,  
now  
postdoc  
CMU



**Sidewinder**

*Crotalus cerastes*





# Sidewinding snakes

Slowed 5x

Sidewinding only occurs in snakes that move on loose material

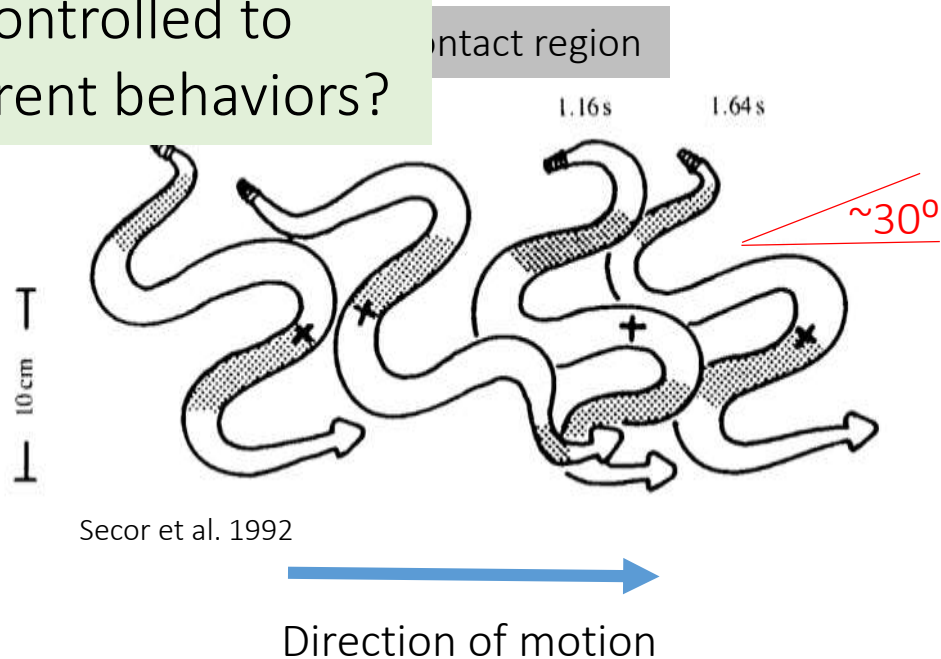


Why use this gait?

How is it controlled to generate different behaviors?

Studies of straight sidewinding on hard ground (1 on flat sand)

- Qualitative description  
Mosauer (1930) and Gray (1946)
- Kinematics, muscular mechanisms  
Jayne (1986, 1988)
- Energetics  
Secor, et al. (1992)
- Robotics  
Burdick et al. (1995), Hatton et al. (2010)



# *Crotalus cerastes*, Sidewinder rattlesnake

( $N = 6$ , mass=  $98 \pm 18$  g, body-length, tip-to-tail,  $L = 48 \pm 6$  cm)



Surprisingly good study subject! They move on “command”

# Facility at Zoo Atlanta

Dr. Hamid  
Marvi,  
postdoc CMU



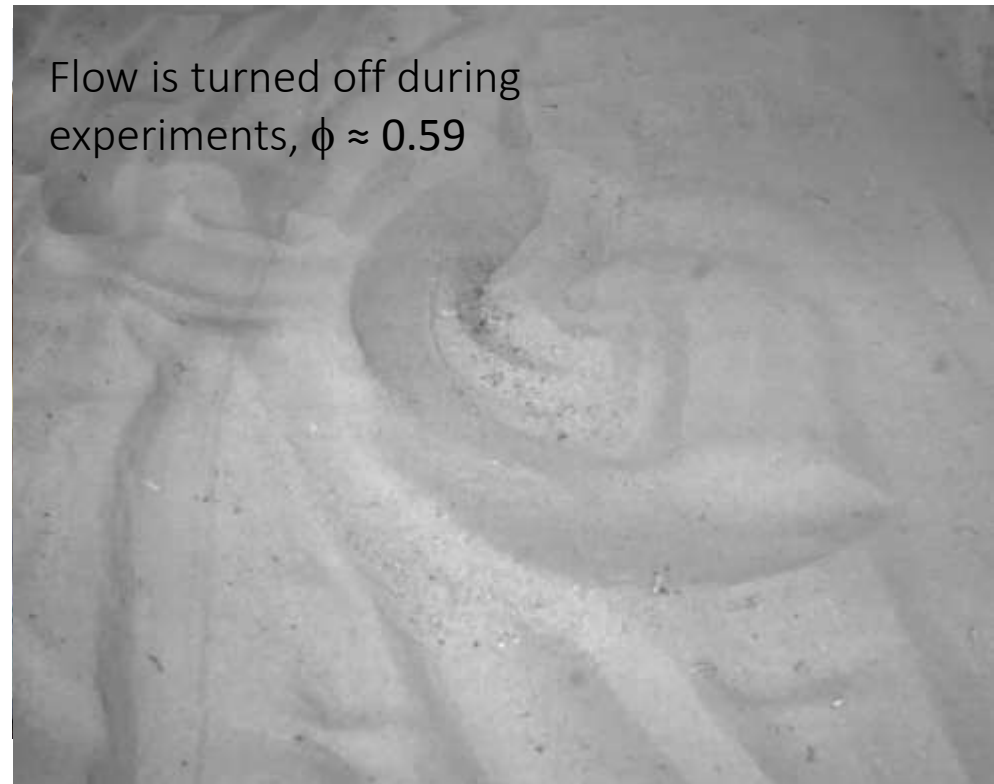
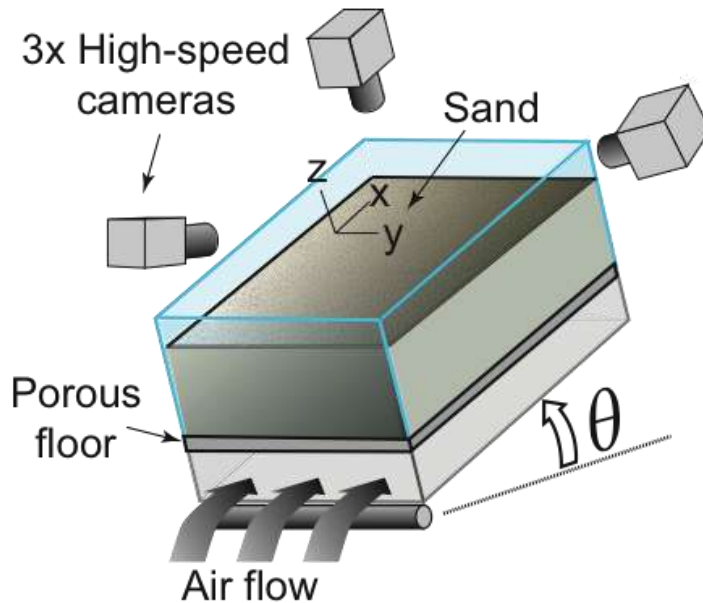
Dr. Henry  
Astley,  
postdoc GT



Prof.  
David Hu,  
ME, GT



Dr. Joe  
Mendelson,  
Zoo ATL

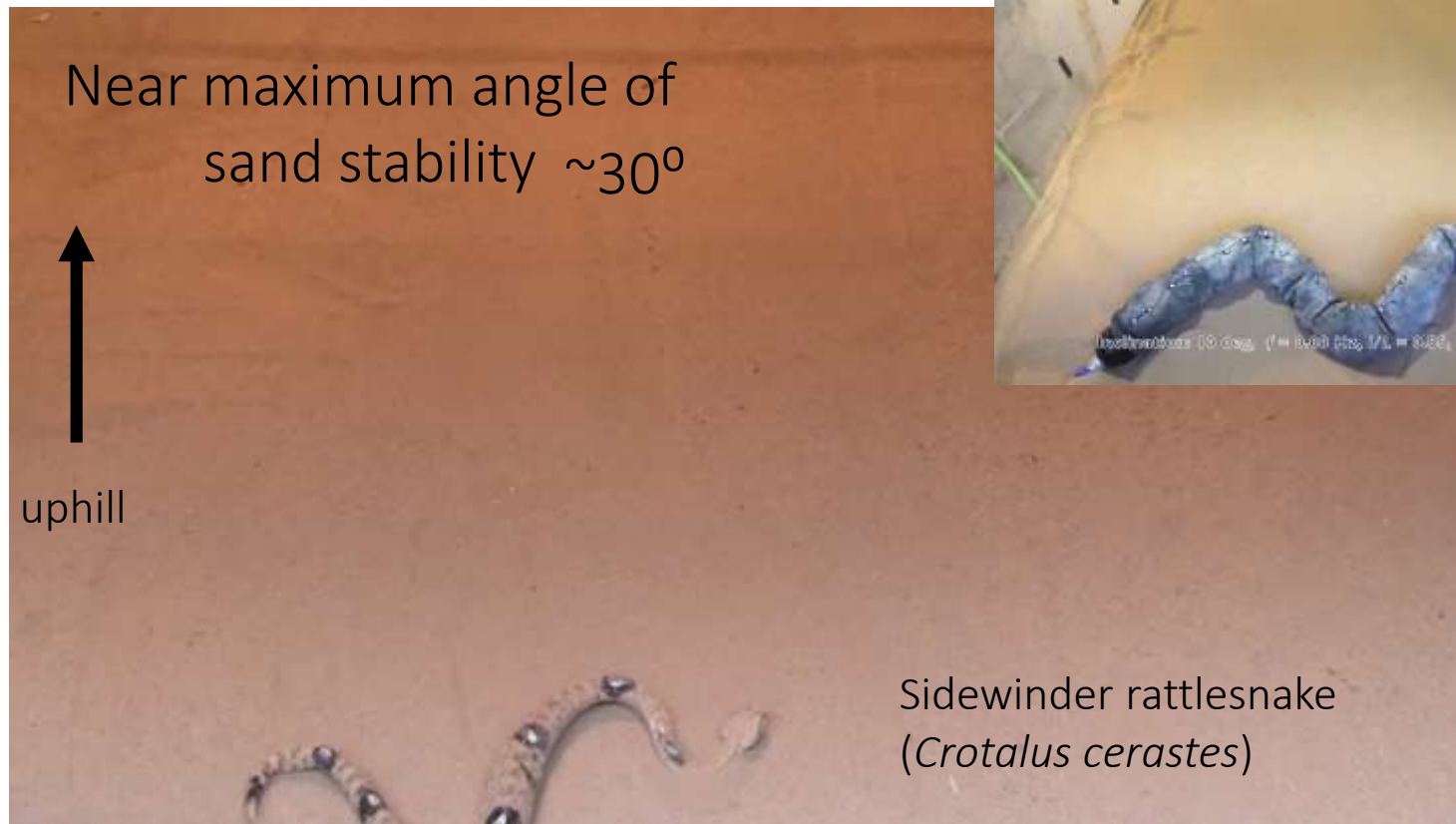


**Air-fluidized bed:** A ground control system to create smooth surface, set volume fraction ( $\phi$ ) and **inclination angle,  $\theta$**

# Substrate manipulation through contact length modulation to remain below yield stress enables effective locomotion

Marvi, Gong, Gravish, Astley, Travers, Hatton Mendelson,  
Choset, Hu, Goldman, *Science*, 2014

Modsnake



# Manipulate the ground to generate a solid state during a step

## Sidewinder rattlesnake

Marvi, et al, *Science*, 2014

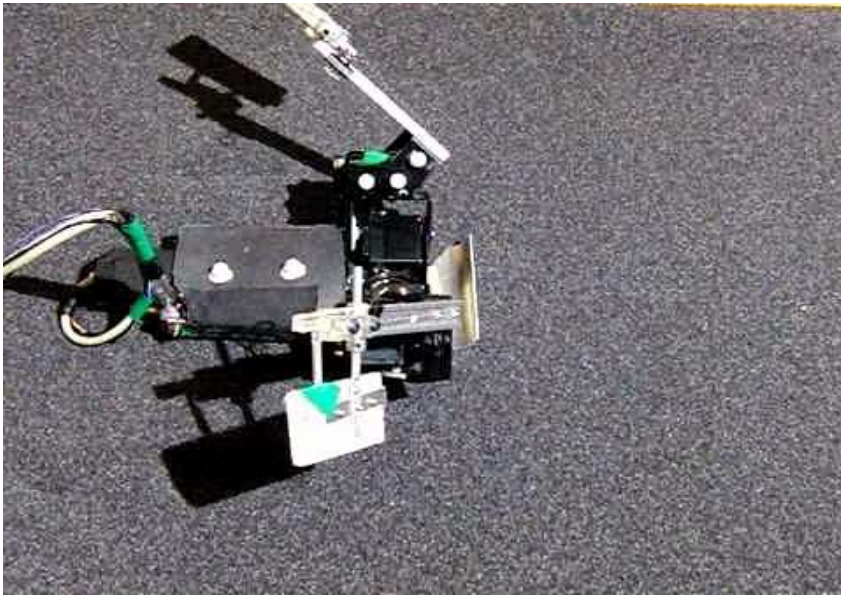


Mazouchova, Gravish, Savu, DIG, *Biology Letters*, 2010



## FlipperBot

Mazouchova, Umbanhowar, DIG, *Bioinspiration & Biomimetics*, 2013



## SandBot (mini RHex)

Li, Komsuoglu, Umbanhowar, Koditschek, DIG, *PNAS*, 2009





Related snakes (vipers) are challenged by GM, sidewinding not common



Dr. Henry Astley,  
postdoc GT

10 degree sand inclines

Dr. Joe Mendelson,  
Zoo ATL

*Agkistrodon piscivorus*

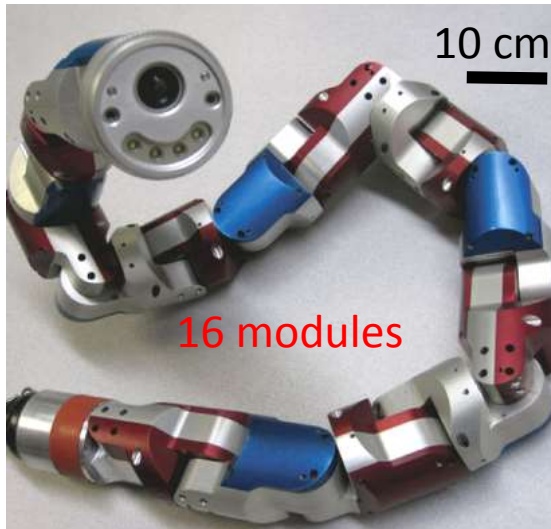
*Crotalus willardi*

*Sistrurus catenatus*

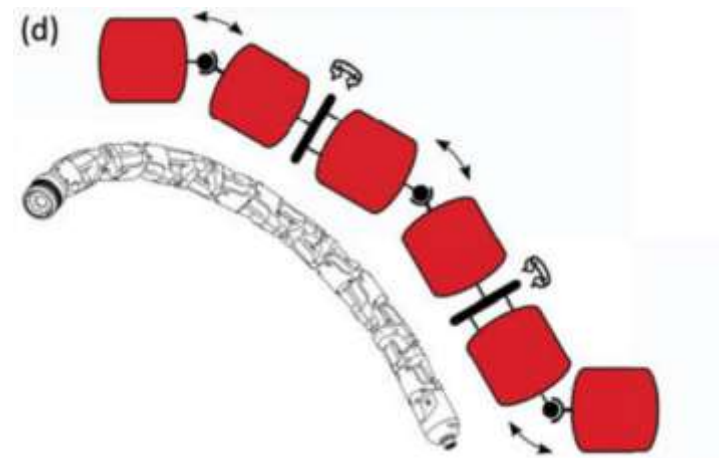
# Sidewinding robot, a physical model of the snakes

*Modsnake*

Prof. Howie Choset, Carnegie Mellon U

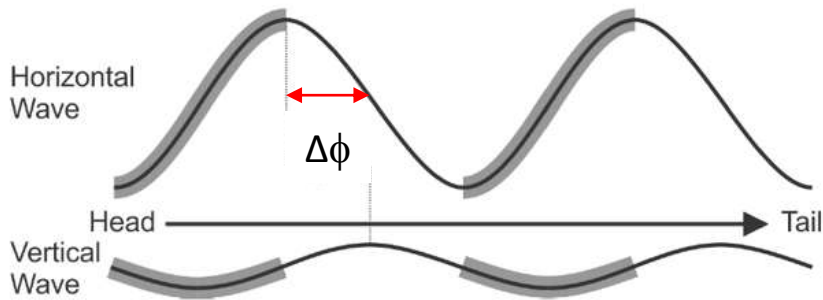


Command joint angles vs time to execute sidewinding gait

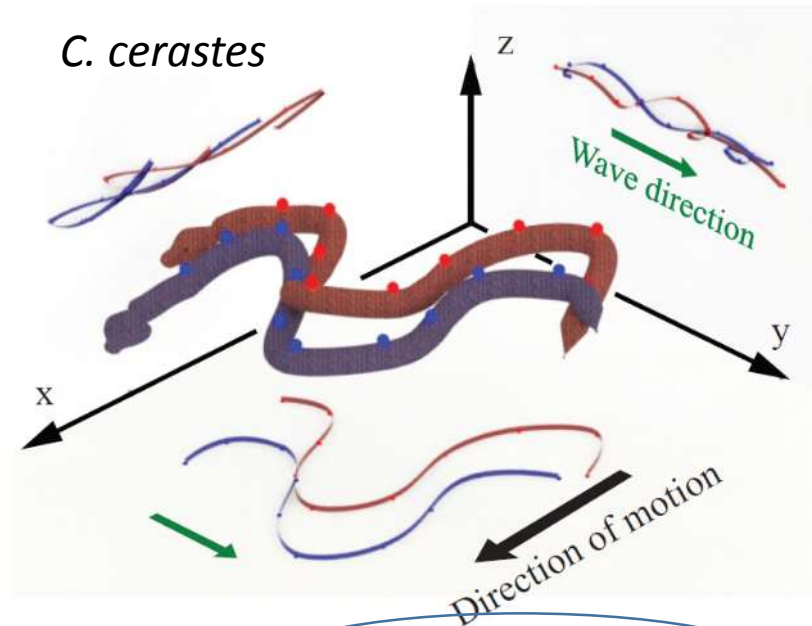
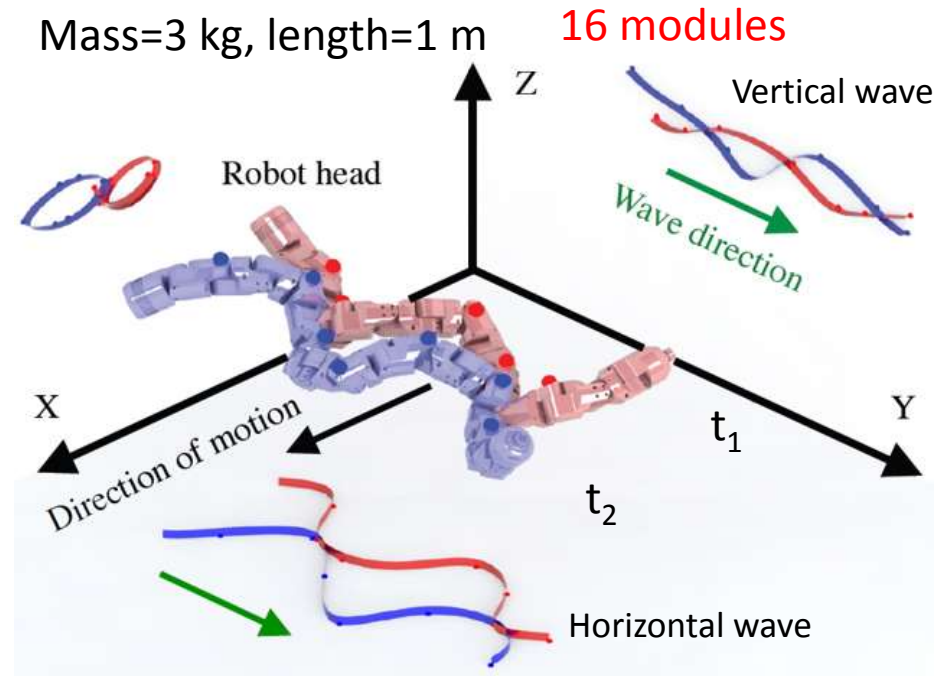


Sidewinding **template**:  
 appropriate mixture of 2  
 orthogonal body waves

**Sidewinding robot**: Command  
 $\Delta\phi = \pi/2$  phase difference between  
 vertical and horizontal waves



(schematic of shape of robot  
 in two projections/planes at a  
 time instant, gray=contact region)



(in snakes  $\Delta\phi = 1.51 \pm 0.17$  rad)



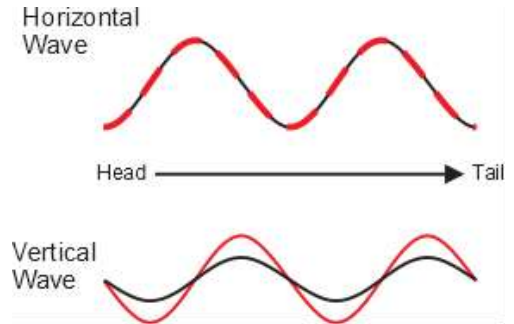
# Modulating the template to manipulate shape to move in the real world

Astley, Gong, Dai, Travers, Serrano, Vela, Choset, Mendelson, Hu, Goldman, *PNAS*, 2015

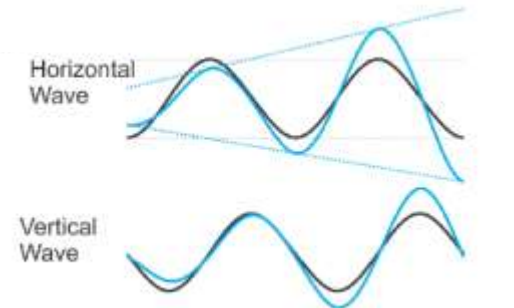
Marvi, Gong, Gravish, Astley, Travers, Hatton, Mendelson, Choset, Hu, Goldman, *Science*, 2014



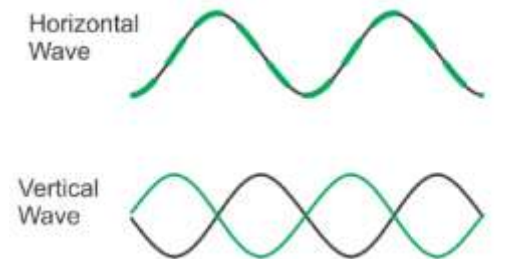
- Sandy slope ascent: modulate **amplitude** of vertical wave to generate contact length that minimizes slip by remaining below yield stress



- Slow turn (“differential”): modulate **amplitude** of horizontal wave to create differential amplitude from head to tail



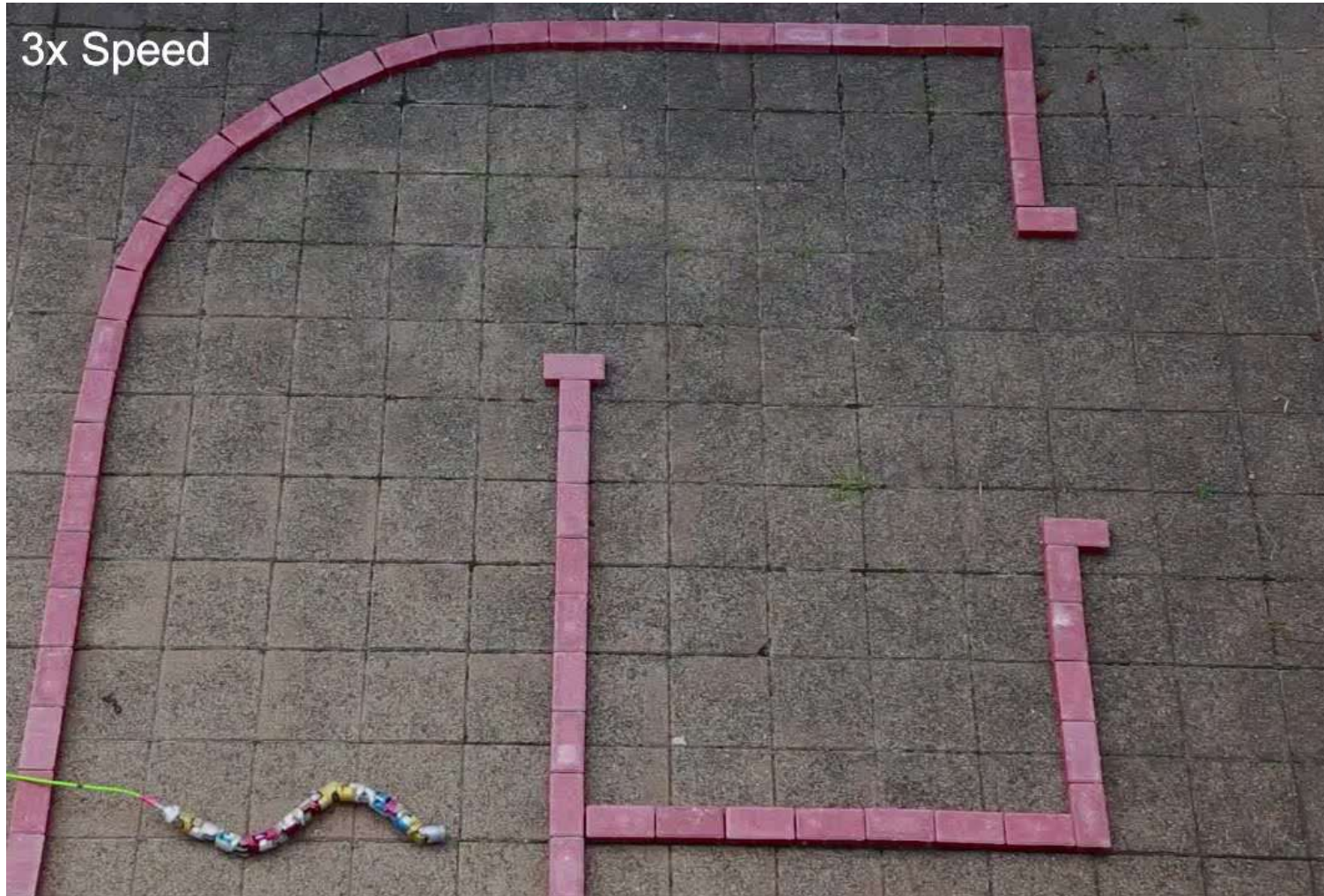
- Rapid turn (“reversal”): modulate **phase** of vertical wave to generate sudden change of direction



*Maneuverability:*  
sequencing modulations  
of sidewinding template



Chaohui Gong,  
Prof. Howie Choset,  
Carnegie Mellon U.

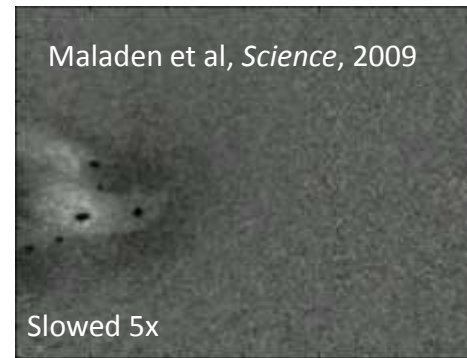
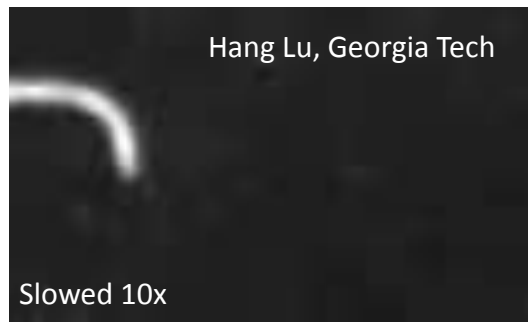


# Questions from the organizers

State-of-the-art methods for locomotion and manipulation can be pushed to deal with systems up to 50 DOF, which is fairly impressive compared to what we could achieve just a few years ago.

- How can we push this dimensionality even further, perhaps all the way to infinity?
  - Geometric mechanics can produce useful predictions for motion for few DOF and  $\infty$  DOF swimmers
- How do we locomote with soft structures?
- How do we manipulate deformable objects?
- How do we plan and control continuum robots?

# Swimming (with no inertia)



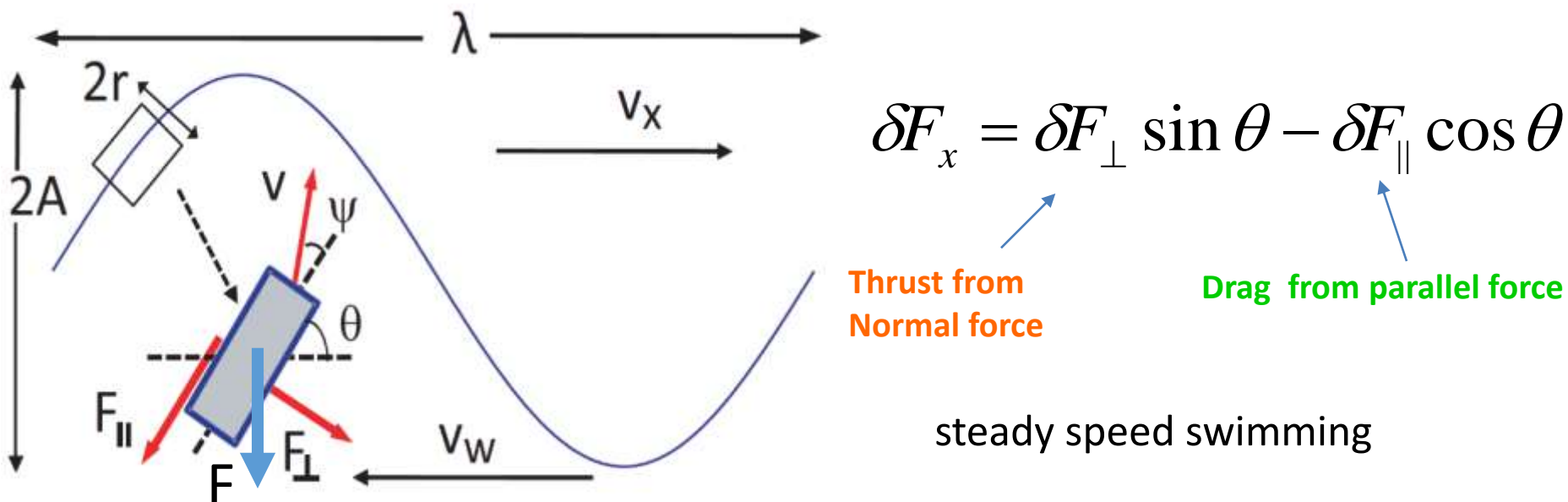
Nematode worm in fluid

Sandfish lizard in dry sand

CAN WE UNDERSTAND SAND-SWIMMING LIKE WE DO FLUID SWIMMING?

# Resistive Force Theory (RFT) for non-inertial swimming

*Biological control assumption: animal controls for pattern of self-deformation*



LINEAR, INDEPENDENT, SUPERPOSITION

$$F_x = \int dF_x = 0$$

**Stokes' law:**

$$\delta F_{\perp} \propto C_{\perp} V_{\perp}$$

**DRAG ANISOTROPY**

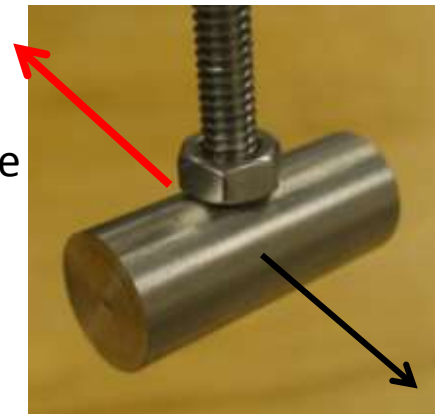
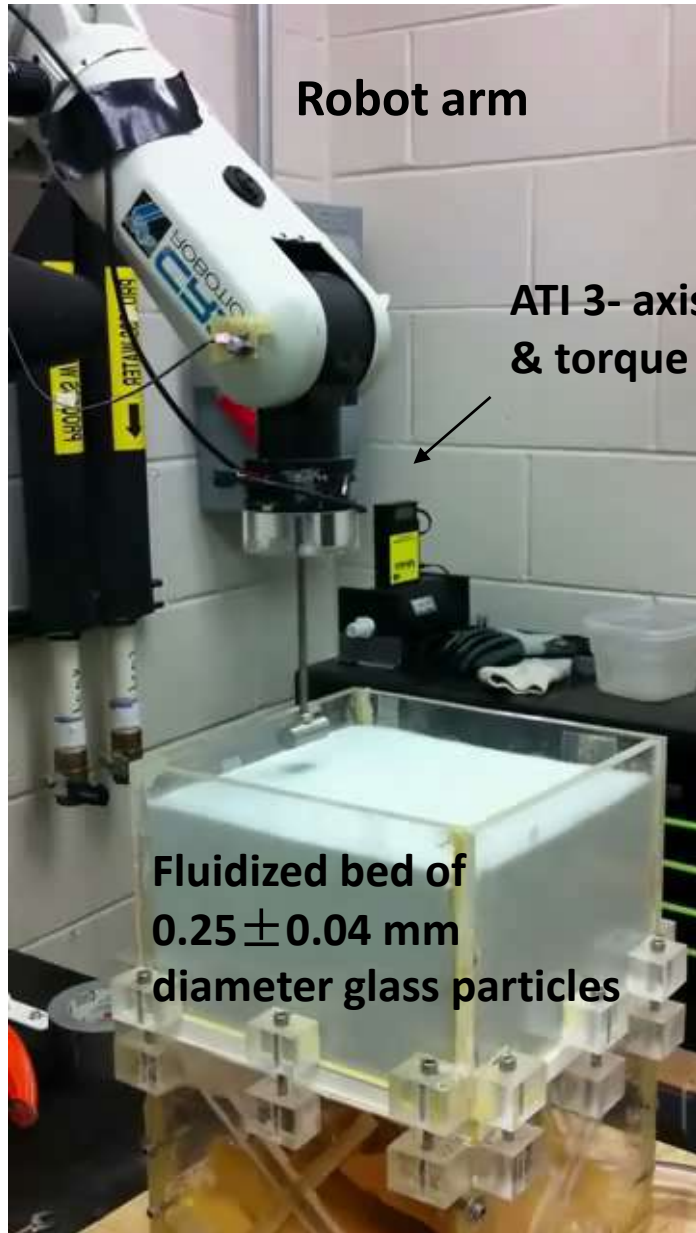
$$\delta F_{\parallel} \propto C_{\parallel} V_{\parallel}$$

$$C_{\perp} / C_{\parallel} > 1$$

- Taylor (1951)
- Gray & Hancock (1955)
- Lauga & Powers (2009)

(long thin cylinder,  $\frac{C_{\perp}}{C_{\parallel}} \rightarrow 2$ )

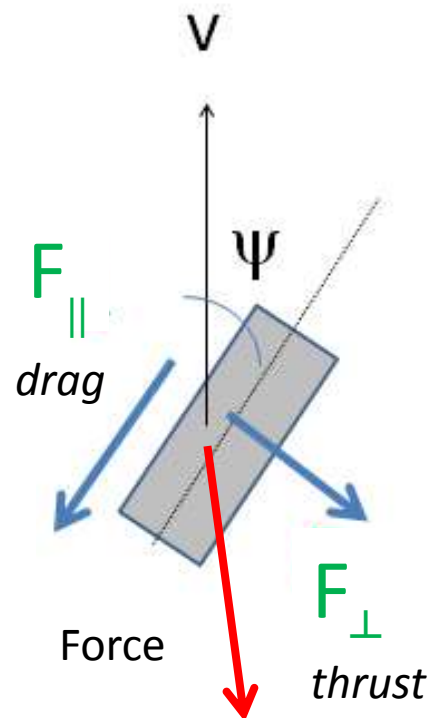
# Resistive forces in GM



1.5 cm diameter, stainless steel rod

(friction  $\sim$  sandfish skin  $\sim 0.2$ )

(overhead view)



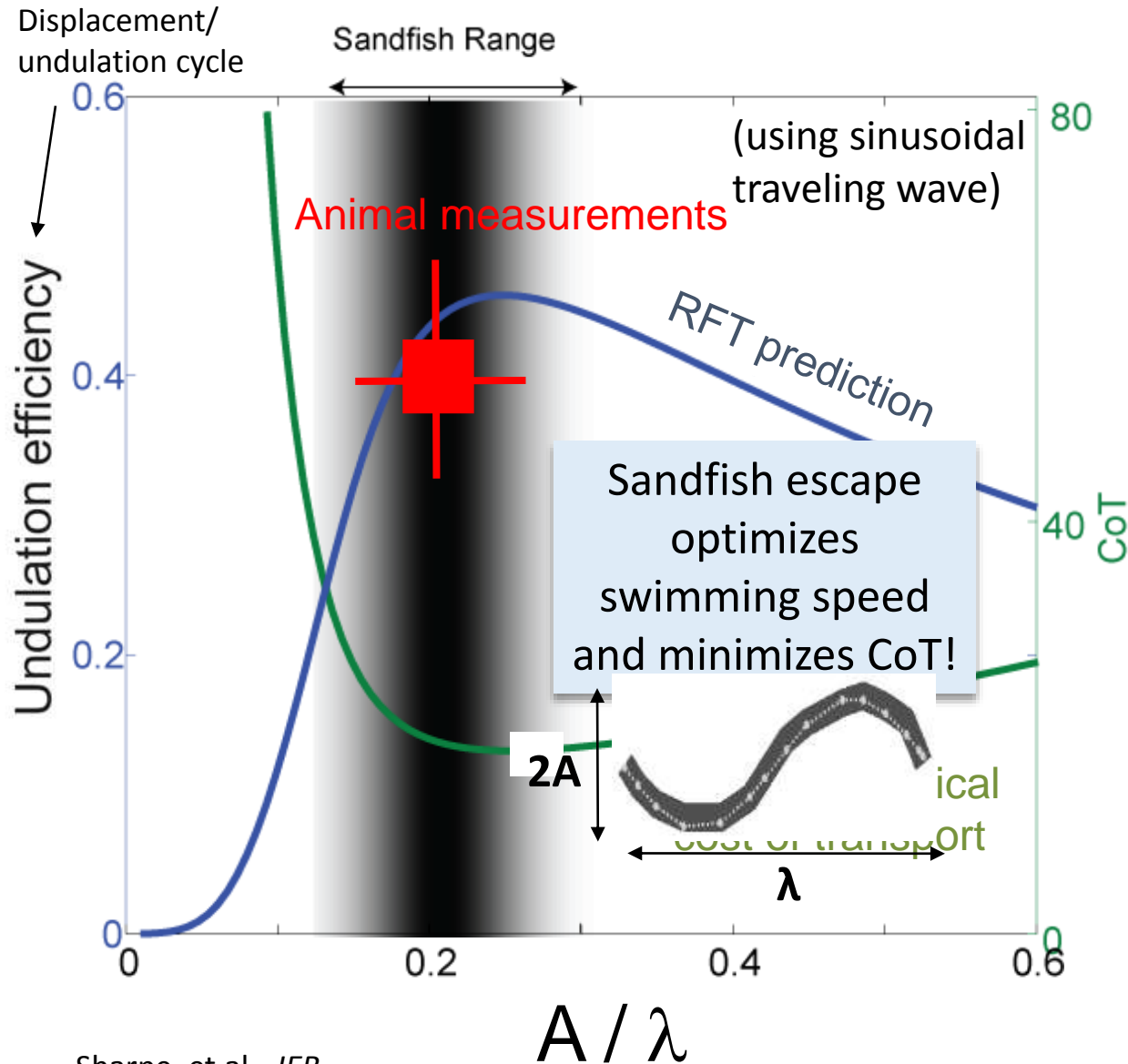
Granular “frictional fluid” analog to Stokes’ drag

(Zhang & Goldman, *Physics Fluids*, 2014)

- $\frac{c_{\perp}}{c_{\parallel}} \sim > 3,$
- no speed dependence

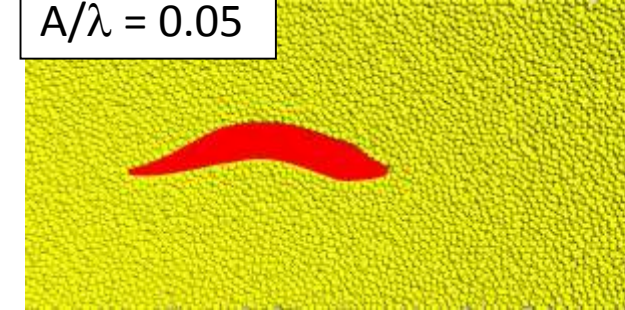
# Optimal sand-swimming in the sandfish

Maladen et al, *Science*, 2009, *Interface*, 2011

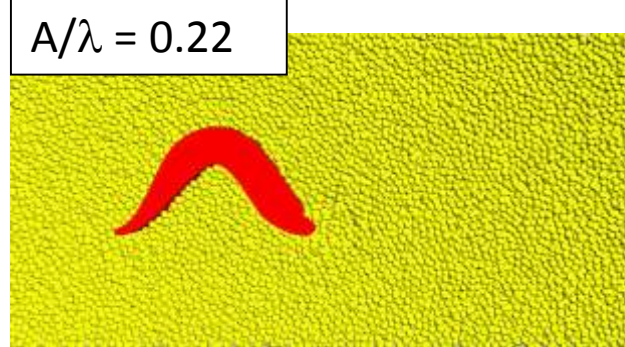


f=2 Hz

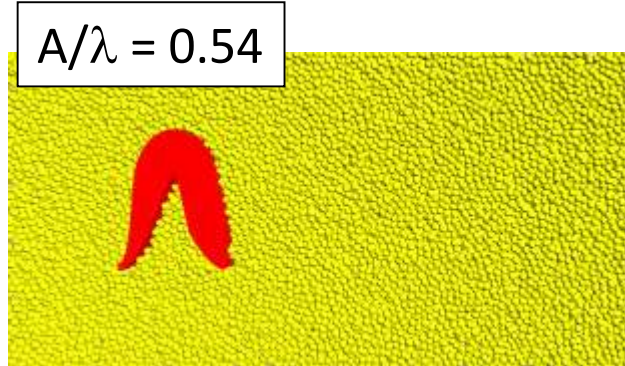
$A/\lambda = 0.05$



$A/\lambda = 0.22$



$A/\lambda = 0.54$



# Geometric mechanics applied to (non-inertial) self-propulsion

VOLUME 58, NUMBER 20

PHYSICAL REVIEW LETTERS

18 MAY 1987

## Self-Propulsion at Low Reynolds Number

Alfred Shapere and Frank Wilczek

*Institute for Theoretical Physics, University of California, Santa Barbara, Santa Barbara, California 93106*

(Received 23 March 1987)

We formulate the problem of self-propulsion at low Reynolds number in terms of a gauge field over the space of shapes. The computation of this field is discussed, and carried out in some examples. We apply our results to determine maximally efficient infinitesimal swimming motions of spheres and circular cylinders.

PACS numbers: 47.10.+g, 87.45.-k Apply to low DOF system

Body  
velocity

$$\xi = A \dot{\alpha}$$

Symmetries at low Re + kinematic motion



IEEE TRANSACTIONS ON ROBOTICS, VOL. 29, NO. 3, JUNE 2013

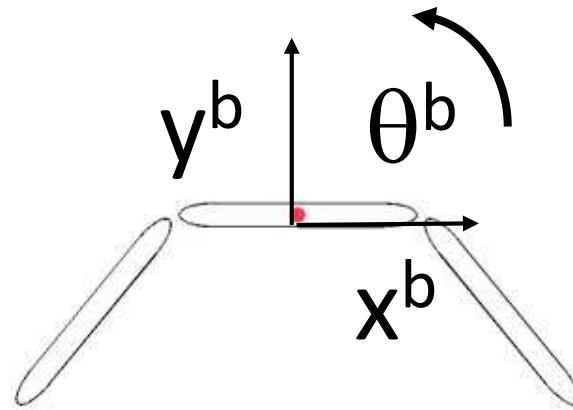
## Geometric Swimming at Low and High Reynolds Numbers

Ross L. Hatton, *Member, IEEE*, and Howie Choset, *Member, IEEE*

Calculate motion for large self-deformations using optimal coordinates

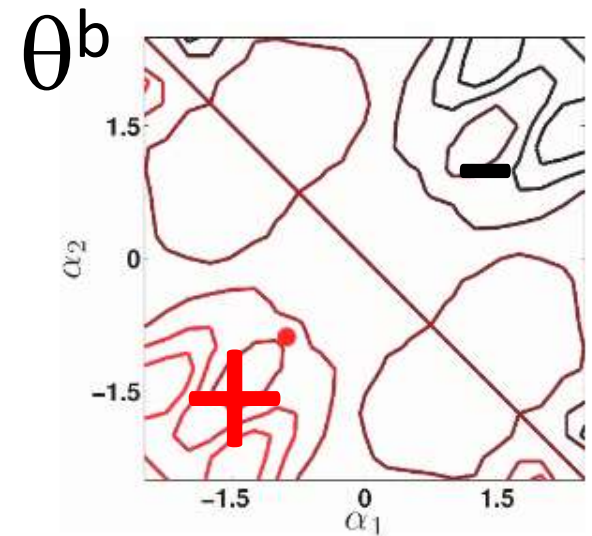
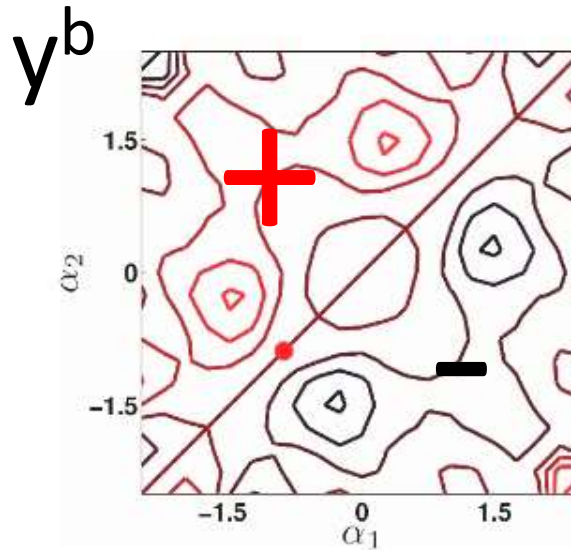
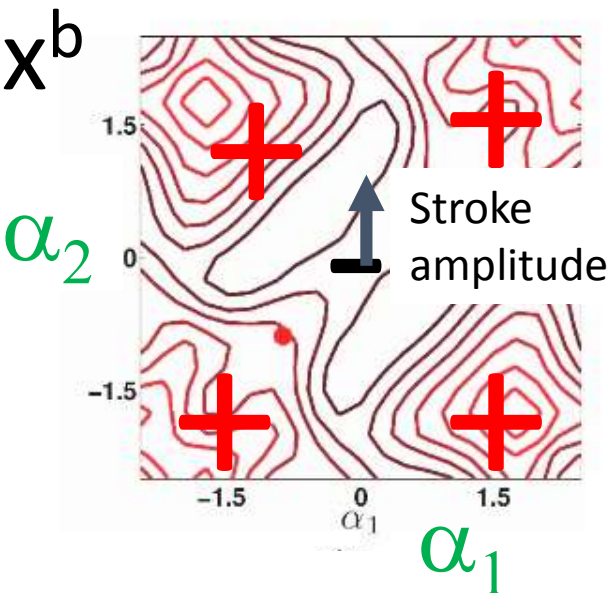


CCFs allow visualization of how shape changes lead to net translation/rotation



Area in CCF space  $\sim$  net displacement or rotation after cycle

CCFs

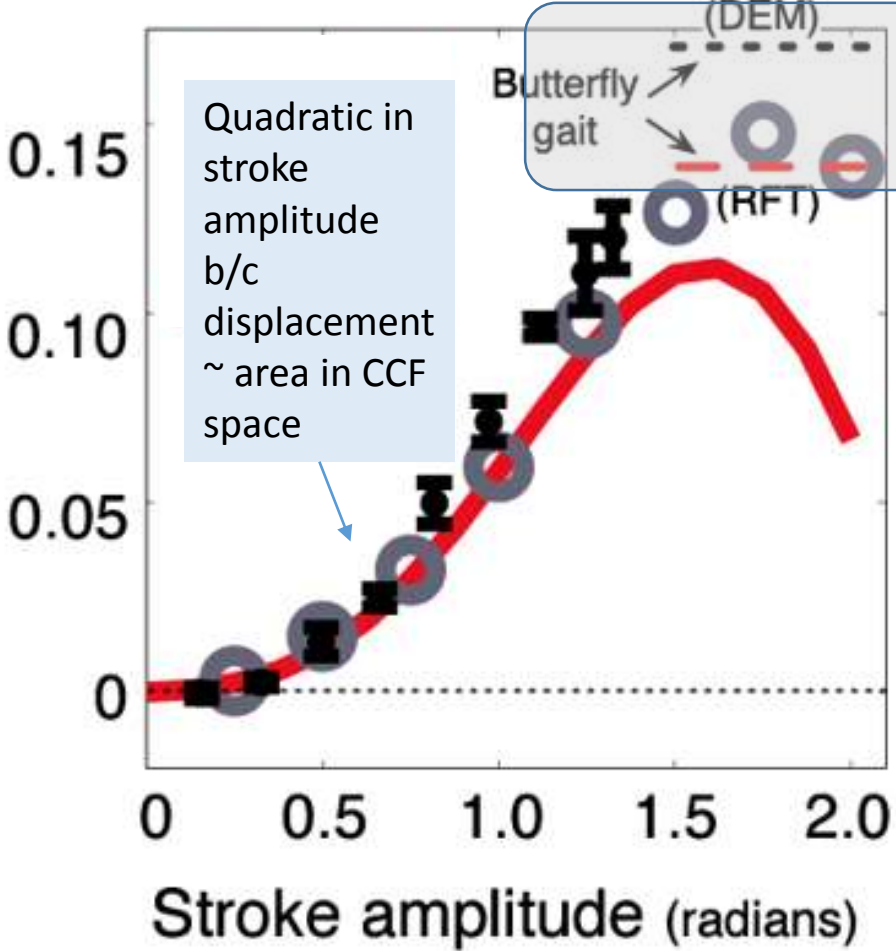


# Geometric mechanics of a granular 3-link swimmer

Hatton, Ding, Choset & Goldman, *PRL*, 2013



Displacement (body-lengths)

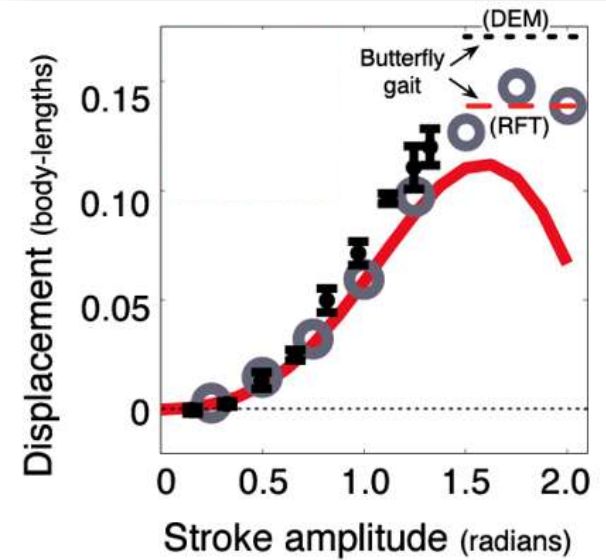
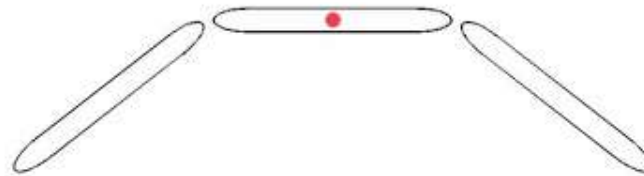


- Assumptions in model:
- kinematic (no inertia) (YES)
  - Linearity in local connectic
  - symmetry in space and time? (YES and  $\sim$ YES)

# Gait optimization

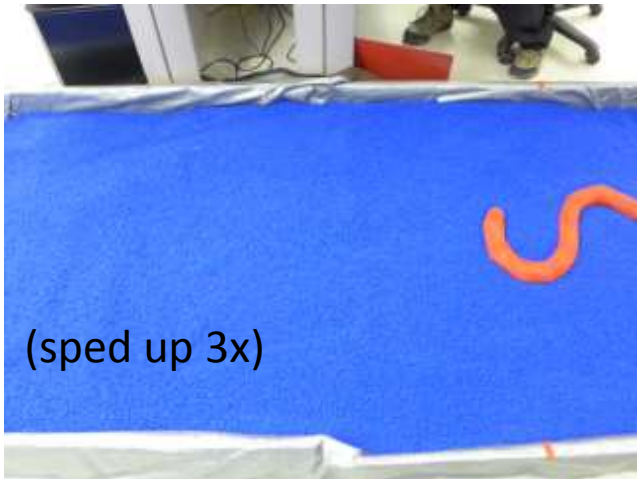
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(Butterfly gait)

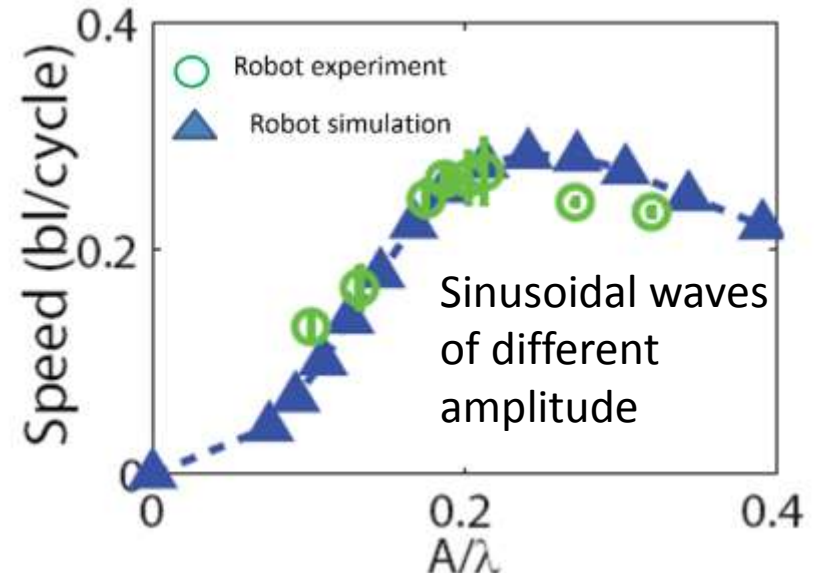
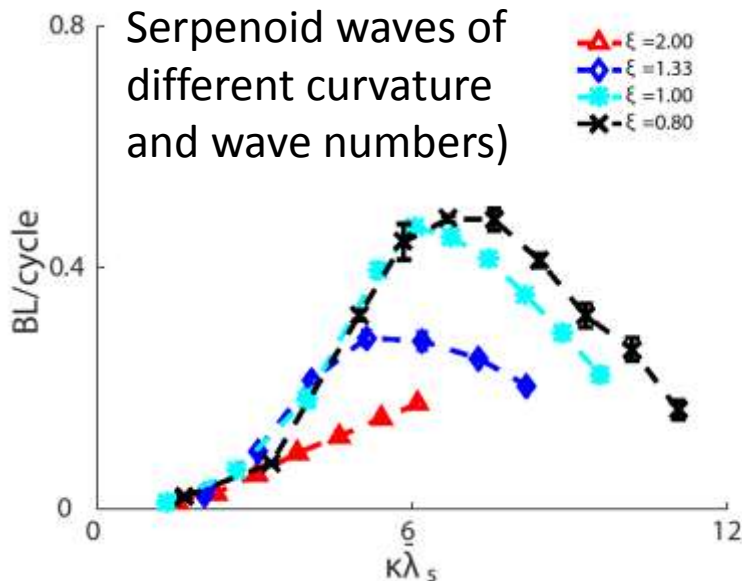


# Can we apply these techniques (geometric mechanics + optimal coordinates) to higher DOF “real world” kinematic systems?

Dai, Gong, Hatton, CMU



Maladen et al, GT



# Reducing a continuum robot to 2D

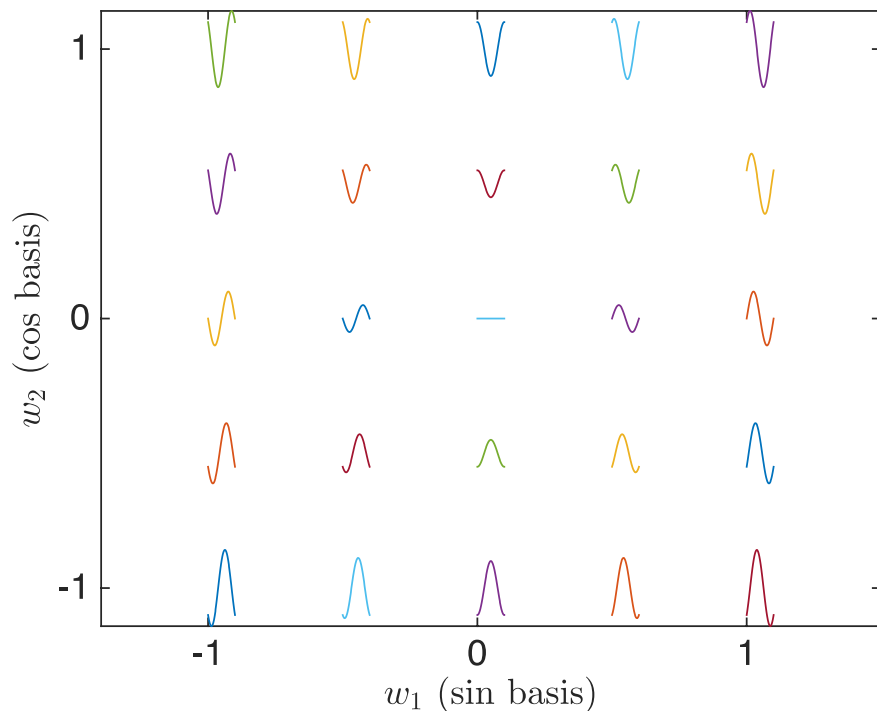


Chaohui Gong,  
Prof. Howie Choset,  
Carnegie Mellon U.

$$\kappa(s) = w_1 \beta_1(s) + w_2 \beta_2(s)$$

$\kappa(s)$  : curvature along the arc length

$\beta(s)$  : curvature basis function

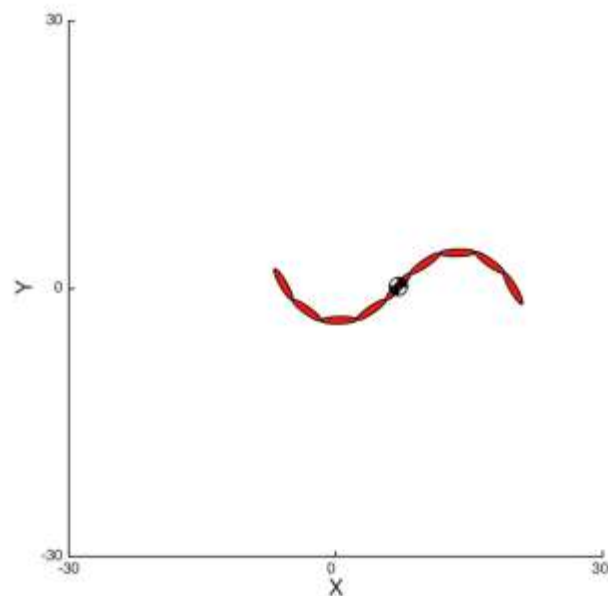
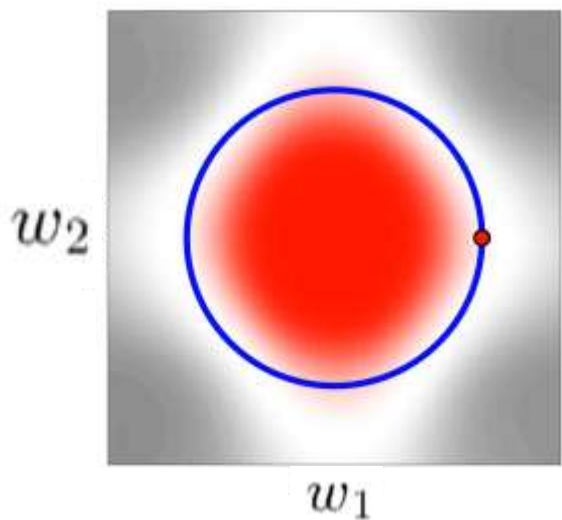


A gait is defined together by the shape bases and the trajectory in the reduced shape space which is defined by the shape bases:

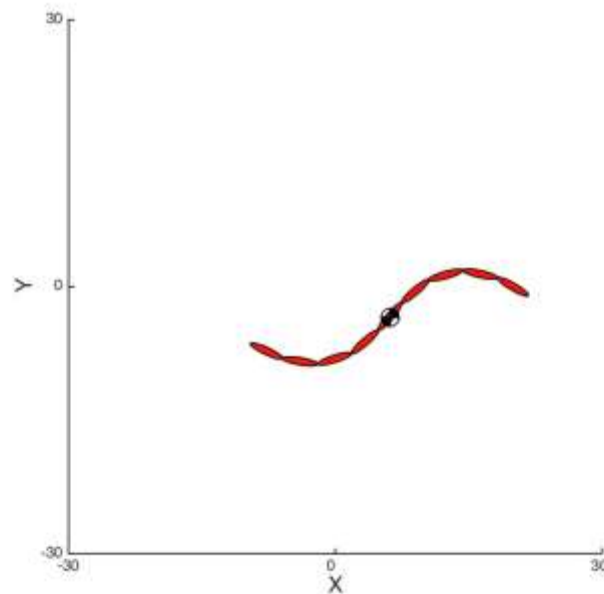
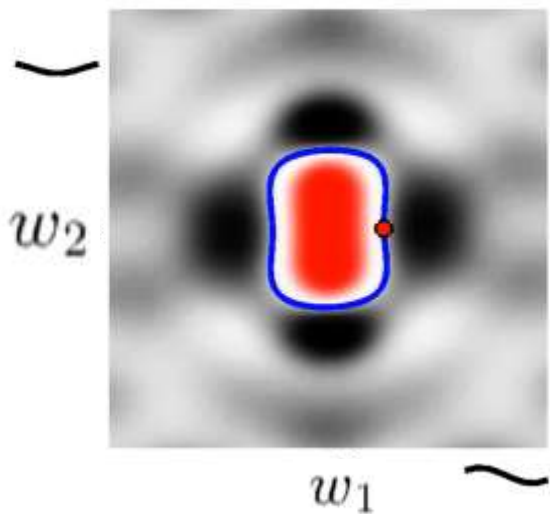
- Approximate arbitrary curve as sum of bases, and compute CCFs
- Optimize shape bases, recompute CCFs

(9 links used so can implement on robot)

### $x^b$ CCF in sin & cos bases (serpenoid)



### $x^b$ CCF in optimal bases

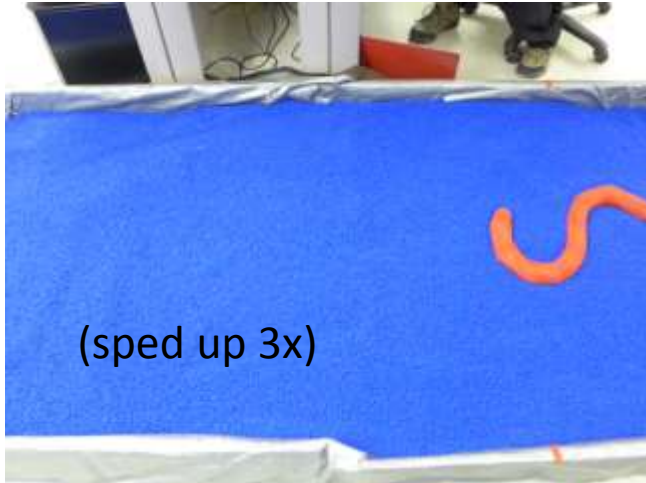


# 2 bases CCFs predict optimal movement!

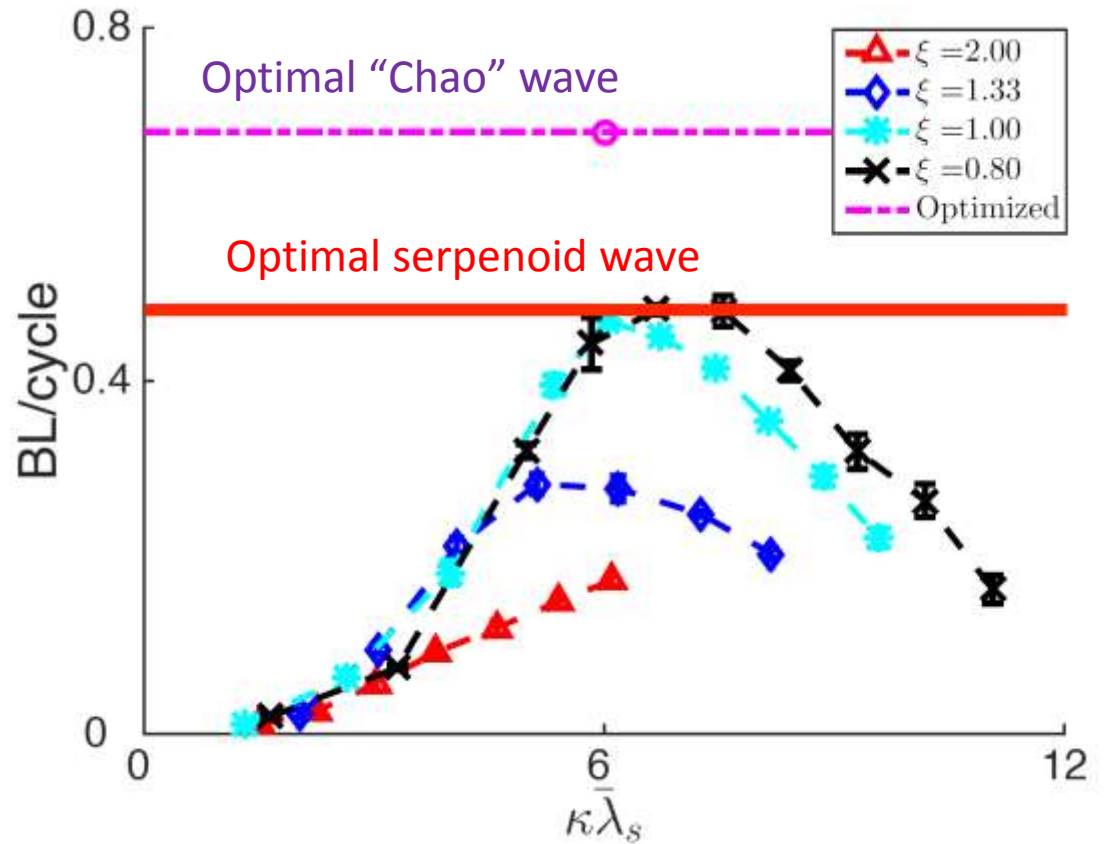


Chaohui Gong,  
Prof. Howie Choset,  
Carnegie Mellon U.

## Serpenoid waves



“Chao” waves



# Questions from the organizers

State-of-the-art methods for locomotion and manipulation can be pushed to deal with systems up to 50 DOF, which is fairly impressive compared to what we could achieve just a few years ago.

- How can we push this dimensionality even further, perhaps all the way to infinity?
- How do we locomote with soft structures?
- How do we manipulate deformable objects?
  - Fire ant nest construction requires sophisticated manipulation and mobility of and in deformable granular materials
- How do we plan and control continuum robots?



# Arthropod manipulation of dry and wet granular media

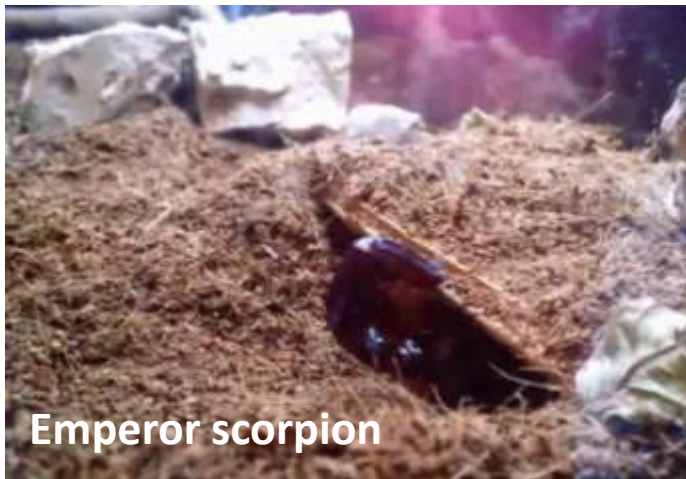
“Rakers”



“Pushers”



“Pullers”

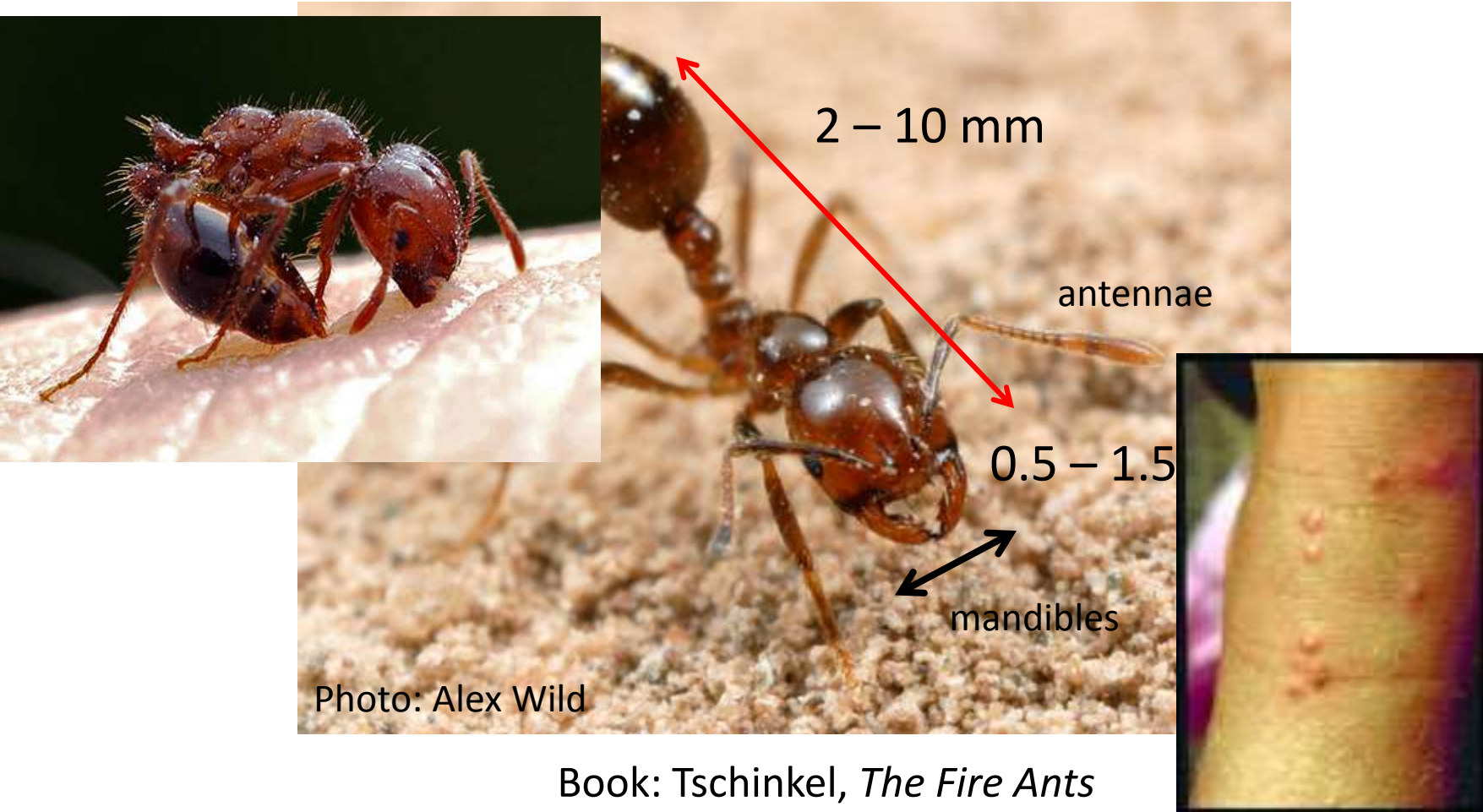


“Carriers”



\*Videos are courtesy of YouTube users. \*\*Behavior lit.: Evans (1966), Muma (1967), Price (2009), Williams (1966), Formanowicz (1991), Springthorpe & Full (2013)

# Red imported fire ant (*Solenopsis invicta* Buren)



Book: Tschinkel, *The Fire Ants*

- Monogyne colonies (single queen) contain  $10^2$  to  $10^6$  workers
- Worker lifespan  $\sim$ months, colony lifespan can be greater than 10 years
- Dig to create subterranean nests which house the colony  $\rightarrow$  "extended phenotype"

**Social (collective)  
substrate manipulation**

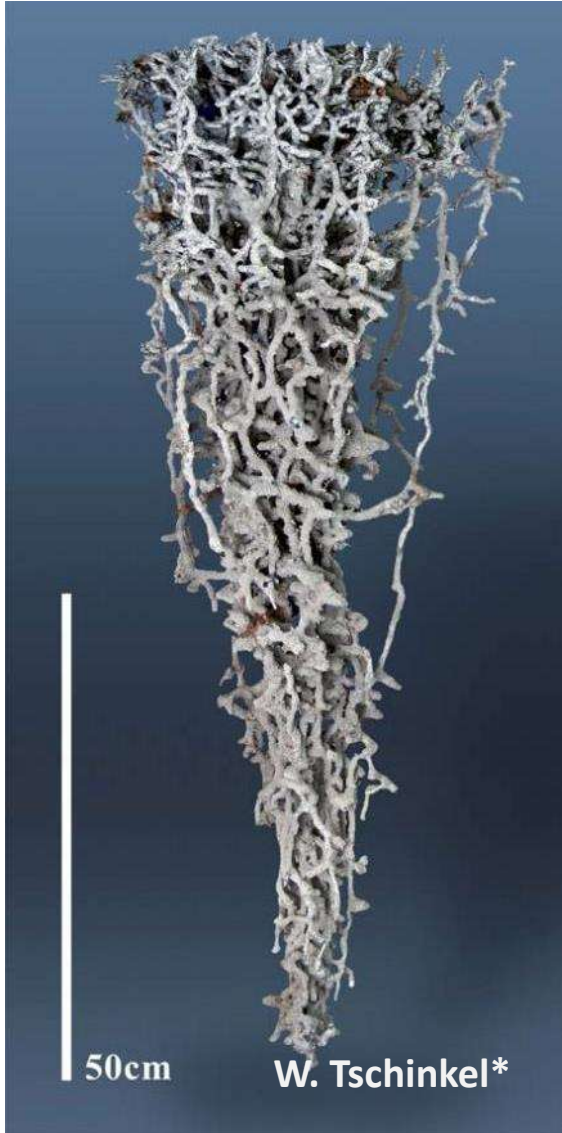
In Georgia, USA

Nest mound



# Nests of social insects (fire ants)

Nest cast\*



$10^3 - 10^6$  ants



2-6 mm

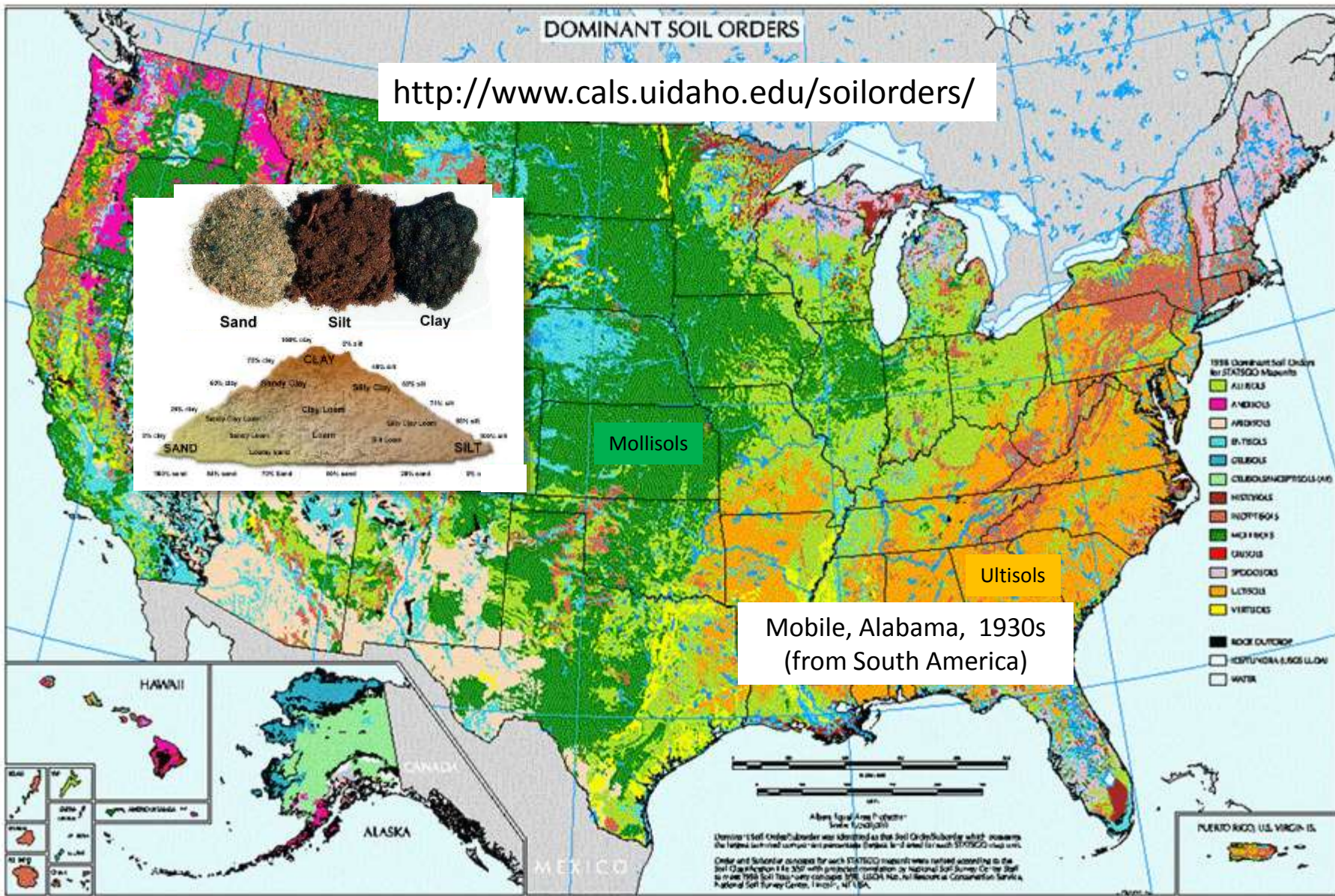
## Social functions:

- Brood care;
- Communication;
- Mating;
- Food sharing and food provision.

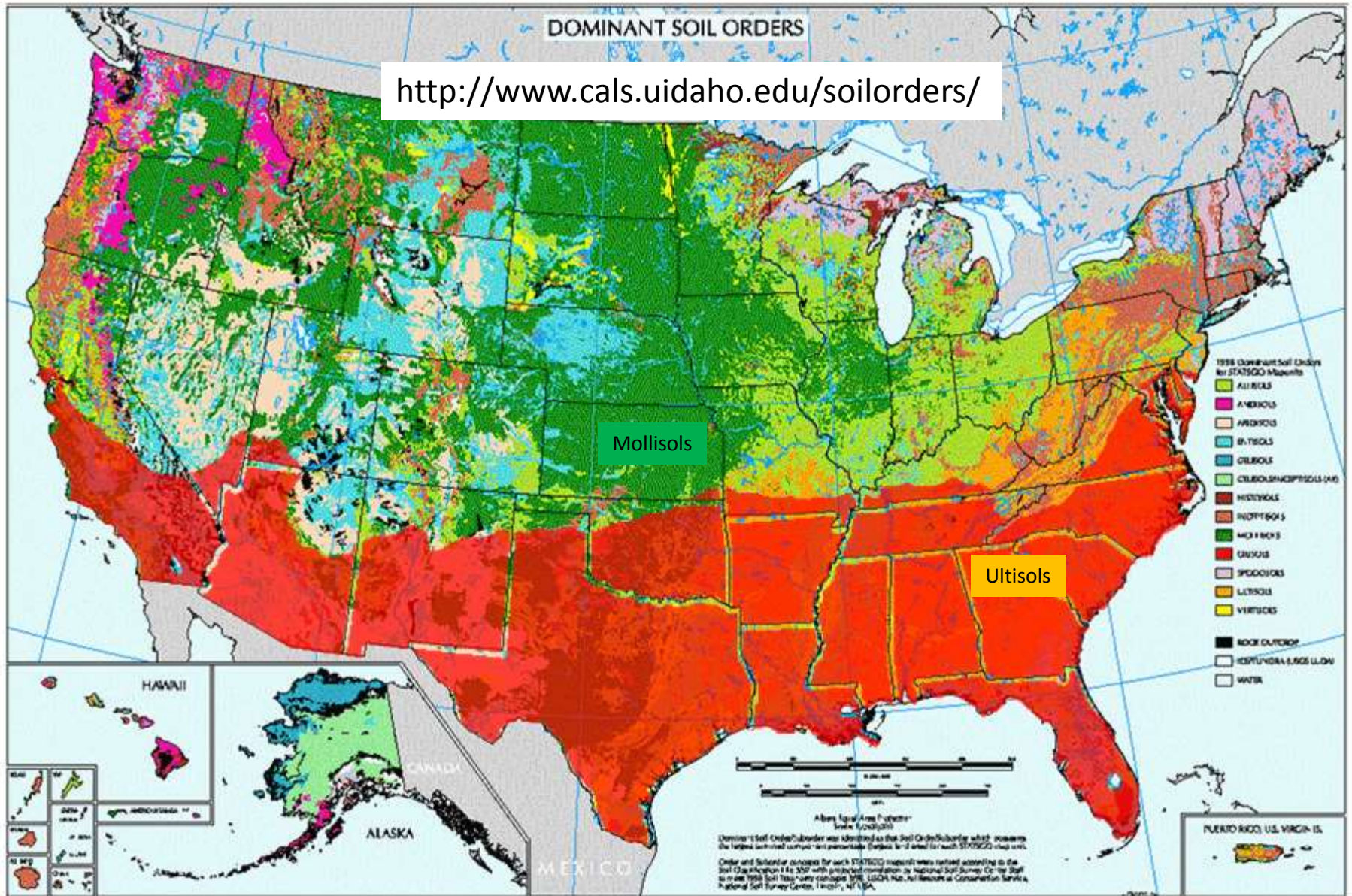
Robot manipulators



# Manipulate any granular media



# Manipulate any granular media



We are interested in how soil properties affect **manipulation & locomotion** strategies and nest structures during collective excavation

- Substrate can deform and fall apart!
- Space constraints (confined & crowded)
- Irregular surfaces
- Perturbations (jostling)
- Lack of vision (dark)



# Simplified laboratory *cohesive* soils: mixtures of sand and water

Dry

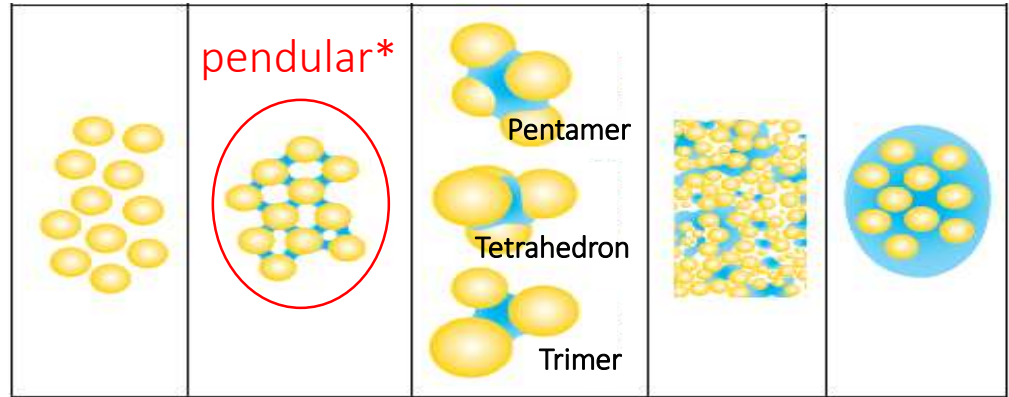


Slightly wet



Microscopically well characterized regime: slightly wet granular media

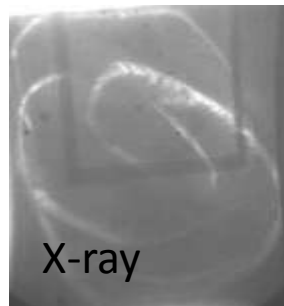
\*Particles are held together by liquid bridges at their contact points



Increasing wetness

Kudrolli, et al. (2008)  
(adapted from Mitari & Nori, 2006)

Challenge: create repeatable homogeneous states in sandy soils



X-ray



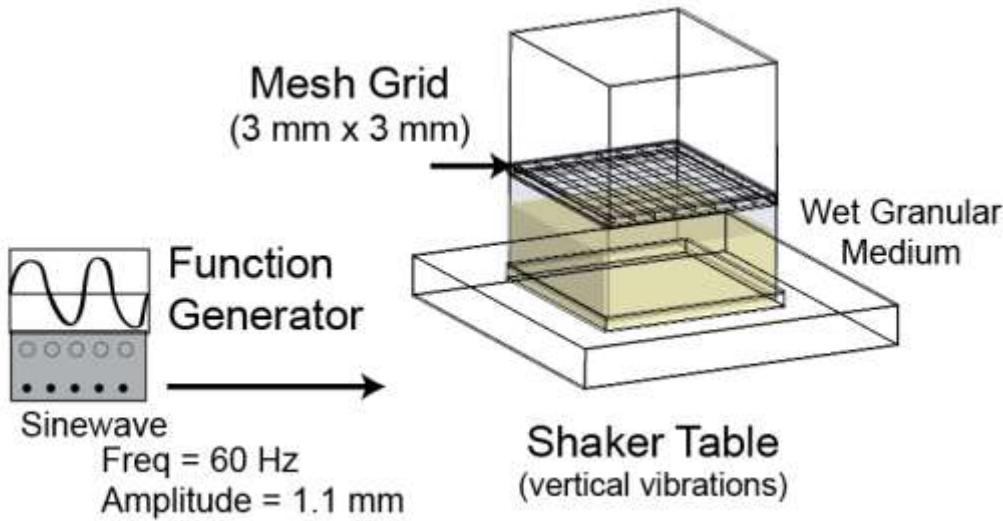
x5



# New method\* to create repeatable & variable homogeneous wet **sandy** substrates

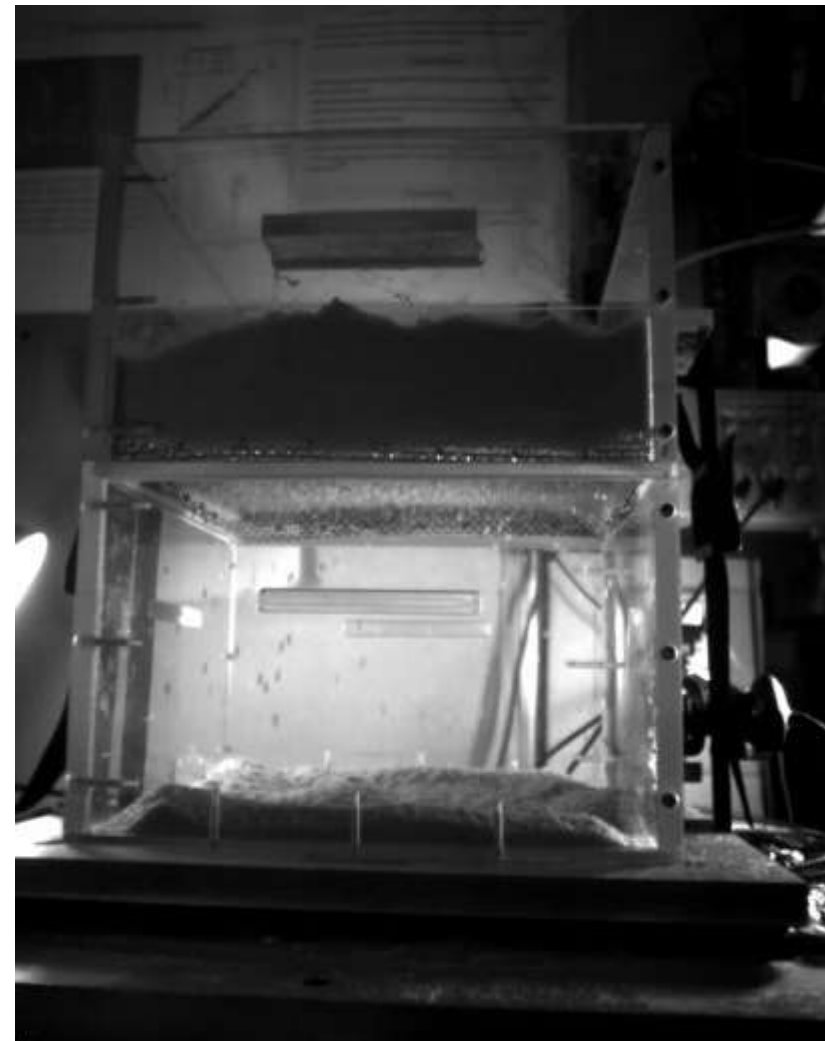
- Sharpe, Kuckuk, Goldman, *Phys. Bio.*, in review 2015
- Monaenkova et al, *J. Exp. Biol.* 2015

0.27 ± 0.04 mm diameter glass particles

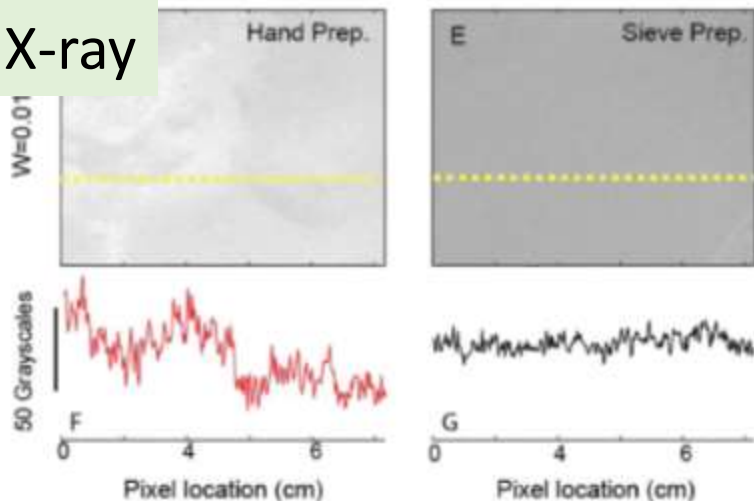


“Make it Rain”

Real Time



X-ray



\*thanks to Nick Gravish

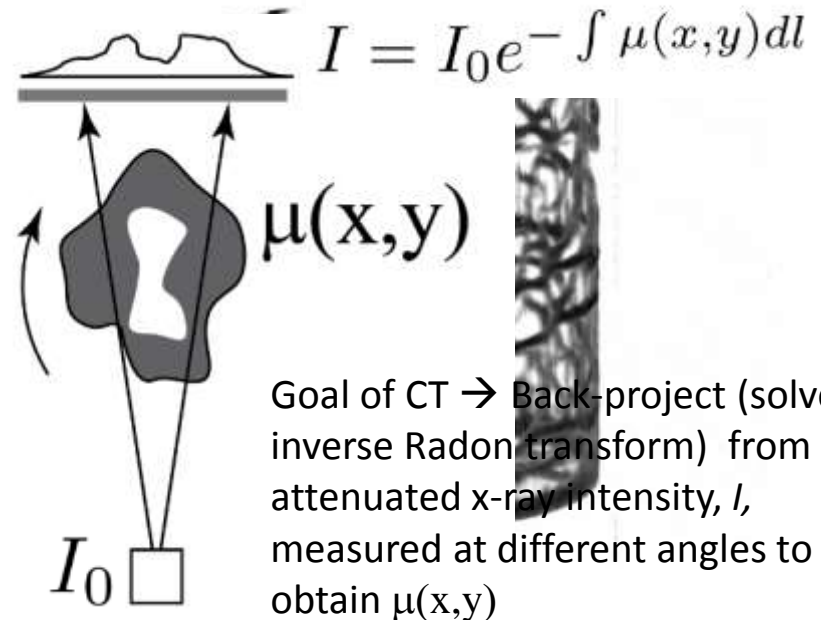
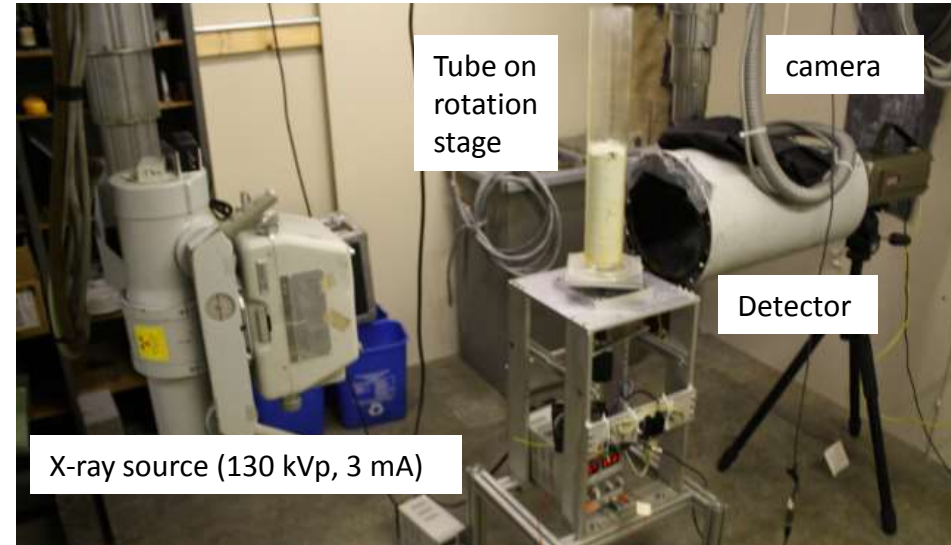
# First study of nest architecture in 3D

Monaenkova et al, *J. Exp. Biol.* 2015

Wetted 0.25 mm glass particles  
in cylindrical glass tube

10 cm

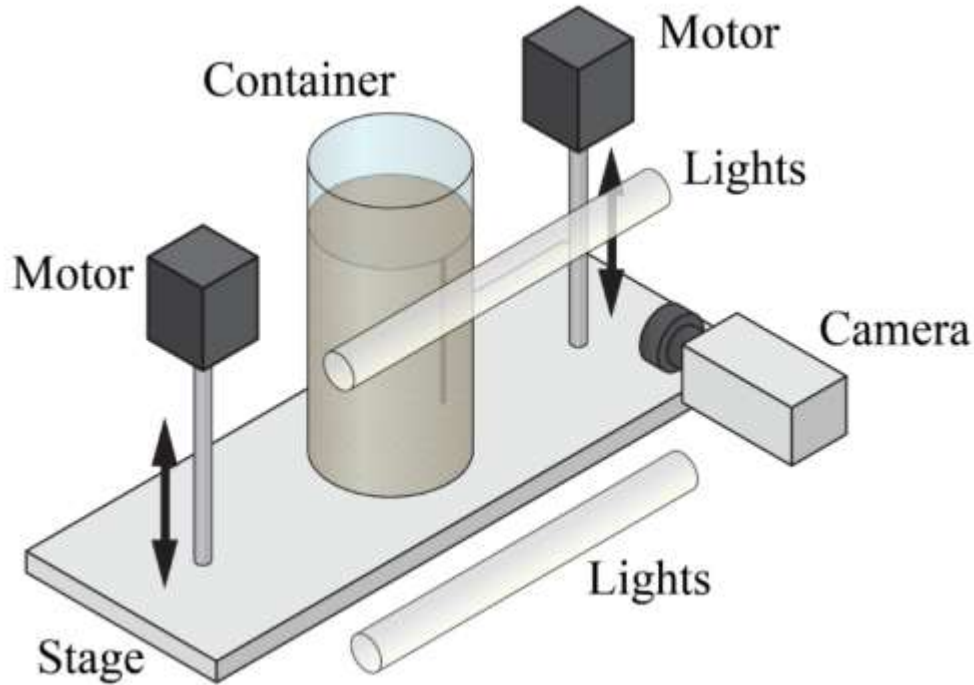
They still dig...



# Visualizing manipulation & excavation behaviors

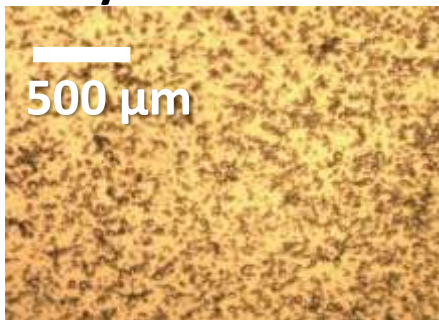


Dr. Daria Monaenkova

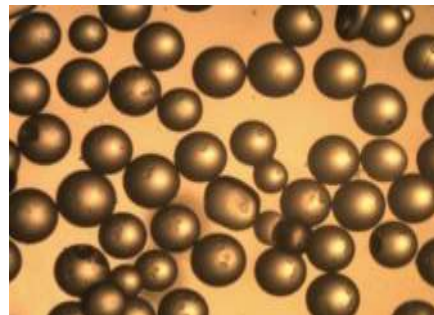


Effective area:  $\pi ab$

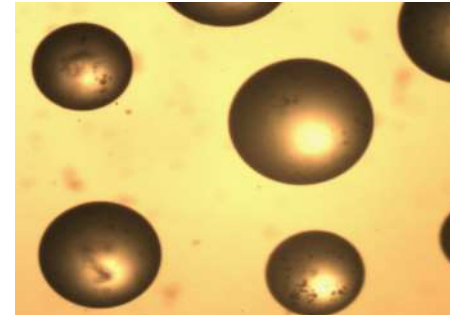
“Clay”: 0-50  $\mu\text{m}$



210-270  $\mu\text{m}$



“Sand”: 0.6-0.8 mm



# Manipulation techniques

“Pulling” mode



1 cm

“Formation” mode



Coordinated use of jaws, limbs and antennae!

Unrealistic substrate, but the coordination is quite visible!



Slowed 3x

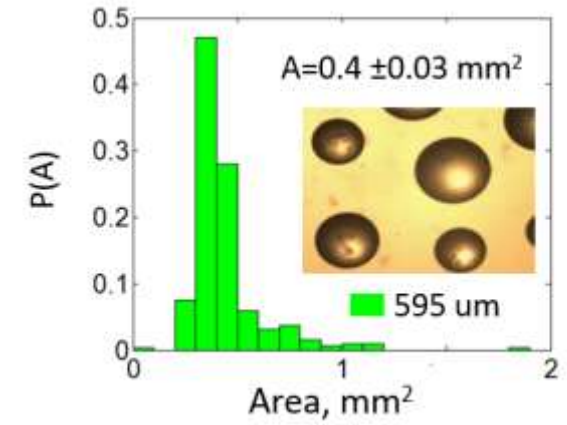
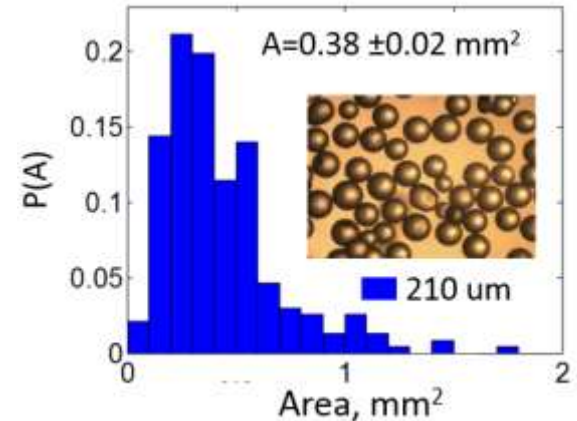
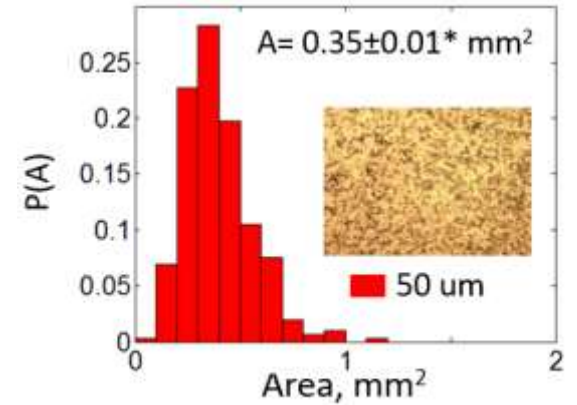
# Effect of grain size on pellet area

Monaenkova et al, *J. Exp. Biol.* 2015



**~NONE!**

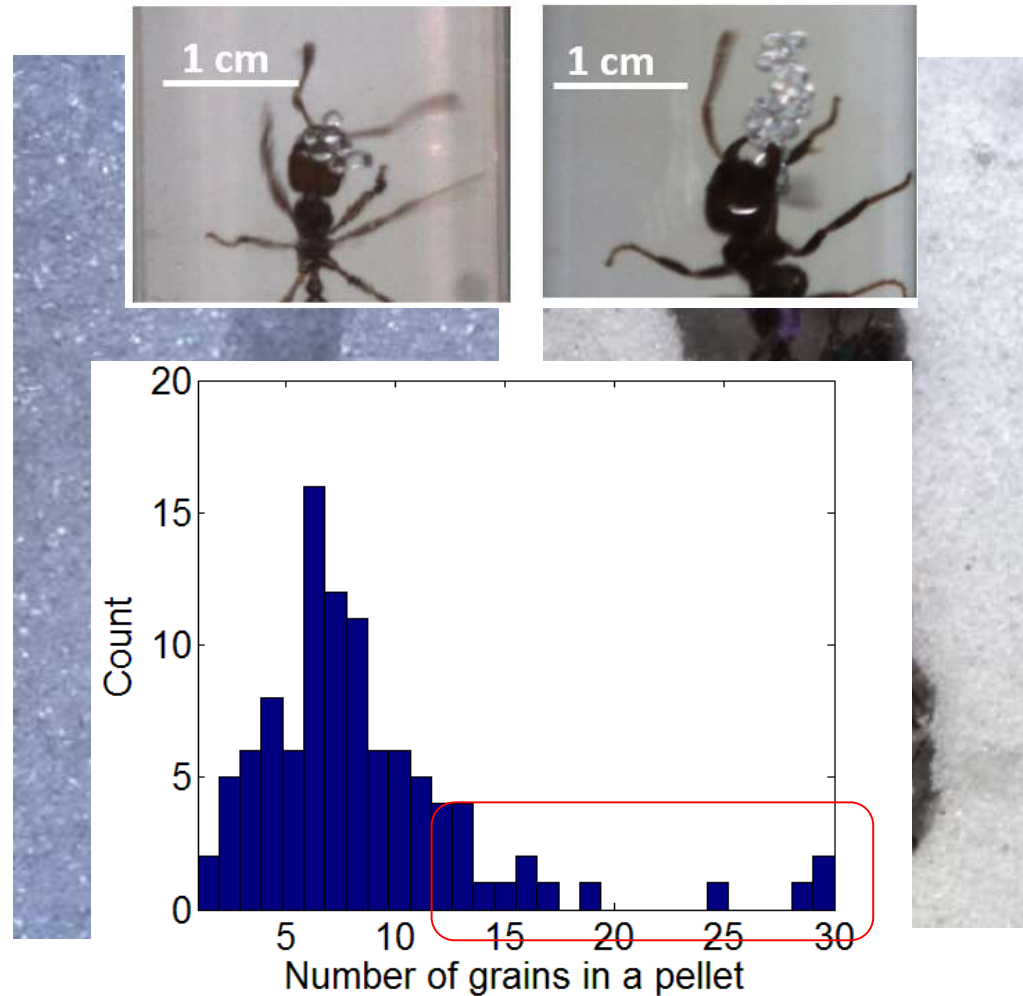
Mean projected area of the pellet independent of particle size, moisture content



# Factors which are important for manipulation of soil to form intermediate pellet

## Fire ants are capable of carrying large pellets

- Pellet stability during transport (“passive sieving”)
- Biomechanical constraints (carrying bulky loads long distances is challenging)
- Collective constraints (neighbors)





Vadim Linevich

# Multiple autonomous granular diggers: task oriented social locomotion and manipulation



Dr. Daria  
Monaenkova

(2 robots, 17 hours of digging shown)



- Excavate cohesive GM
- Fully autonomous (locomote, dig, recharge, locate “soil”)
- CoTS components
- Test hypotheses of social laziness





# Questions from the organizers

State-of-the-art methods for locomotion and manipulation can be pushed to deal with systems up to 50 DOF, which is fairly impressive compared to what we could achieve just a few years ago.

- How can we push this dimensionality even further, perhaps all the way to infinity?
  - Geometric mechanics can produce useful predictions for motion for few DOF and  $\infty$  DOF swimmers
- How do we locomote with soft structures?
- How do we manipulate deformable objects?
  - Fire ant nest construction requires sophisticated manipulation and mobility of and in deformable granular materials
- How do we plan and control continuum robots?
  - Templates (low DOF control targets) to manipulate the body and environment to effect locomotion

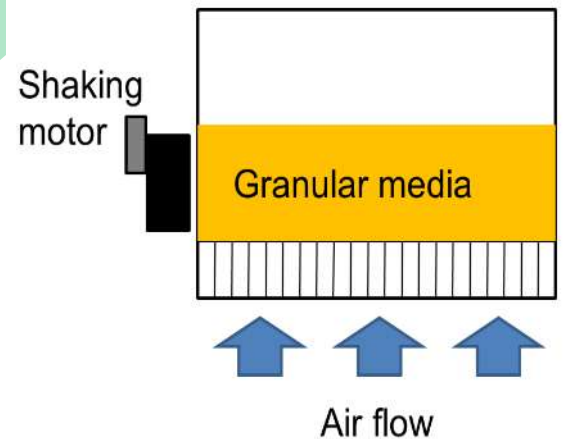
# Discover principles of terrestrial locomotion

goldmanlab.gatech.edu

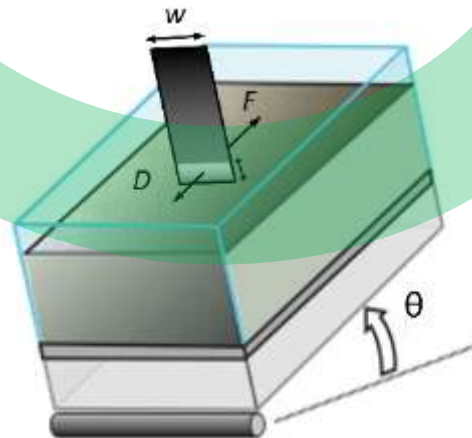
Bio/neuromechanics



Substrate control



Soft matter interaction physics



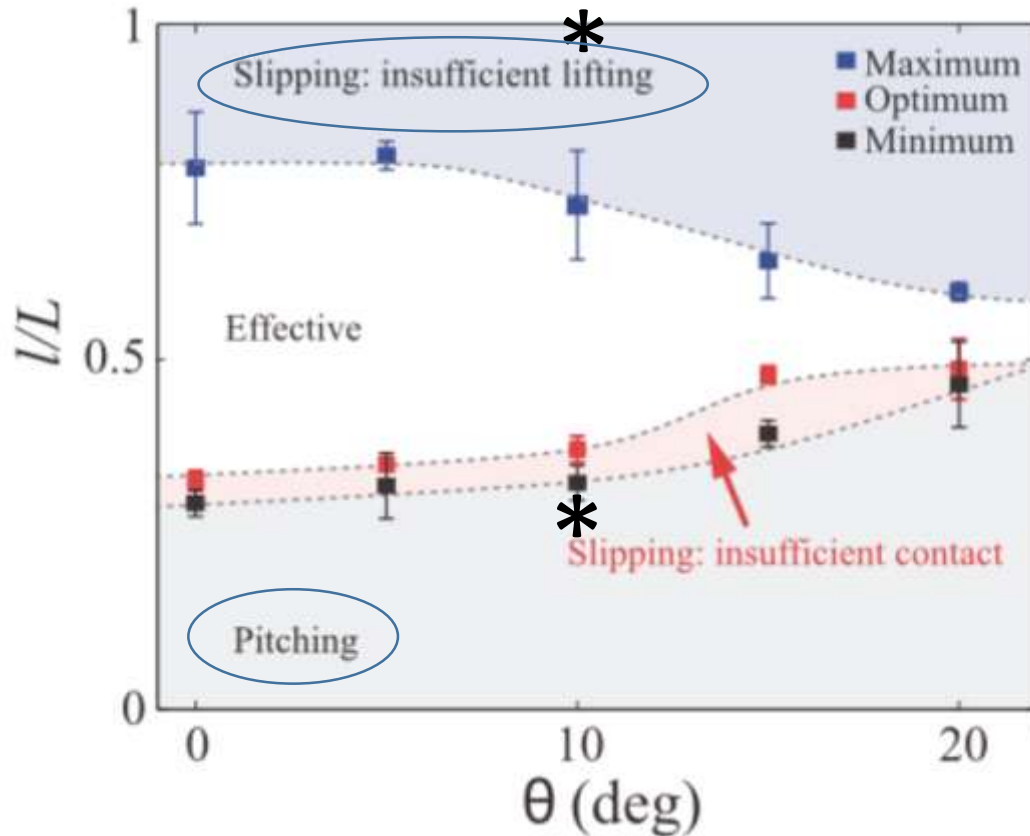
Physical models  
"robophysics"

Aguilar et al, *Rep. Prog. Physics*, in prep.



# Robophysics “phase diagram” for robot sidewinding

Marvi, Gong, Gravish, Astley, Travers, Hatton, Mendelson, Choset, Hu, Goldman, *Science*, 2014



Slipping failure ( $I/L=1$ )



Pitching failure ( $I/L=0.27$ )



*Robot failure is often more interesting (and useful) than robot success!*

**END**