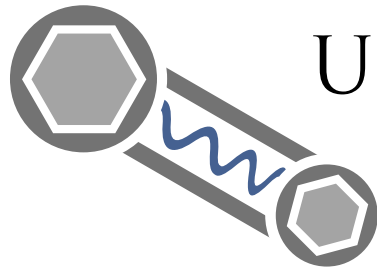


# Trade-offs in Limbed Mobility

---

NSF Workshop on Locomotion and Manipulation  
April 2, 2015

Katie Byl



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---

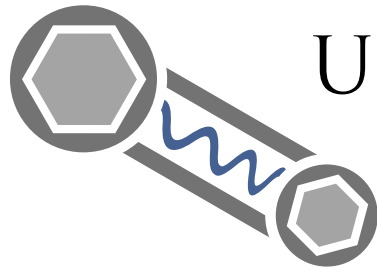
Robotics Lab

# Trade-offs in Limbed Mobility

---

NSF Workshop on Locomotion and Manipulation  
April 2, 2015

Katie Byl <sup>^</sup> Bill



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---

Robotics Lab

# Why Locomotion is Hard...

# Why Locomotion is Hard...

## Stochastic Environments

# Why Locomotion is Hard...

Stochastic Environments  
**variability**



[variability doesn't necessarily  
mean uncertainty...]

# Locomotion Goals

Robustness

Agility

Energetics



Robustness  
unknown variability

Agility

Energetics

Robustness  
unknown variability



**Agility**  
**known variability**

Energetics



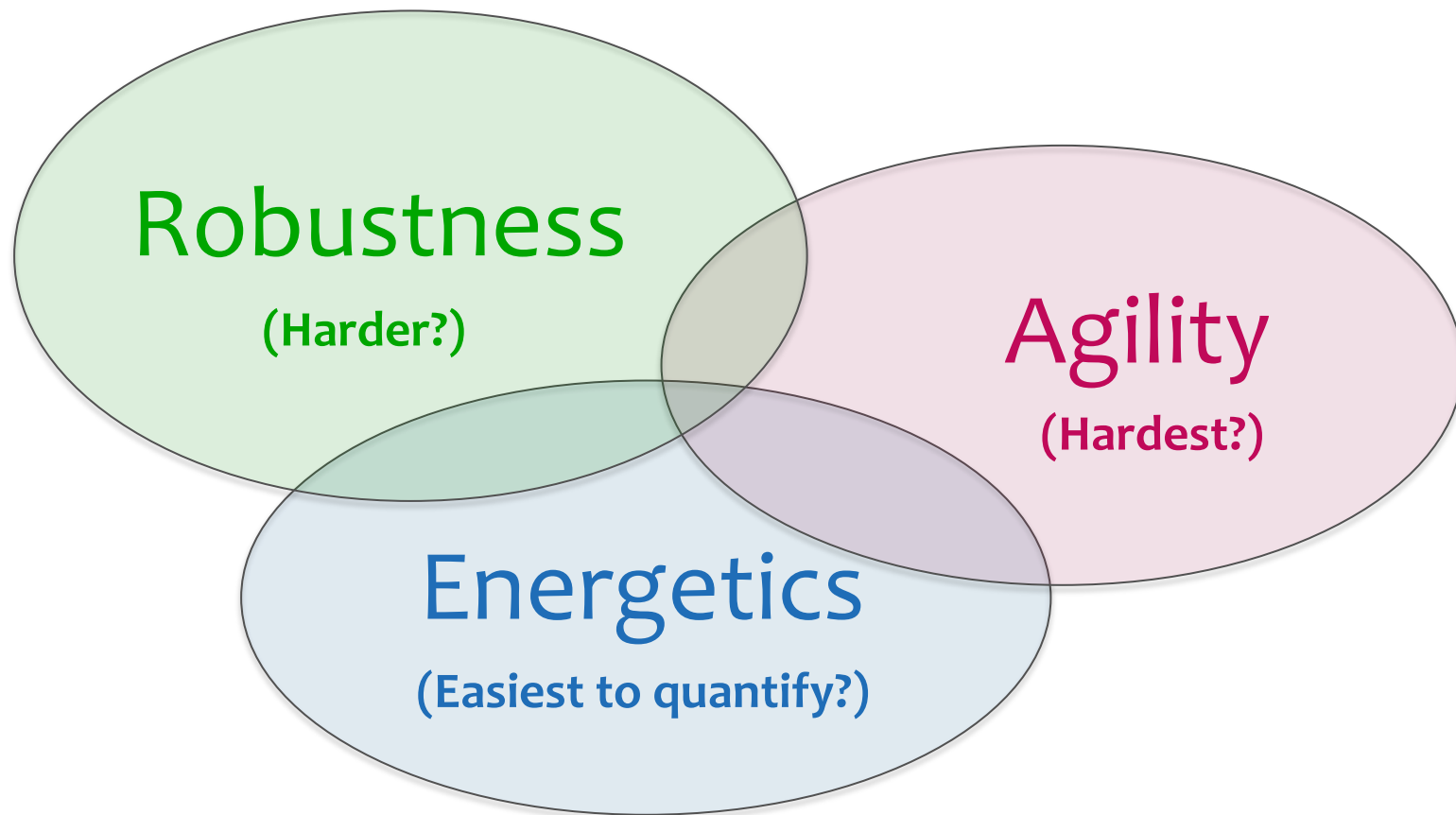
Robustness  
unknown variability

Agility  
known variability

Energetics  
as efficient as practical



# Locomotion metrics?



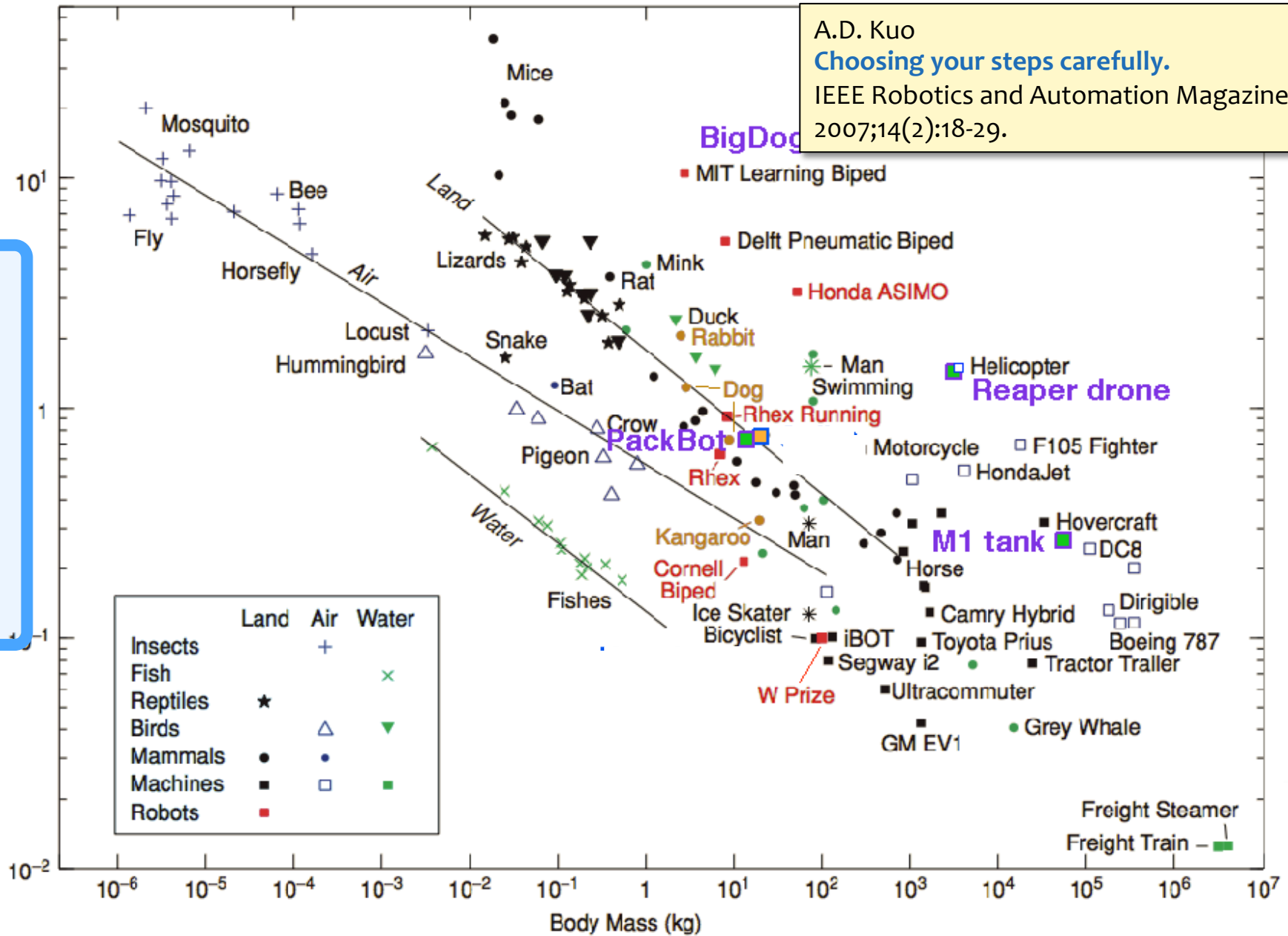
# Energetics: Cost of Transport

A.D. Kuo

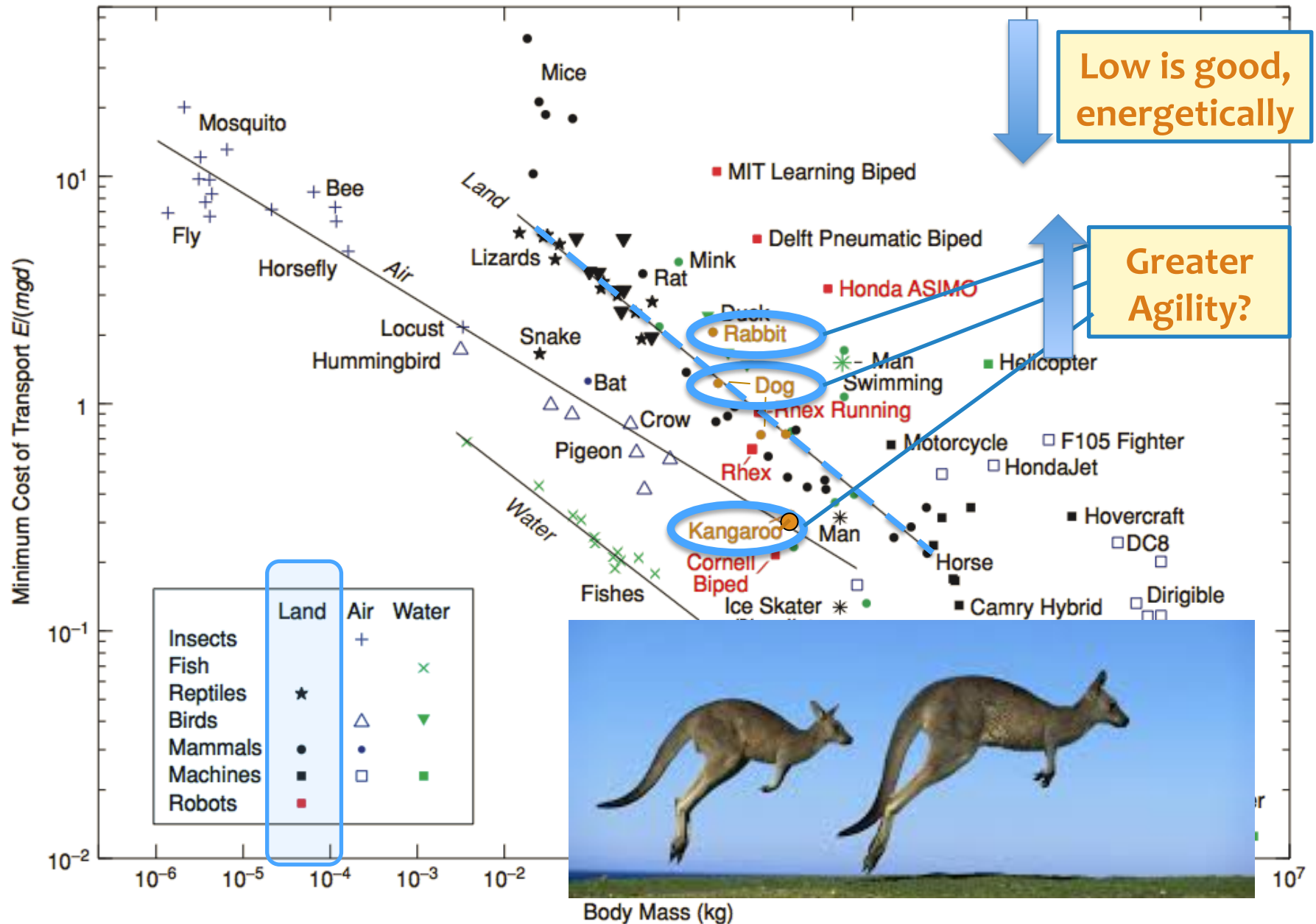
Choosing your steps carefully.

IEEE Robotics and Automation Magazine.  
2007;14(2):18-29.

Minimum Cost of Transport  $E_i/(mgd)$



# Agility vs Energetics Trade-off?



	Land	Air	Water
Insects		+	
Fish			x
Reptiles	*		
Birds		Δ	▼
Mammals	•	•	
Machines		□	■
Robots	■		



Body Mass (kg)

# Rabbit Agility



Danish Rabbit Hopping Championship, 2010  
<https://www.youtube.com/watch?v=ptyKSiRyQ4Y>

(Wait: Did she throw the bunny?)

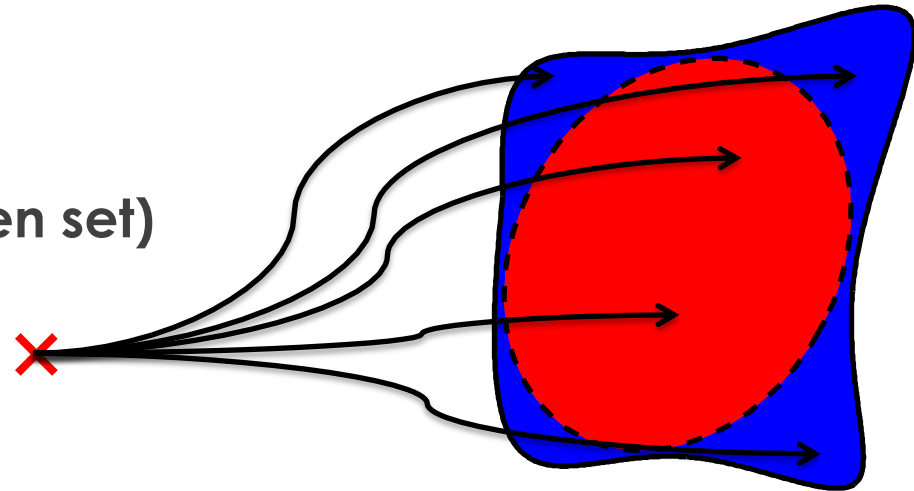


Danish Rabbit Hopping Championship, 2010  
<https://www.youtube.com/watch?v=ptyKSiRyQ4Y>

# Agility and Robustness, Intuitively

- One to many  
(can reach points in some open set)

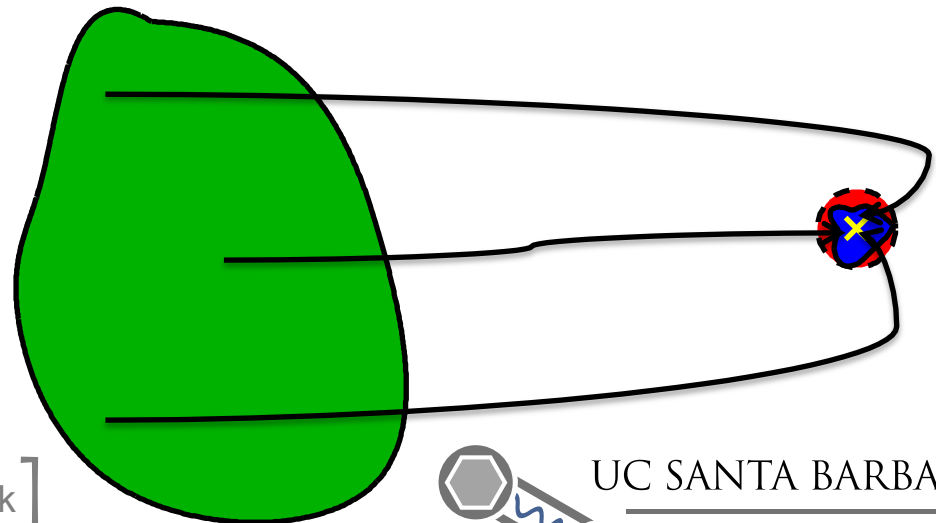
Agility (?)



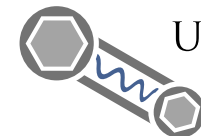
(arriving at/within some  $\Delta t$ )

- Many to one  
(recover, to some tolerance)

Robustness (?)



[e.g., “funnels”... Burridge, Rizzi, and Koditschek]



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Robotics Lab

# Quantifying Agility

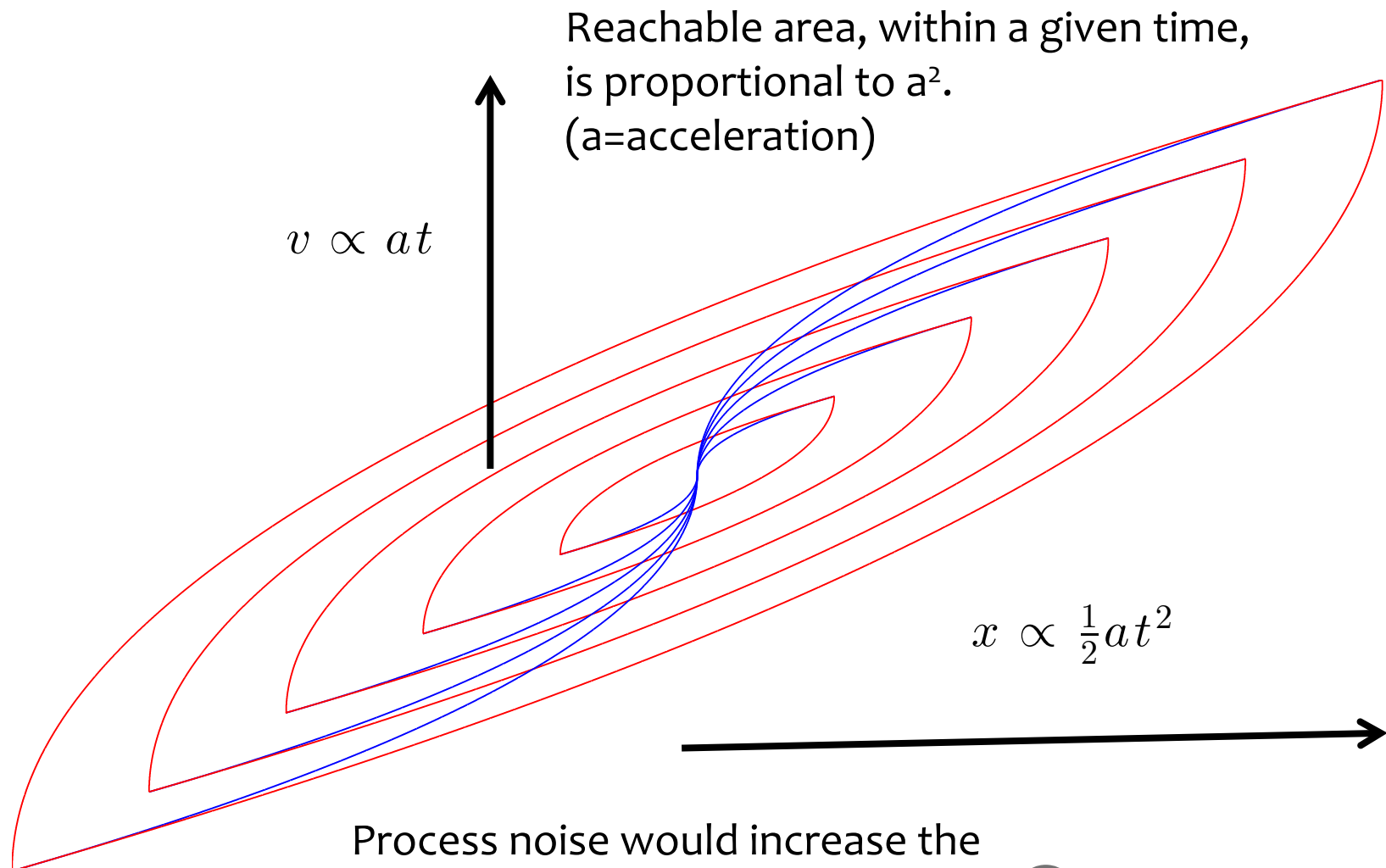
- Want to: quantify the set of states achievable in a characteristic time,
- Penalized by inaccuracies.

Coping with variable terrain is a challenge – even without uncertainty\*. Errors should be quantifiable, in terms of their impact.

[\* e.g., DARPA LittleDog program]



# Bang-bang control analogy

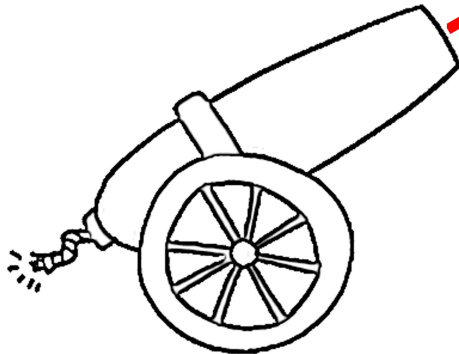


Process noise would increase the  
expected time to a goal state.

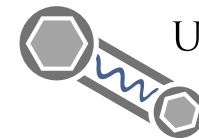
# Rock vs. Cannonball



Rock never moves.  
Zero agility, since reachable set has zero area.



- Is the cannonball better or worse?
- What if the reachable set is also just a single point? (i.e., if no variability in trajectory can be commanded)
- What if this is not entirely repeatable?



# Golf analogy

Hitting the ball further can reduce the total number of shots required.

But bad aim on a long shot will result in a greater expected number of total swings to sink the ball, on average.



In metrics for agility, effects of greater speed and greater inaccuracy should be mapped to the net effect on average “time to reach a given state” and/or “volume of states reachable in some time”.

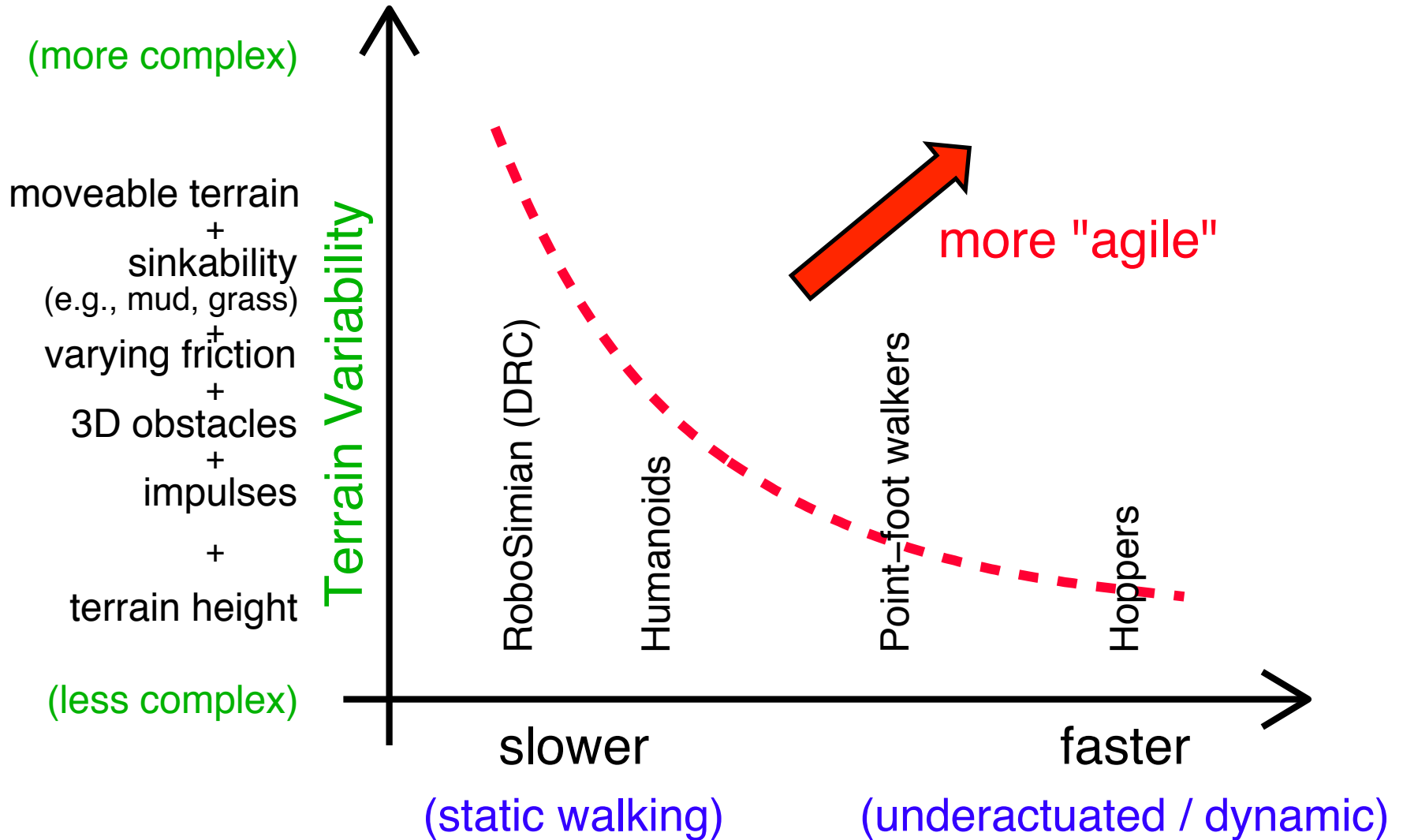
(Analogies with balancing financial risk vs reward?  
With information theory?)

# Current Agility Metrics?

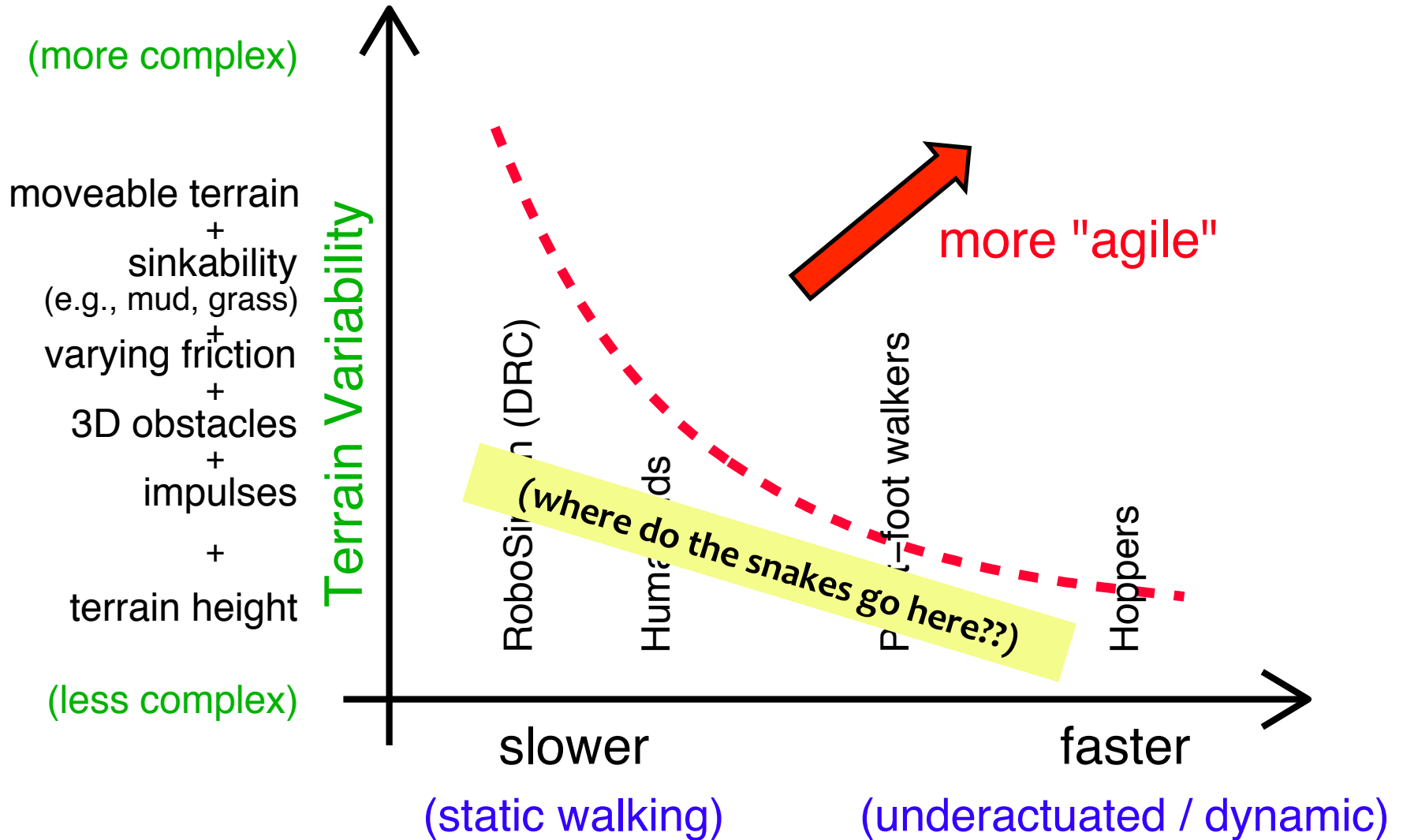
Flight dynamics and human dynamics seem to value twisting and turning...

Perhaps point-to-point mobility is more key, with turning useful iff it enables that goal.

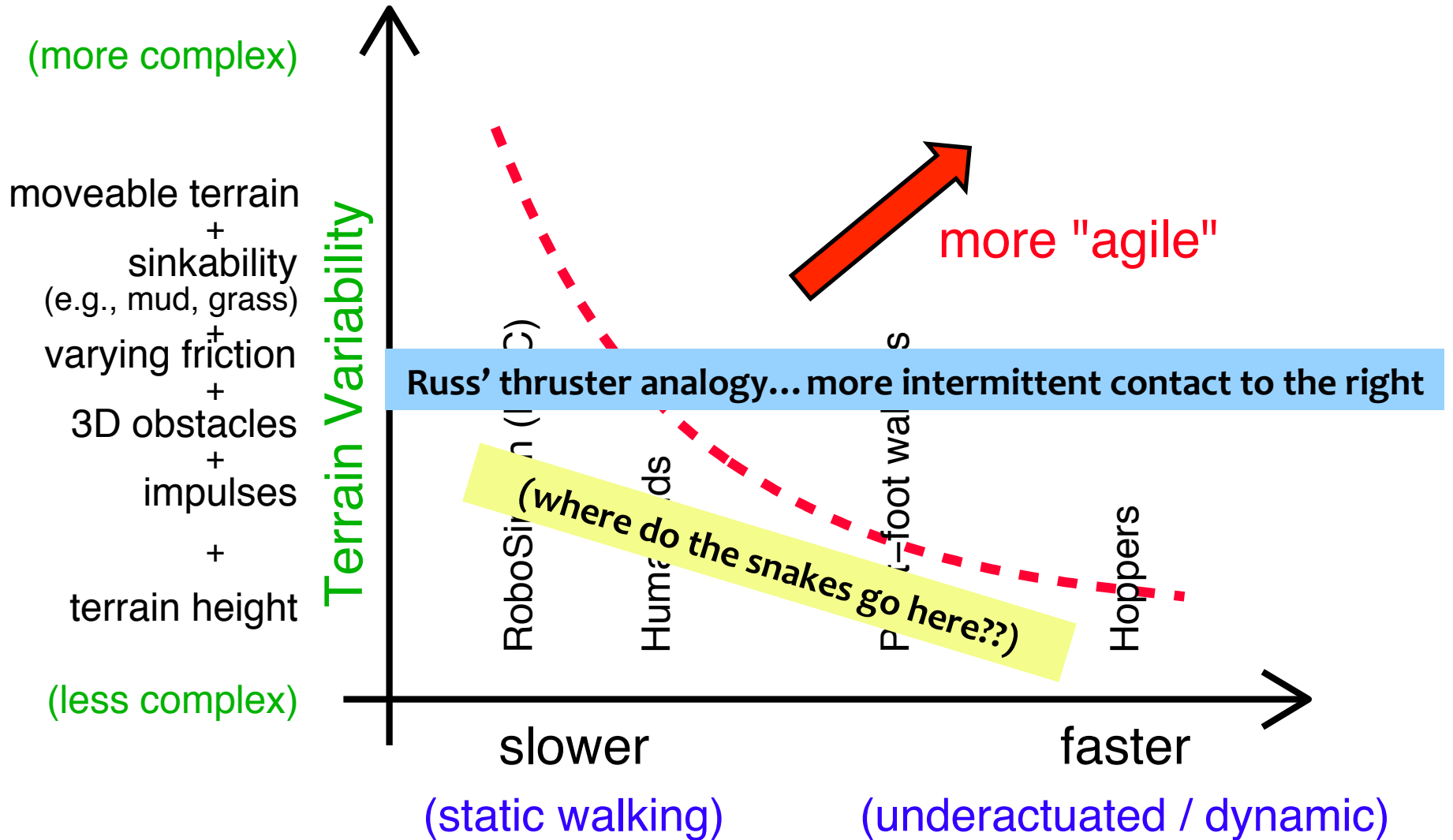
# Range of Locomotion Research



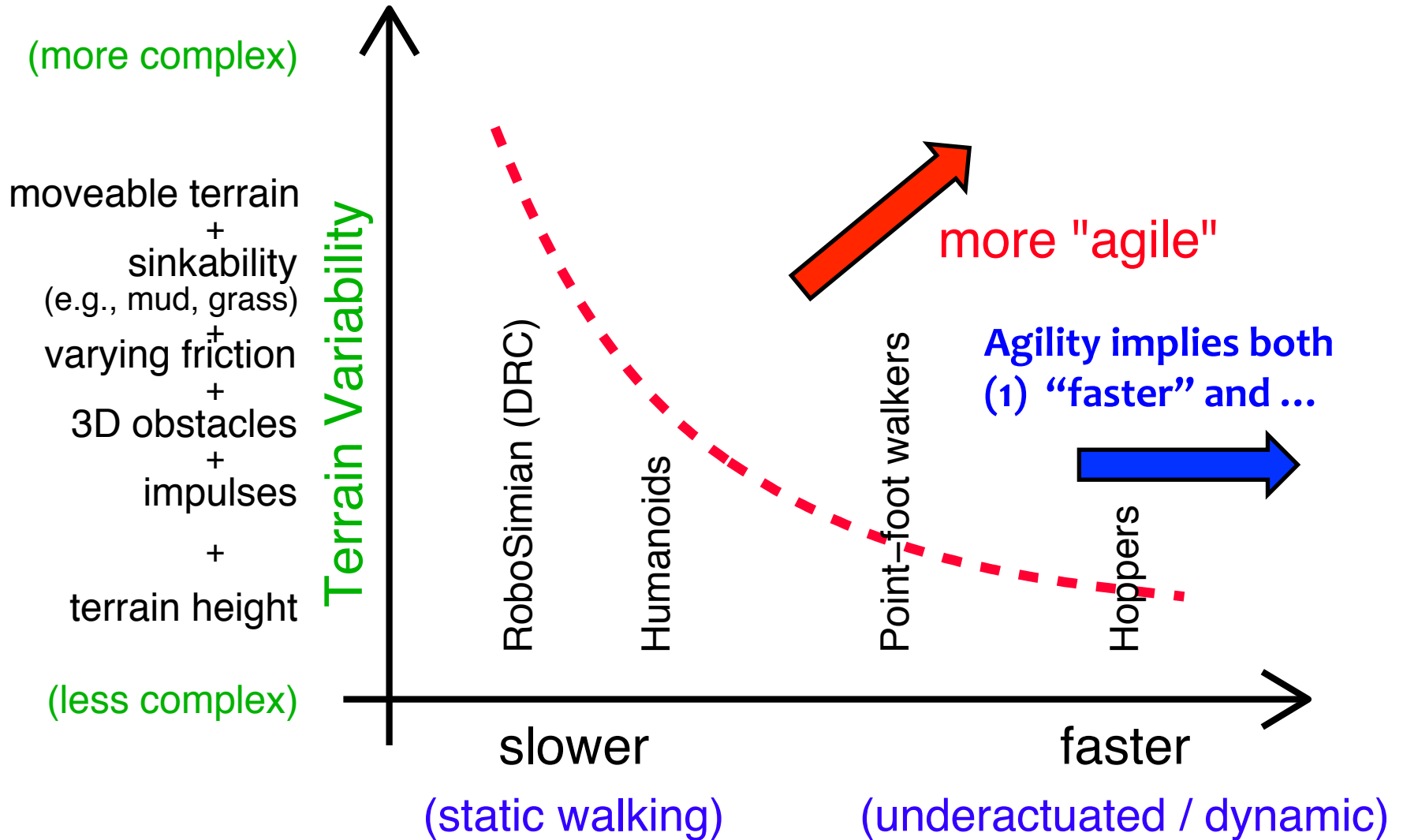
# Range of Locomotion Research



# Range of Locomotion Research

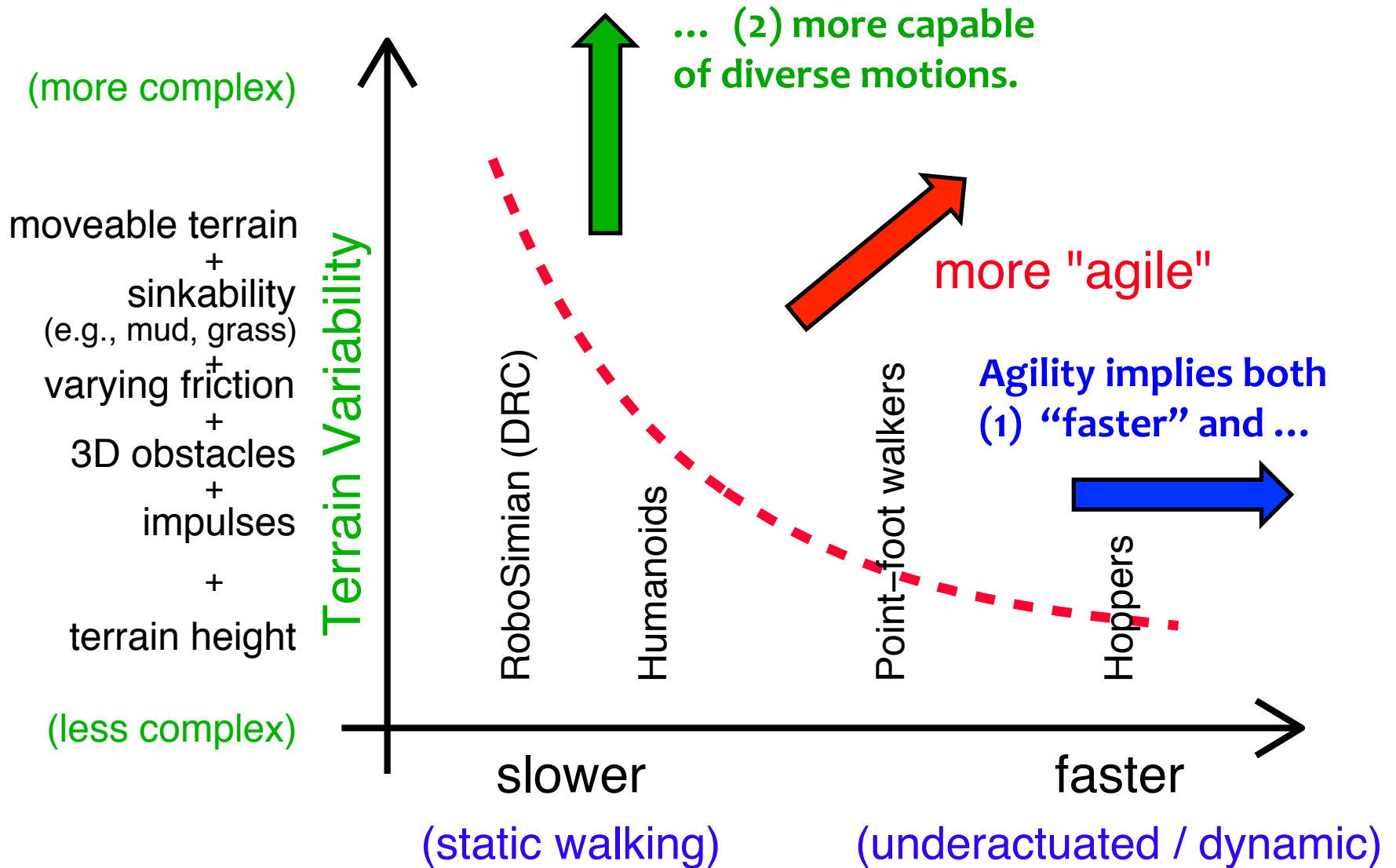


# Range of Locomotion Research

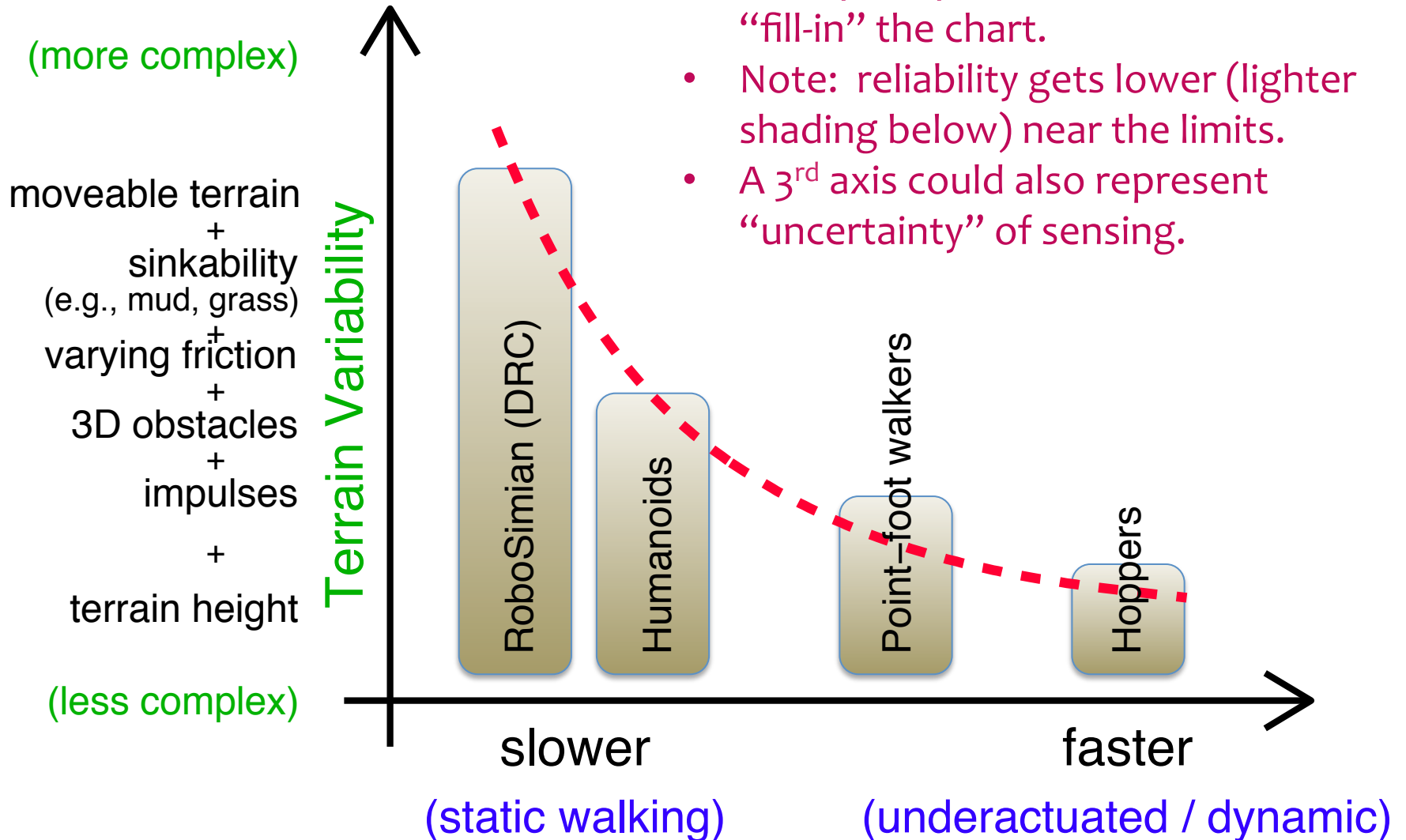




# Range of Locomotion Research

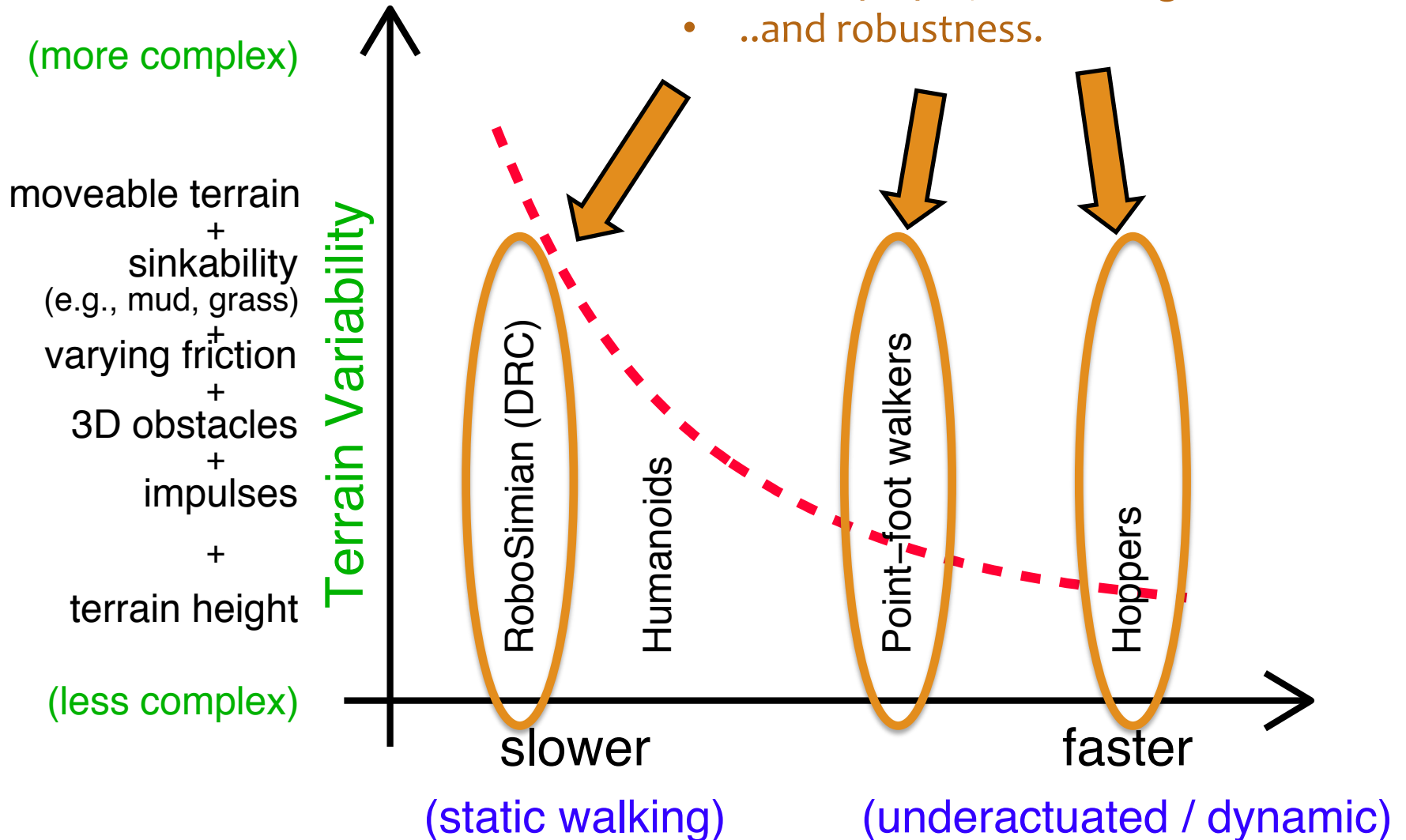


# Range of Locomotion Research



# Our Locomotion Research

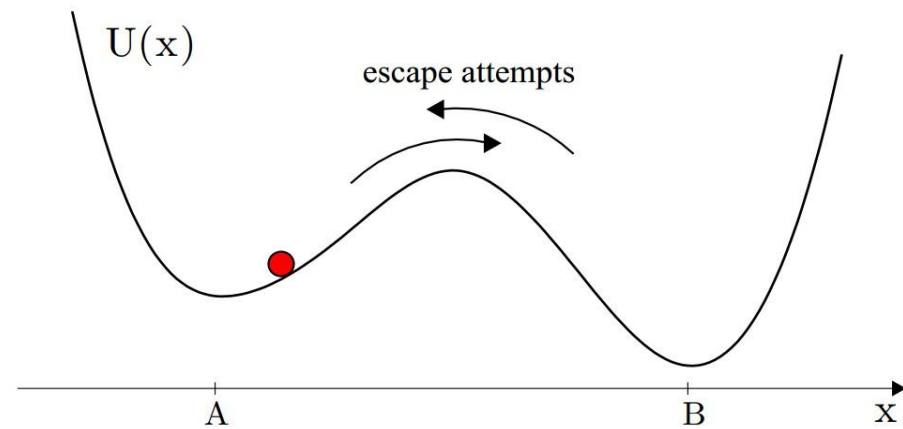
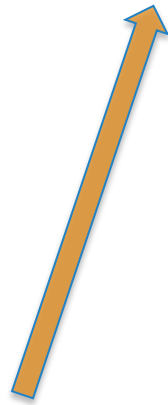
- I'll wrap up by discussing our work,
- ..and robustness.



# Robustness

# Robustness: Rarely Failing

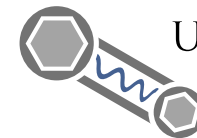
1. Achieve **metastable** locomotion



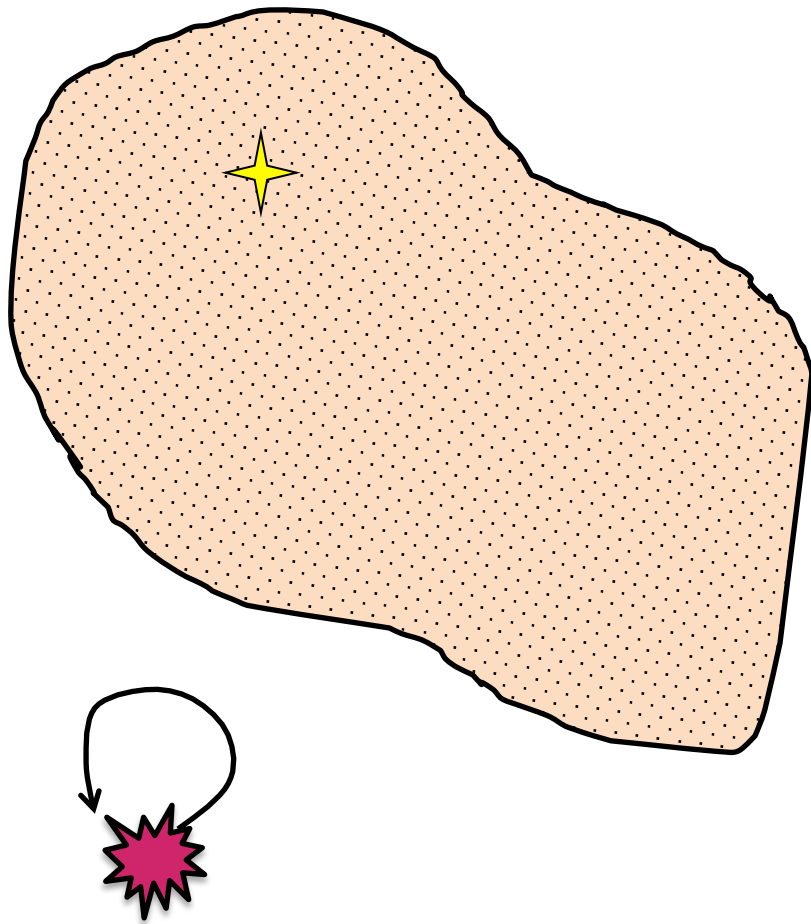
## **Metastable:**

Not strictly stable, but exhibiting long-living behaviors. (literally, “beyond stable”.)

**Probabilistic framework. Want to discretize things, to use machine learning.**

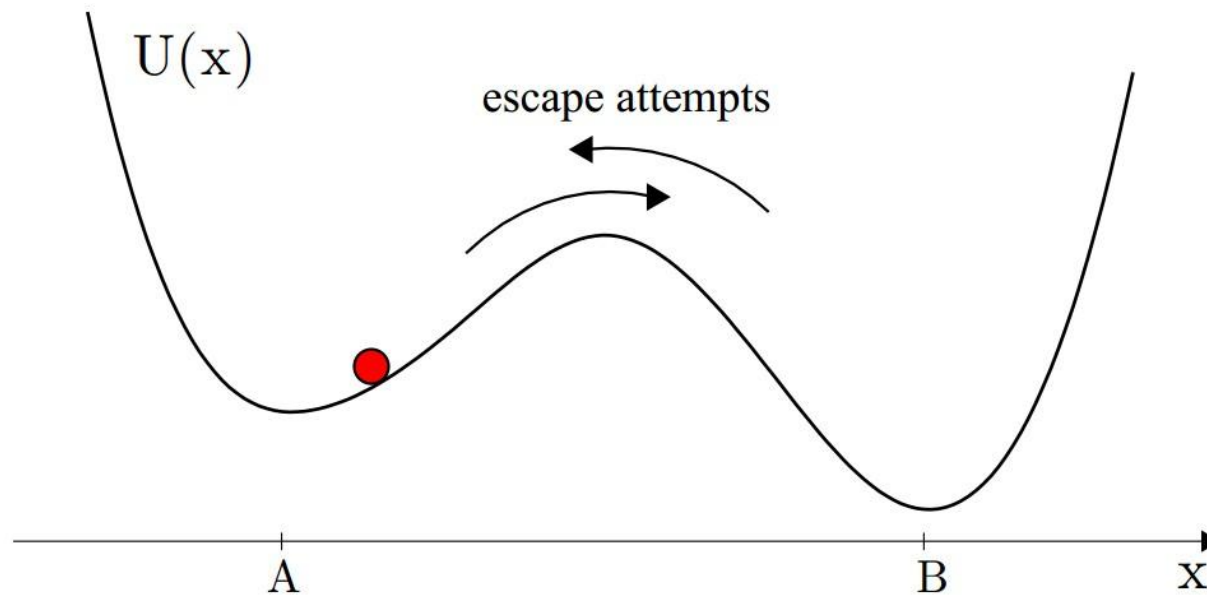


# How to estimate MFPT???



- Start with the fixed point for a given gait, on level ground.
  - Create a mesh (deterministically) of reachable (Poincare) states, i.e., of snapshots at some point of the gait cycle, given some range of variability – e.g., terrain height.
  - **This can be done, because a gait controller drives the dynamics to low-dimensional manifolds within the full state space.**
  - Build a transition matrix, which describes the stochastic dynamics of rough terrain walking.
- A single, absorbing failure state capture all failure events.

# Mean first-passage time (MFPT)



**A system-wide metric**  
(Based on 2<sup>nd</sup>-largest eigenvalue  
of transition matrix.)

$$M \approx \frac{1}{1 - \lambda_2}$$

# Look-ahead: known variability

When the terrain is flat, controller 1 is stable and the walking is periodic.

Step: 1

Controller: 1



flat terrain: stable



# Framework

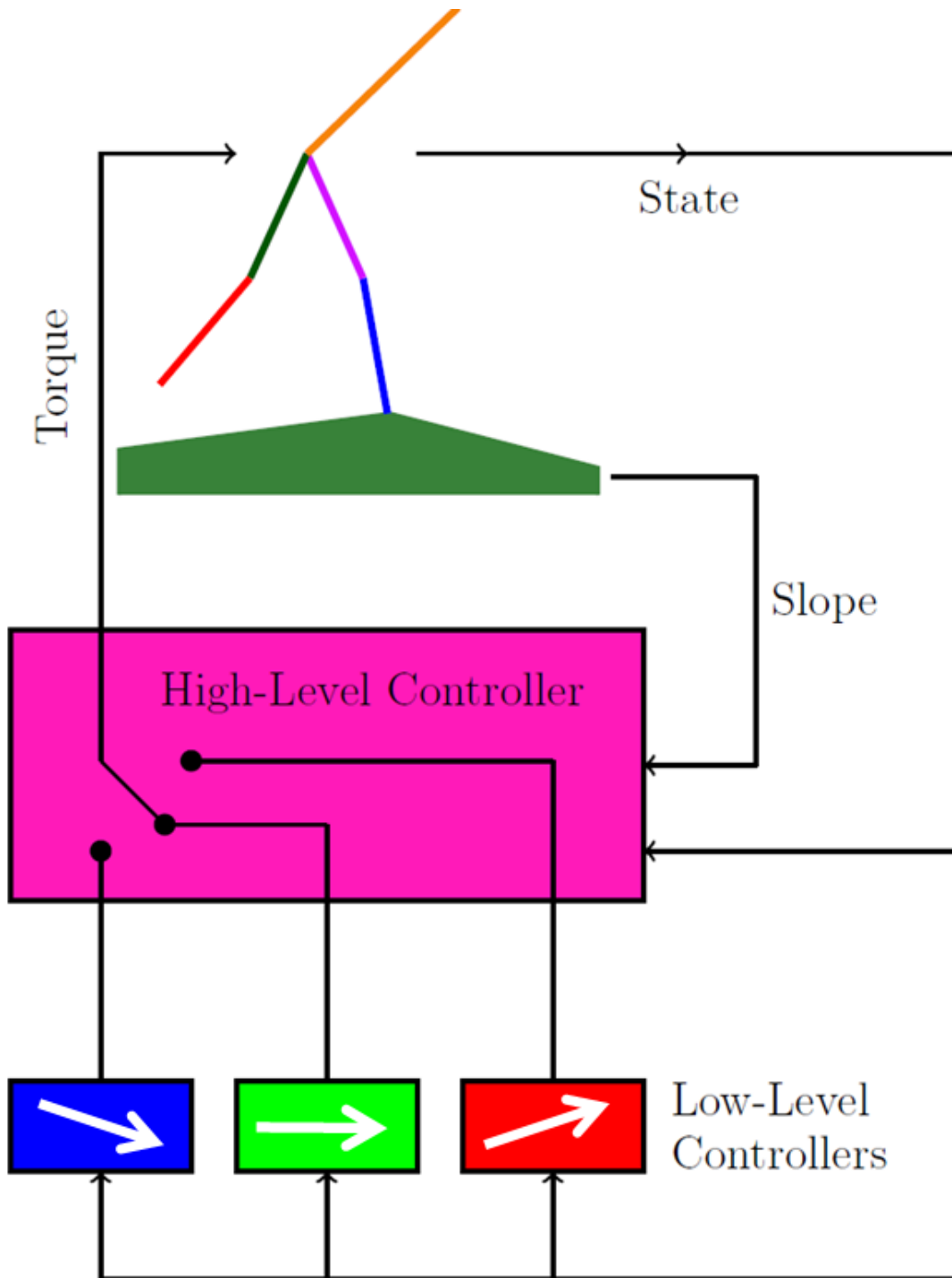
Having a robustness metric enables **OPTIMIZATION!** (that is pretty much the whole point...)

One can optimize:

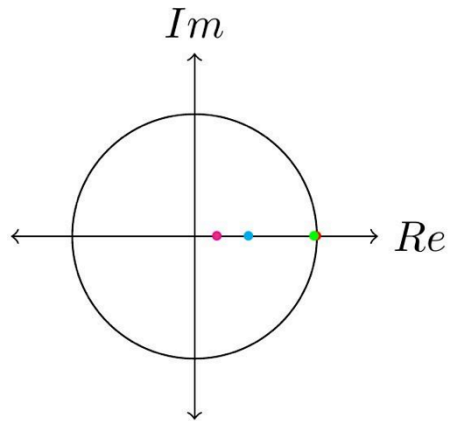
- High-level switching control
- Parameterizations of low-level controllers
- Morphology of the robot

The high-level switching policy will be globally optimal, while other searches find locally optimal solutions.

One can optimize for a metric considering MFPT *and* energy.

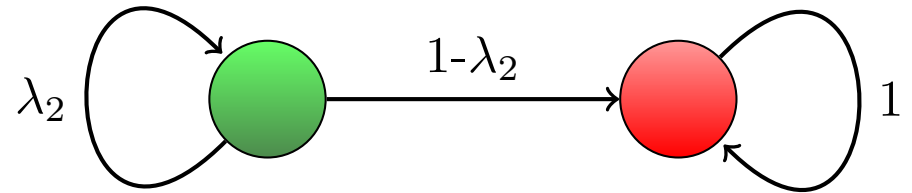


# Eigenvalues: Discrete-time system

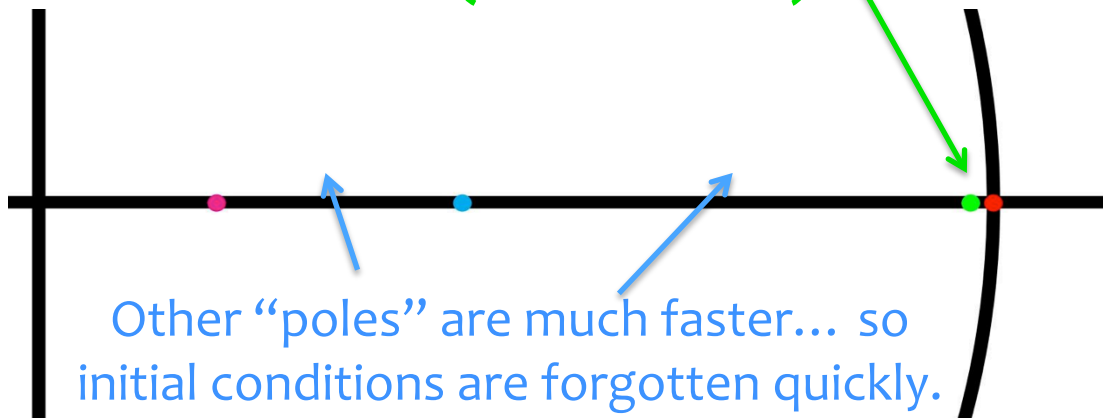


$\lambda_2$

Slow rate  
(dominant)



Metastable system is like a very biased coin toss: Usually returns to a metastable neighborhood, with very rare failures.



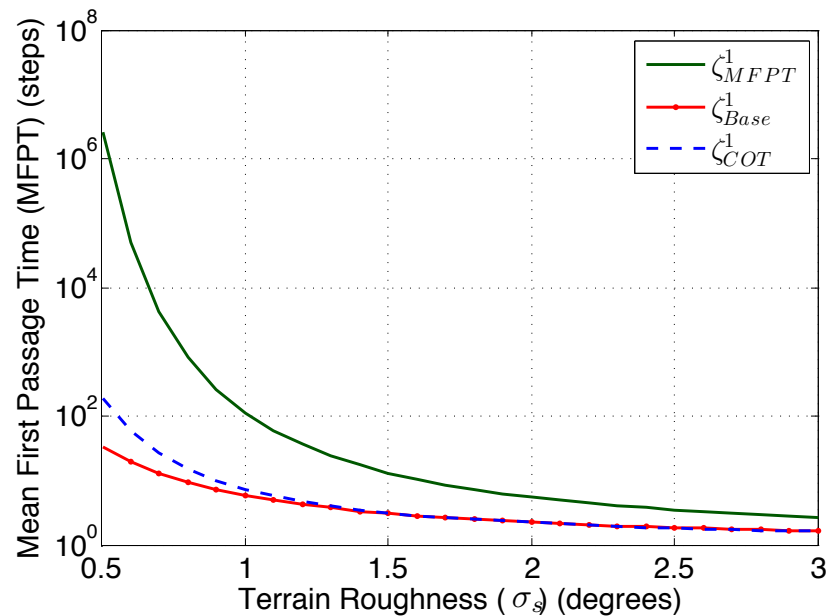
Other "poles" are much faster... so initial conditions are forgotten quickly.

# Example Benchmarking

## Optimizing each of two low-level controller

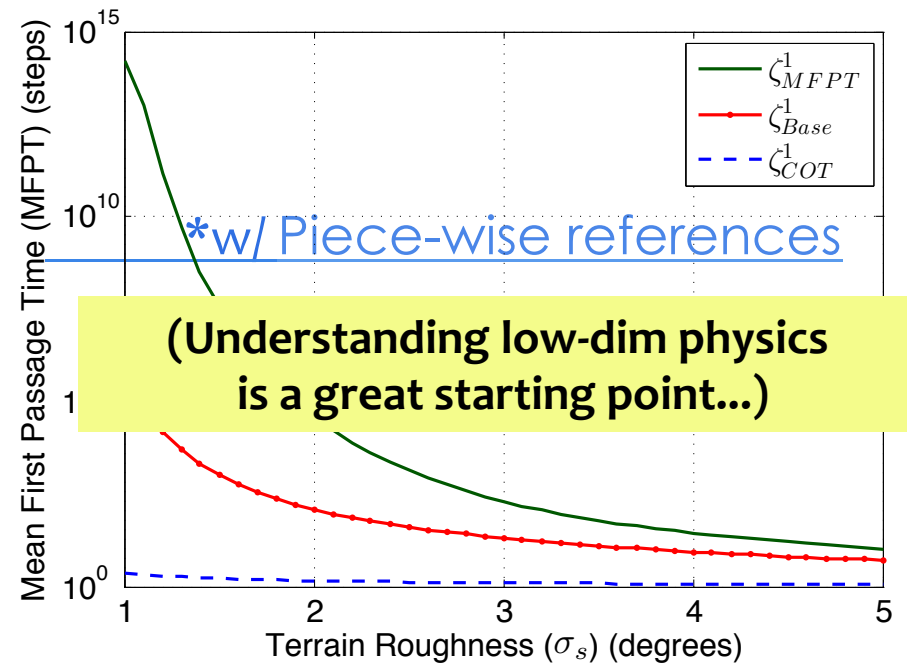
### Hybrid Zero Dynamics

Grizzle et al. (Umich)



### Sliding Mode Control\*

Saglam and Byl (UCSB)

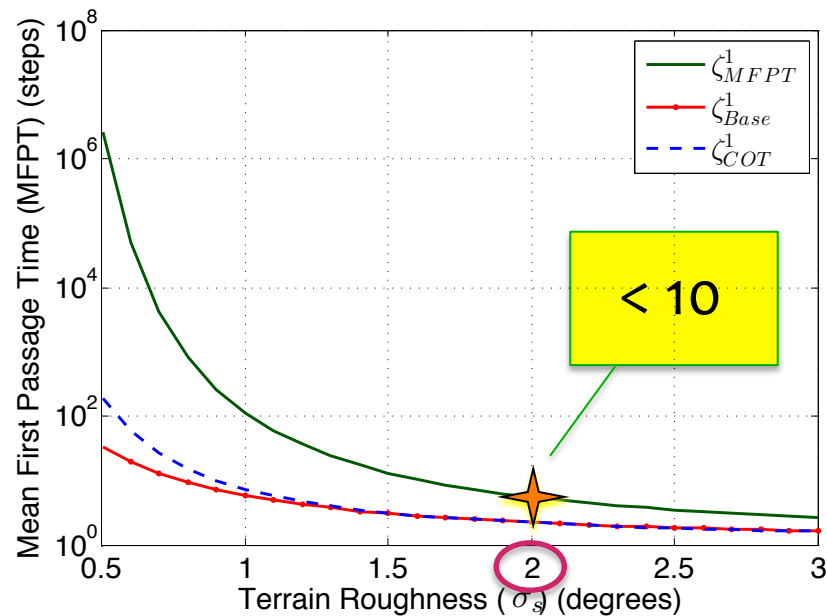


# Example Benchmarking

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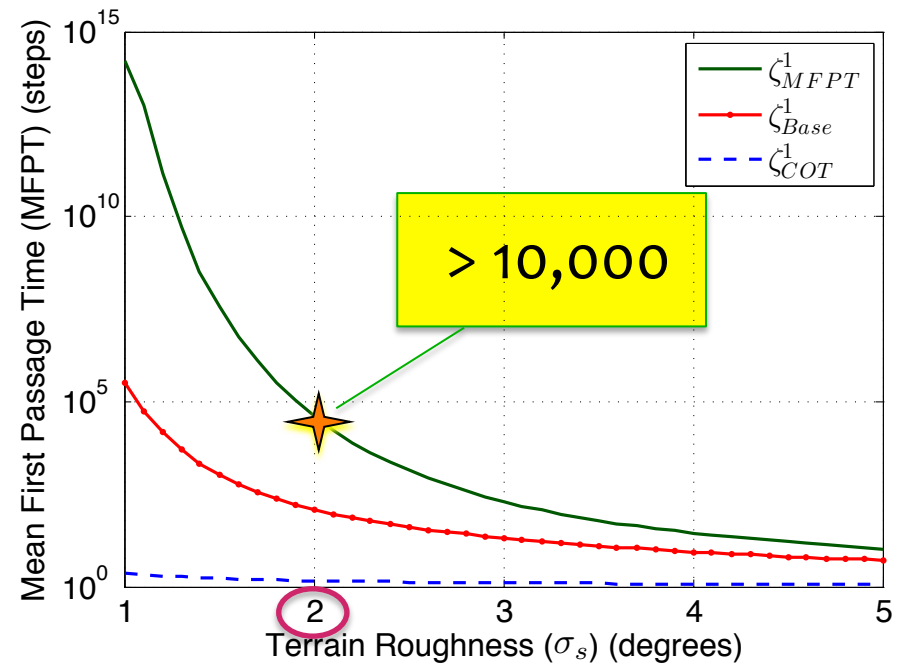
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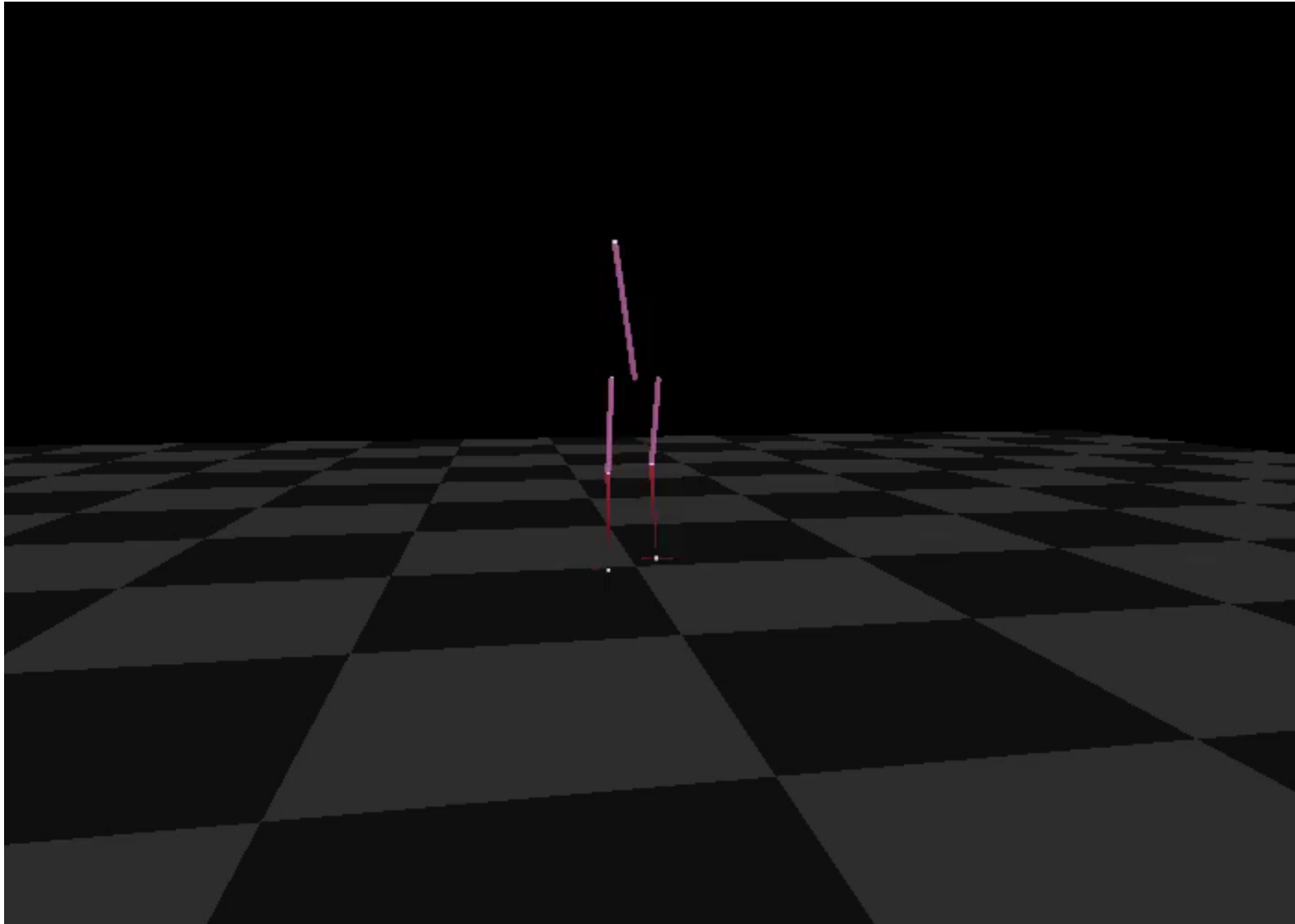


### "Sliding Mode Control"

Saglam and Byl (UCSB)



# Goal is to control higher-DOF system



MuJoCo – Emo Todorov. (Thanks Emo!!)

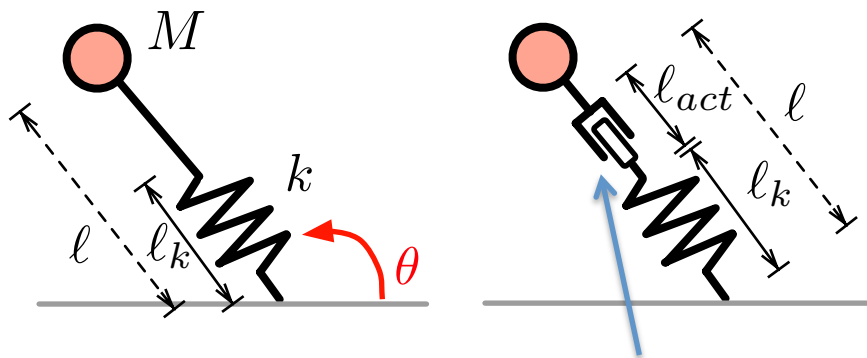
**(Understanding low-dim physics is a great starting point...)**

# Reachability

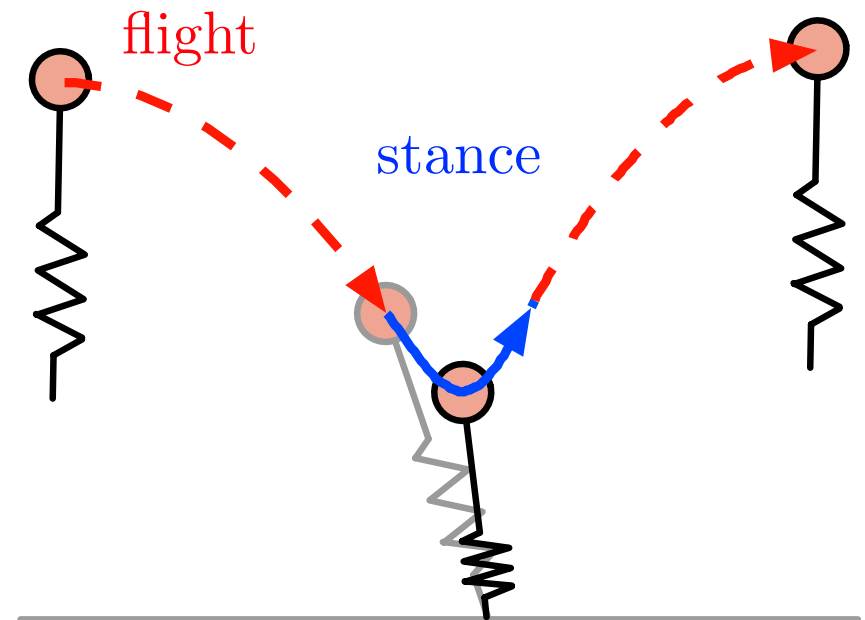
# Planar Hopper Model

Motivation: enable MPC (model predictive control), by accurately steering toward desired next apex states.

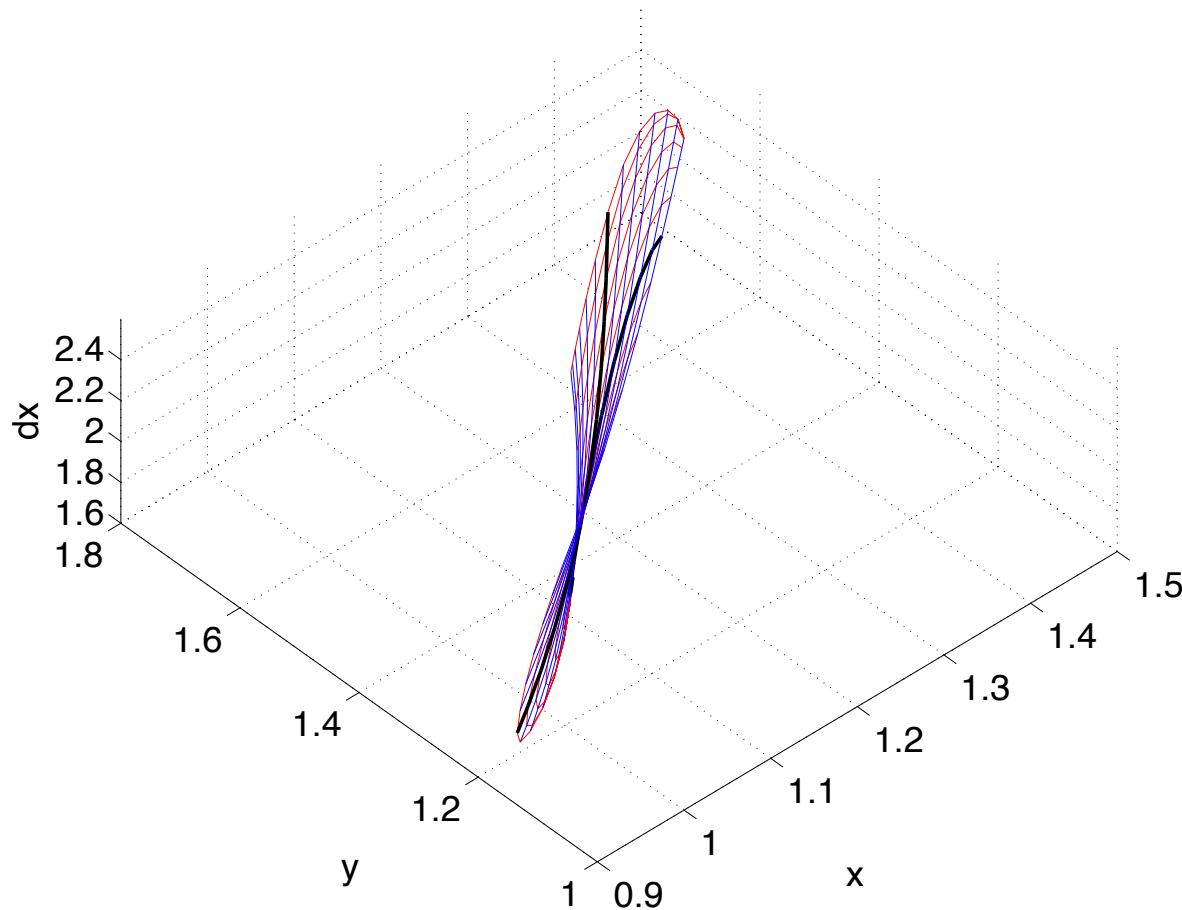
- Spring-Loaded Inverted Pendulum (**SLIP**)



**Passive vs Active**



# Reachable set ?



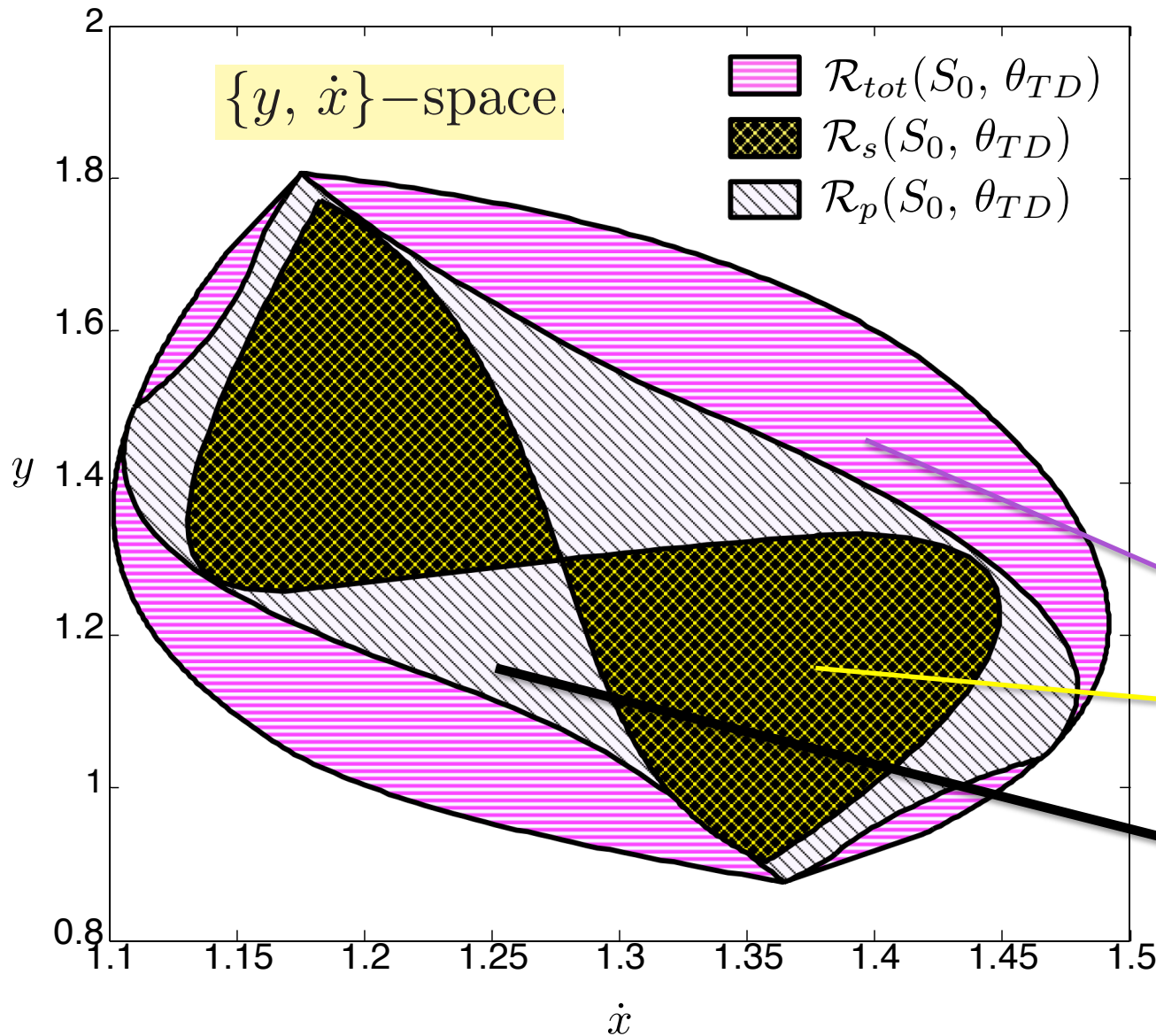
**Next apex states:**  
 $dy/dt=0$ , leaving  
 $x$ ,  $y$ , and  $dx/dt$ .

Once touch-down  
angle is set, reachable  
states for a 2D set  
(approximately).

Spanning this region  
requires 2 “knobs to  
twiddle” in active  
control during stance.



# Reachability of Control Laws



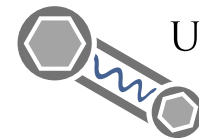
Wanted:

Ability to reach a large, open set (e.g., not a “bow-tie”). Trade-offs in computation time vs. accuracy exist.

$\mathcal{R}_{tot}$ : Full Reachable Space

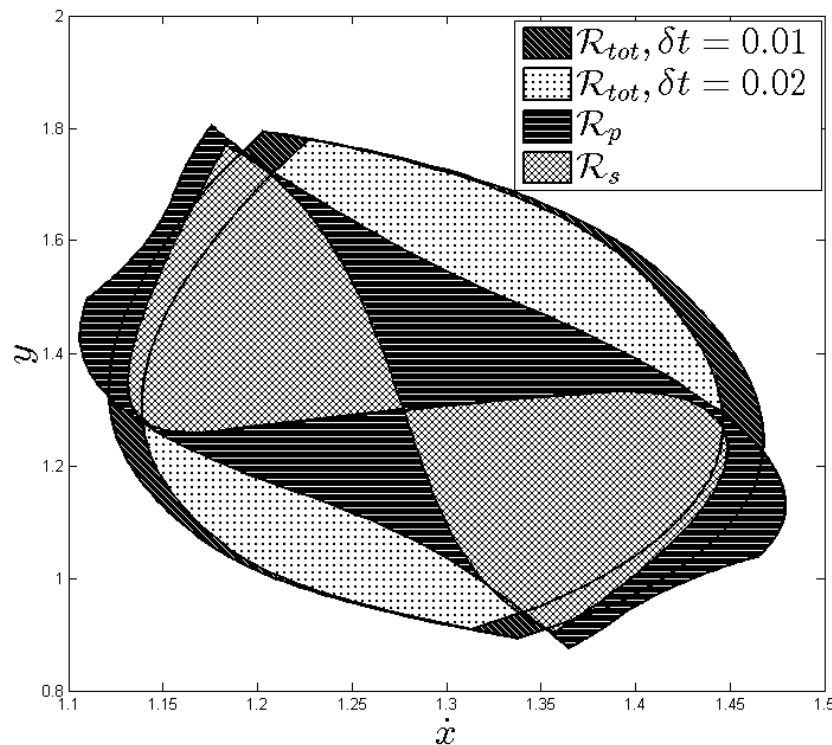
$\mathcal{R}_p$ : Schmitt/Clark (2009)

$\mathcal{R}_p$ : Piovan/Byl (2013)



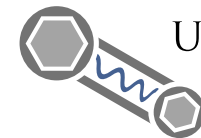
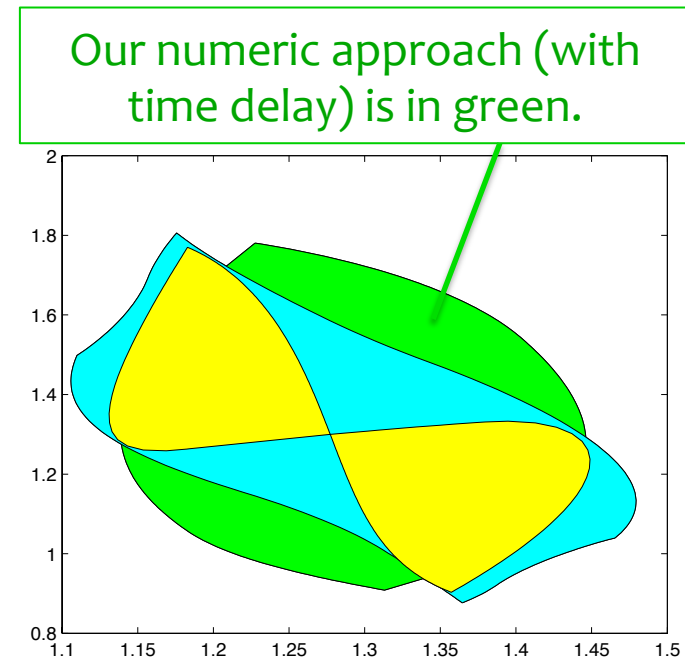
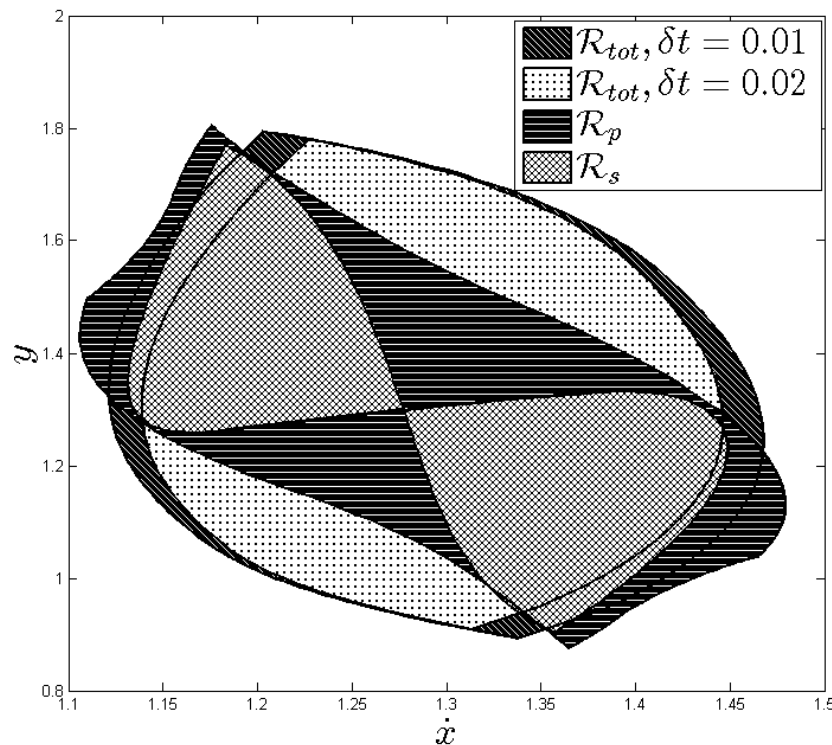
# Computational Time Delay

- Let's say we cannot act for the first  $\delta t$ , while initial computations are done.
  - Motivation: We are uncertain about terrain.



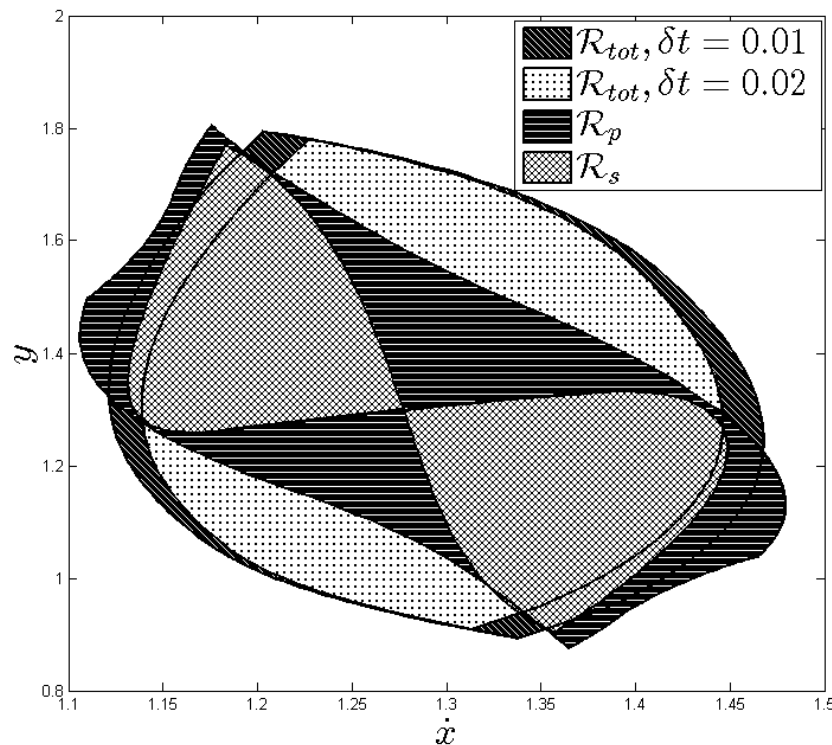
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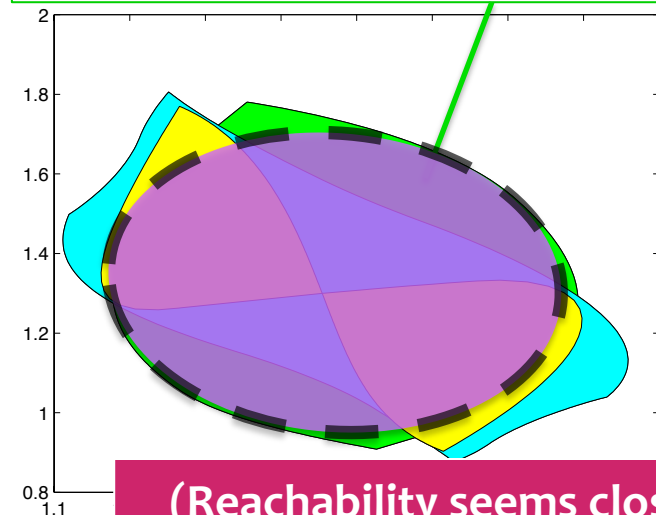


# Computational Time Delay

- Let's say we cannot act for the first  $\delta t$ , while initial computations are done.
  - Motivation: We are uncertain about terrain.



Our numeric approach (with time delay) is in green.

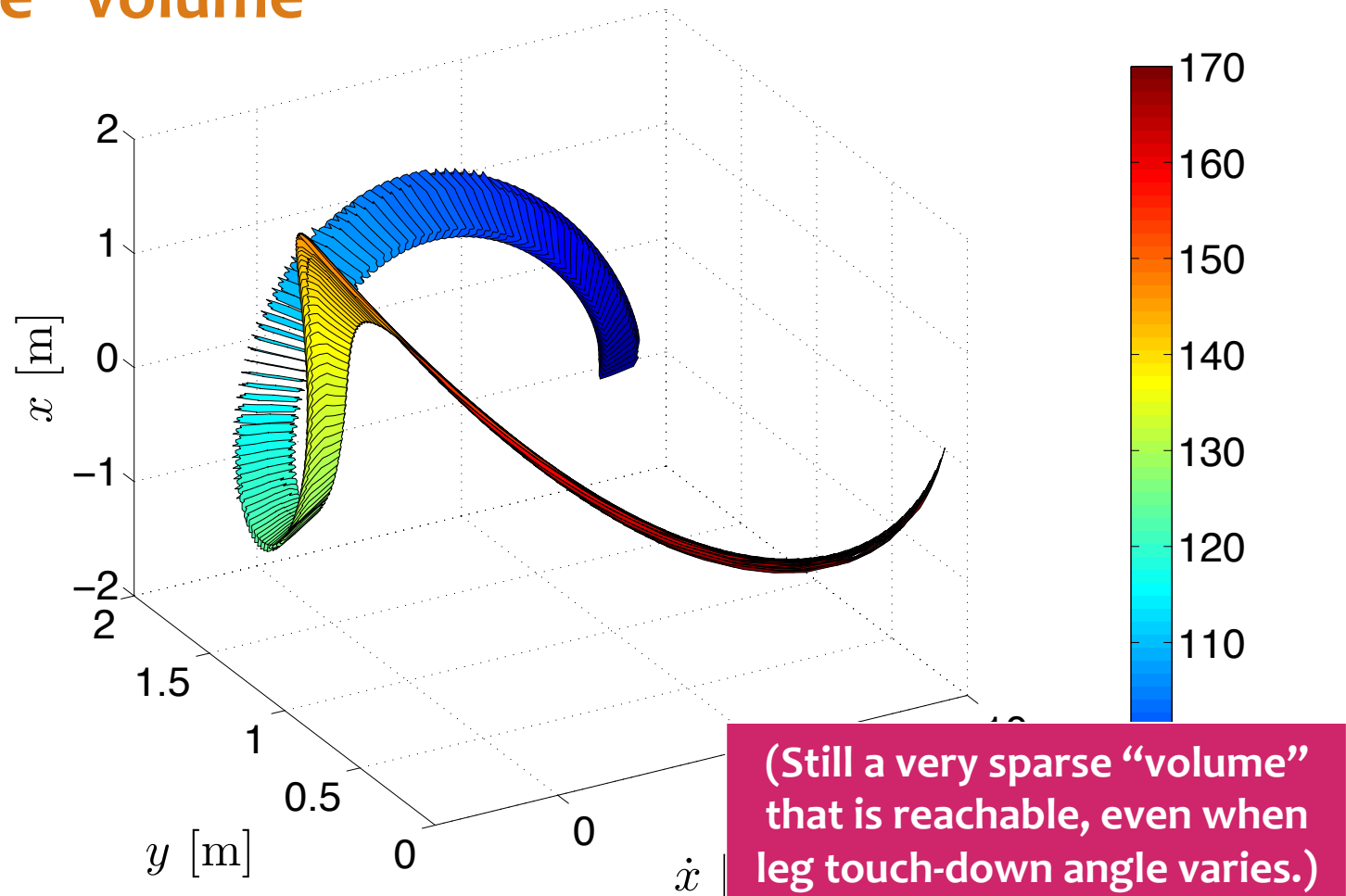


(Reachability seems closely related to “agility”... See slide 15 again.)

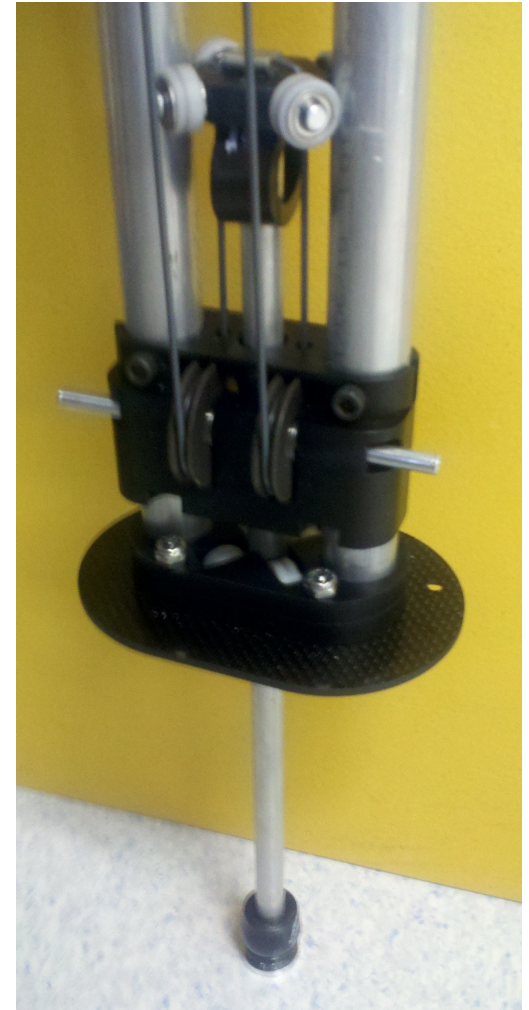
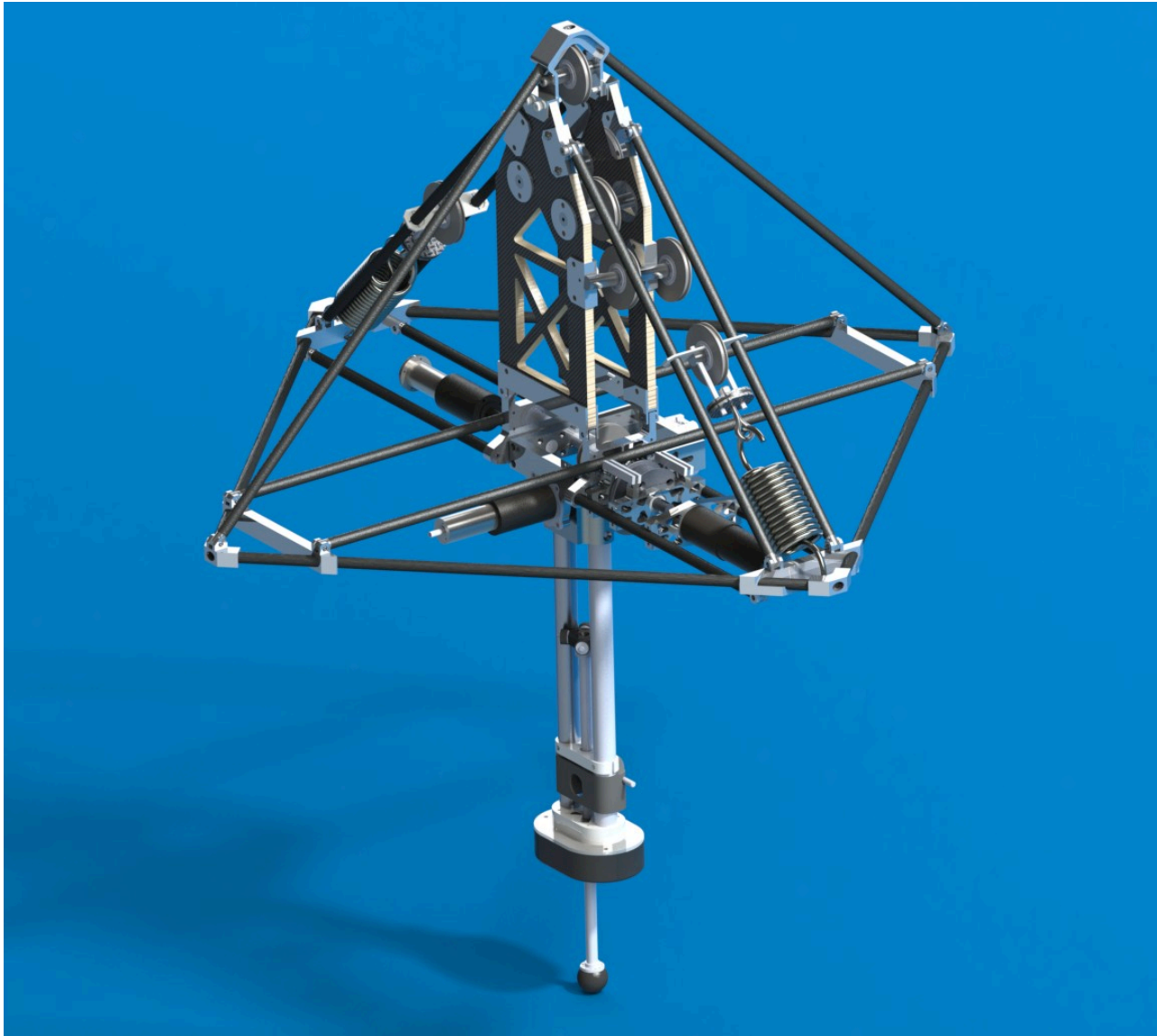


# Varying touchdown angle

- Reachable “volume”



# “Hopper C” (Jason Cortell)



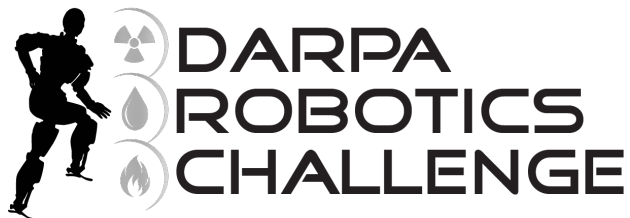


# Robustness and Agility... and the DRC?



# DARPA Robotics Challenge (DRC)

- Humanitarian Rescue, inspired by Fukushima



# FOUR TRACKS OF THE DRC



## REVIEW OF PROPOSALS (APR-OCT 2012)

- > 7 Track A teams received \$1.8M each initial DARPA funding
- > 11 Track B teams received \$375K each initial DARPA funding

## VIRTUAL ROBOTICS CHALLENGE (MAY-JUN 2013)

- > 115 Track C teams initially registered
- > 10 Track B and 16 Track C teams qualified to compete
- > 7 teams won DARPA funding and use of an Atlas robot

## CRITICAL DESIGN REVIEW (JUN 2013)

- > DARPA evaluated performance vs. proposed objectives
- > 6 teams qualified for additional DARPA funding

## SAFETY AND PERFORMANCE QUALIFICATIONS (NOV 2013)

- > 4 Track D teams qualified
- > 17 teams in all will compete in the DRC Trials

## DRC TRIALS (DEC 2013)

- > Up to 8 top teams from Tracks A/B/C will receive DARPA funding to compete in 2014 DRC Finals
- > Any team can register to compete in DRC Finals with independent funding



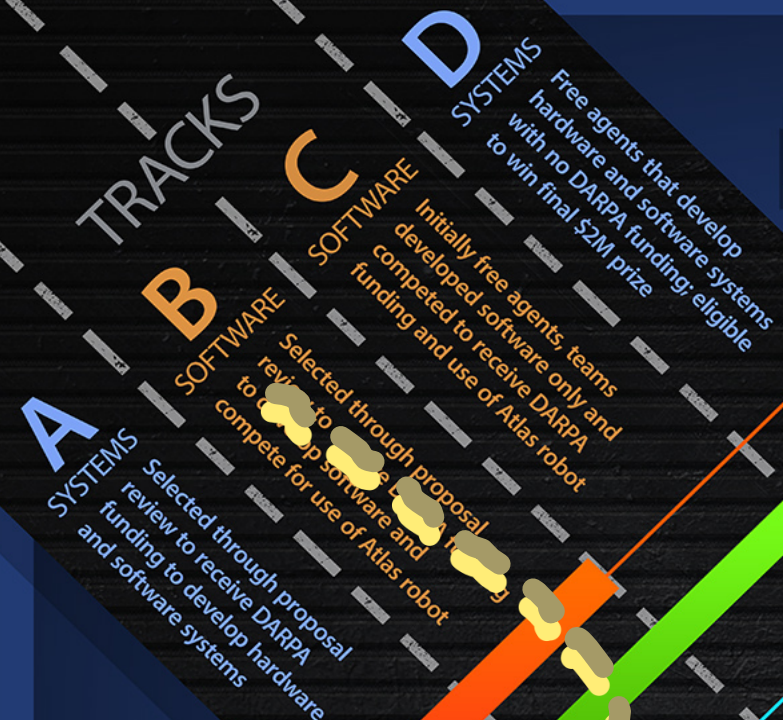
ROBOTICS  
CHALLENGE  
**2013**  
TRIALS



2014 DRC FINALS

#DARPADRC

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ROBOTICS  
CHALLENGE  
**2013**  
TRIALS

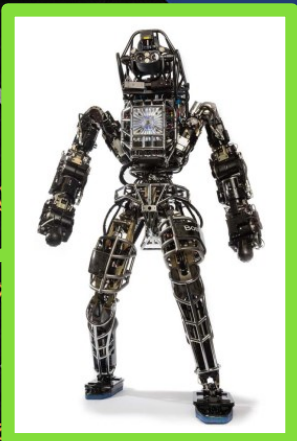


2014 DRC FINALS

#DARPADRC

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We started out on Track B...



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- > Any team can register to compete in DRC Finals with independent funding

**A** SYSTEMS Selected through proposal review to receive DARPA funding to develop hardware and software systems

**B** SOFTWARE Selected through proposal review to compete for use of Atlas robot

**C** SOFTWARE Selected through proposal review to compete for use of Atlas robot

**D** SOFTWARE Selected through proposal review to compete for use of Atlas robot



ROBOTICS CHALLENGE 2013 TRIALS



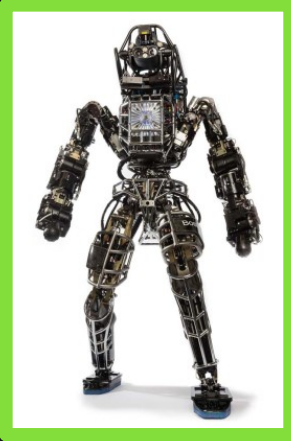
2014 DRC FINALS

2013 DRC TRIALS

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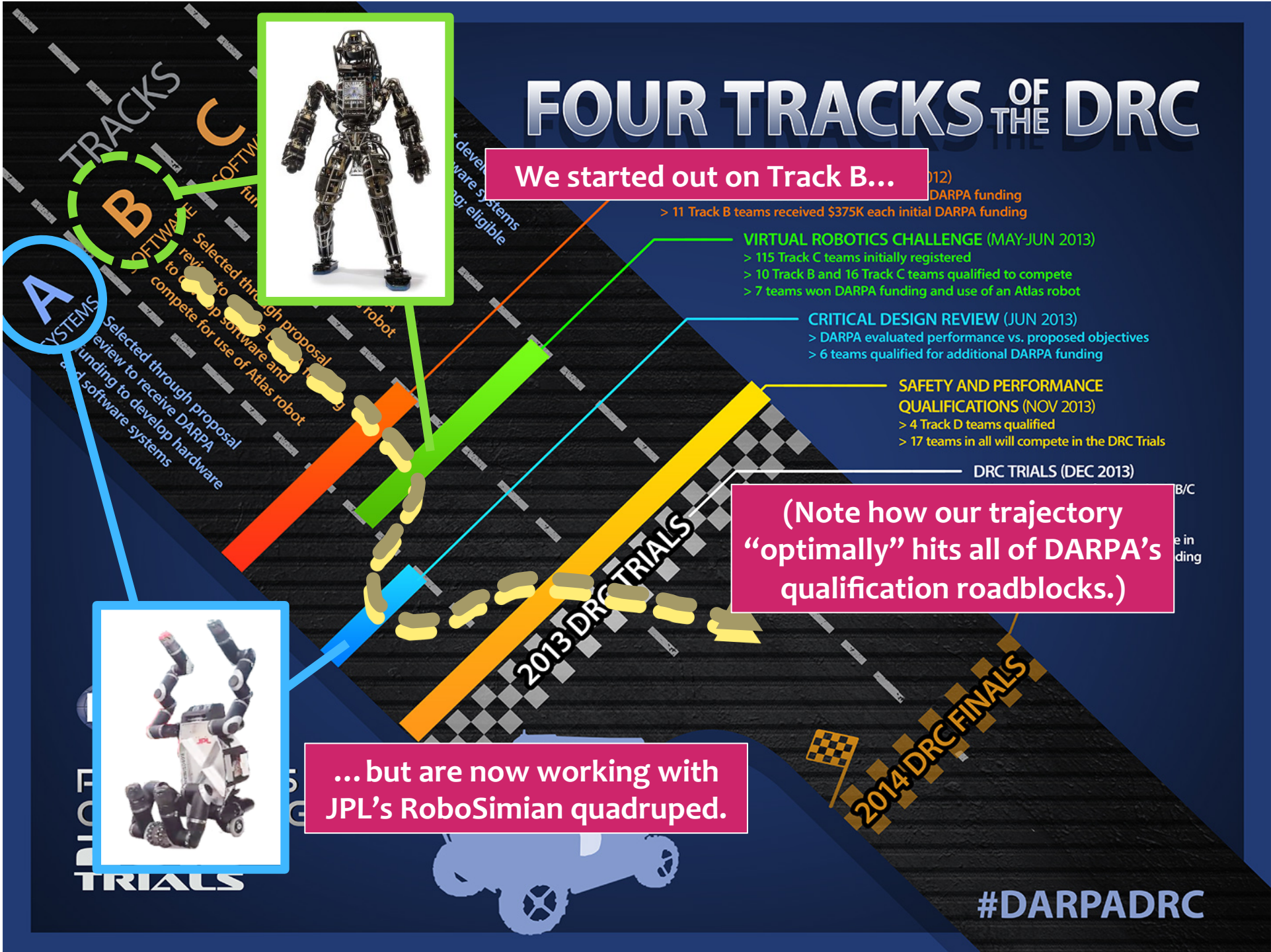
(Note how our trajectory “optimally” hits all of DARPA’s qualification roadblocks.)

...but are now working with JPL’s RoboSimian quadruped.

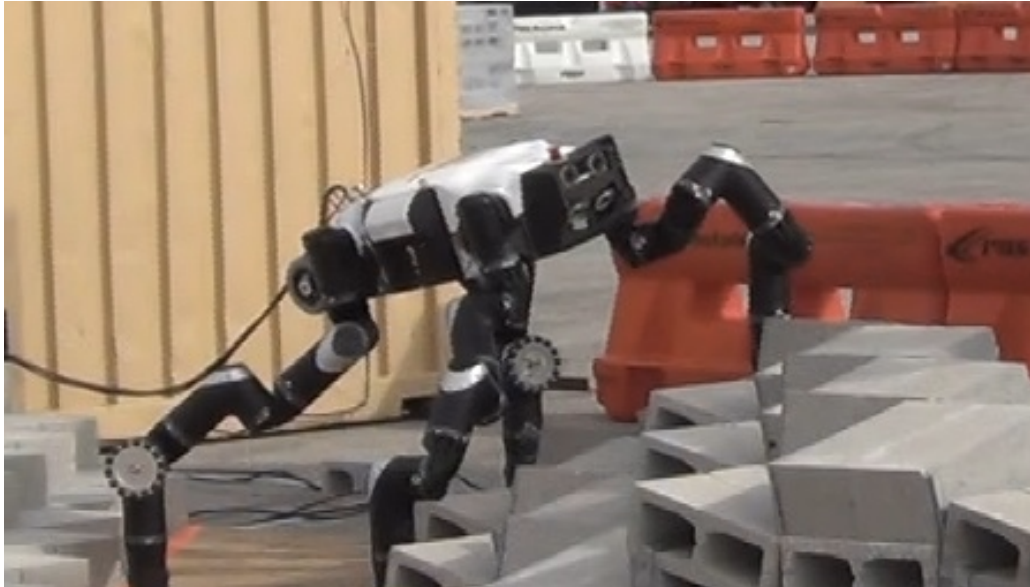


2014 DRC FINALS

#DARPADRC

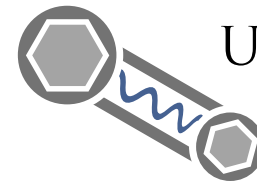


# RoboSimian



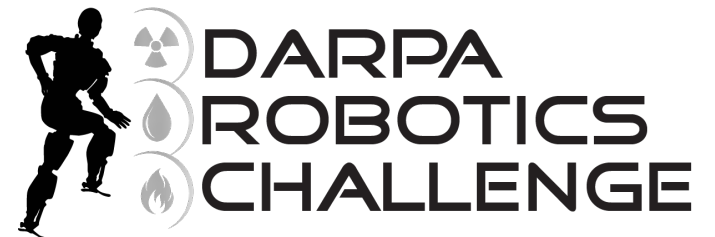
# JPL

Jet Propulsion Laboratory  
California Institute of Technology



UC SANTA BARBARA

Robotics Lab



# Asides on DRC Status

- RoboSimian's design is robust on variable terrain. As for agility: dexterous 7-DOF limbs are slow.
- JPL's approach/viewpoint (with DARPA)
  - Not trying to “game things”
  - Trying to keep “in the spirit DARPA intends”
- High robotics personnel turn-over lately...
  - Google, Apple, etc. hiring a lot of roboticists lately

And a *really* quick update...





# RoboSimian: Coping with Variability

- End-on-contact limb trajectories; then replan.
- Lot of pre-processing (e.g., kinematics):
  - IK tables map 3-DOF location (x,y,z) of end effector to 7-DOF joint solution.
  - Solutions give efficient/fast motions.
  - Designed for minimal collisions due to uncertainty.
- Very strong hands are *very* useful (occasionally).
- For very complex mobility, we're NOT generalizing “behaviors” – instead trying to demonstrate robot capabilities.

# R2T2, at UCSB: Going Up...



7x true speed.

# R2T2, at UCSB: ...and Down.



7x true speed.

# IK Tables Alone ~ Fast Walk



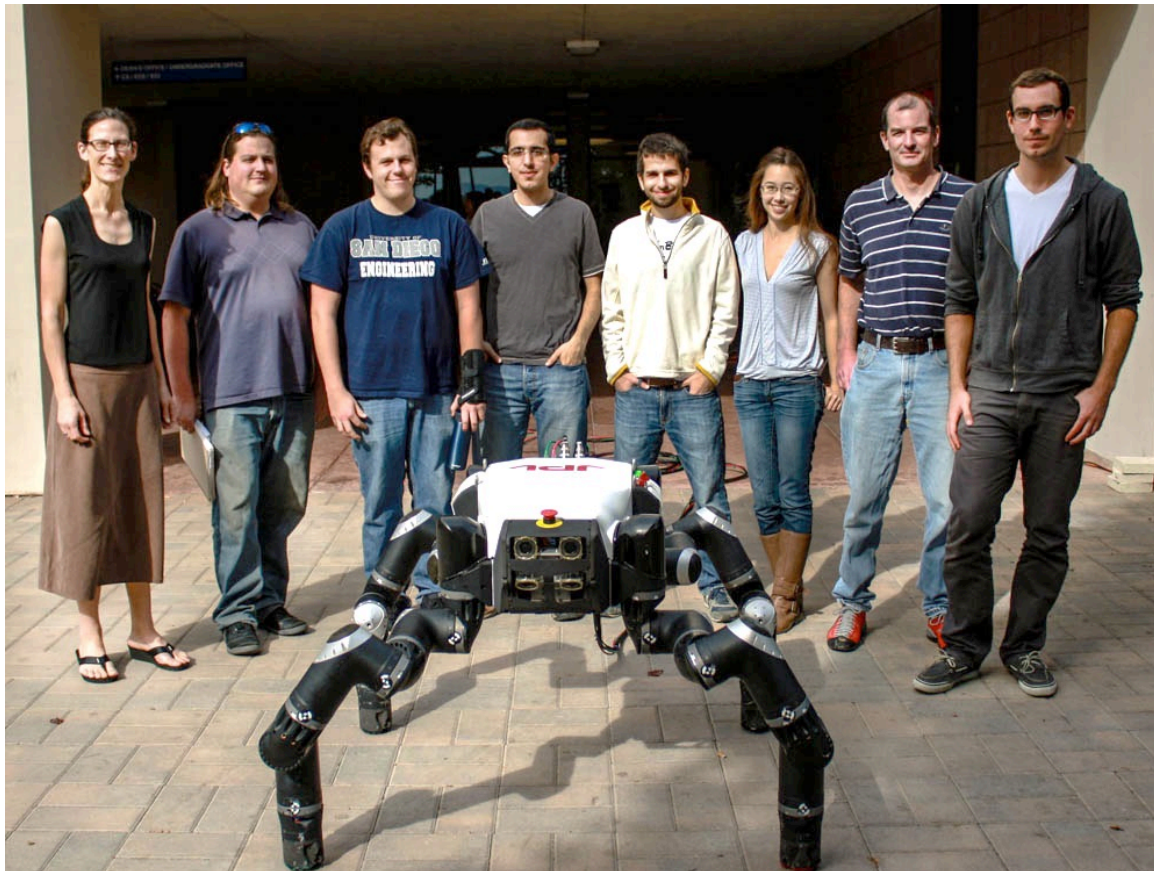
# More RoboSimian



# More RoboSimian



4150 Harold Frank Hall



Katie Byl

UCSB



# More Rabbit Agility





# Other metrics of interest

How do we quantify:

- Terrain challenge / complexity ?